| Question |  |  | Answer | Marks | Guidance |
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| 1 | (a) | (i) | KE change: $\frac{1}{2} \times 0.6 \times\left(7.5^{2}-5.5^{2}\right)$ $=7.8 \mathrm{~J}$ <br> GPE change: $0.6 \times 9.8 \times 1.5=8.82 \mathrm{~J}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { B1 } \\ & \text { [3] } \end{aligned}$ | Difference of two KE terms <br> Allow -8.82J |
| 1 | (a) | (ii) | $W$ is work done against resistance $\begin{aligned} & 7.8=8.82-W \\ & \text { so } W=1.02 \mathrm{~J} \end{aligned}$ | M1 <br> A1 <br> [2] | W-E all terms. Allow sign errors FT (i) only. Also FT only if mod (their KE) $<\bmod$ (their PE) -1.02 gets M1A0; 16.62 gets M1A0 |
| 1 | (a) | (iii) | Average resistance is $F$ <br> so $F \times 1.5=1.02$ <br> so $F=0.68$ <br> Power is $0.68 \times 5.5$ $=3.74 \text { so } 3.74 \mathrm{~W}$ | M1 <br> A1 <br> M1 <br> A1 <br> [4] | Use of WD $=F s$ OR find $a=8.667$ and use $\mathrm{F}=0.6 g-0.6 \times 8.667$ May be implied. FT (ii) <br> Use of $P=F v$ any calculated F cao |
| 1 | (b) | (i) | $\begin{aligned} & R=m g \cos 40 \\ & F_{\max }=m g \sin 40 \\ & F_{\max }=\mu R \\ & \text { so } \mu=\frac{m g \sin 40}{m g \cos 40}=\tan 40 \end{aligned}$ | B1 <br> B1 <br> M1 <br> E1 <br> [4] | Seen or implied <br> Seen or implied <br> Use of $F=\mu R$ : substitute $F$ and $R$ <br> This is the minimum amount of working needed to earn the E1 <br> Must see explicit evidence of method <br> Note: $g$ omitted, treat as MR |
| 1 | (b) | (ii) | EITHER $\begin{aligned} & \tan 40 \times 0.8 \times 9.8 \times \cos 20 \\ & \times 3(=18.545) \\ & (+) 0.8 \times 9.8 \\ & \times 3 \sin 20(=8.044) \\ & =26.5897 \ldots \text { so } 26.6 \mathrm{~J}(3 \text { s.f. }) \end{aligned}$ | B1 <br> M1 <br> B1 <br> M1 <br> A1 | Use of $F_{\text {max }}=\mu R$ with tan 40 and $\cos 20$ <br> Use of WD = Fs NOTE: This mark may be awarded here or for use in PE term <br> Use of $m g h \quad$ Allow sin $\leftrightarrow$ cos interchange <br> Two relevant terms added <br> Cao Allow 26.7 Allow 27 <br> Omission of $g$ can get B0M1B1M1A0 |


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|  |  |  | $\begin{aligned} & \text { OR } \\ & \tan 40 \times 0.8 \times 9.8 \times \cos 20(=6.182) \\ & (+) 0.8 \times 9.8 \times \sin 20(=2.68) \\ & (=8.8632444 \ldots) \\ & \text { WD is } 3 \times 8.8632444 \ldots \\ & =26.5897 \ldots \text { so } 26.6 \mathrm{~J}(3 \text { s.f. }) \end{aligned}$ | B1 <br> B1 <br> M1 <br> M1 <br> A1 <br> [5] | Use of $F_{\max }=\mu R$ with tan 40 and $\cos 20$ <br> Allow $\sin \leftrightarrow$ cos interchange <br> Two relevant forces added <br> Use of WD = Fs (for at least one of forces) <br> cao <br> Omission of $g$ can get B0B1M1M1A0 |
| 2 | (i) |  | $\begin{aligned} & \text { a.c. moments about B } \\ & 10 T_{\mathrm{C}}-15 \times 2=0 \\ & \text { so } T_{\mathrm{C}}=3 \text {. Tension at } \mathrm{C} \text { is } 3 \mathrm{~N} \\ & \uparrow T_{\mathrm{C}}+T_{\mathrm{B}}-15=0 \\ & \text { so } T_{\mathrm{B}}=12 \text {. Tension at } \mathrm{B} \text { is } 12 \mathrm{~N} \end{aligned}$ | M1 <br> A1 <br> M1 <br> F1 <br> [4] | Moments with all forces present, no extra forces. <br> May take moments again |
| 2 | (ii) |  | a.c. moments about A $25 T \sin 30-15 \times 17=0$ <br> so $T=20.4$ <br> At A Let force $\uparrow$ be $Y \mathrm{~N}$ $\begin{aligned} & \uparrow Y+T \sin 30-15=0 \text { so } Y=4.8 \\ & \rightarrow X=T \cos 30=17.6669 \ldots \mathrm{~N} \\ & \sqrt{4.8^{2}+(T \cos 30)^{2}} \\ & =18.3073755 \ldots \text { so } 18.3 \mathrm{~N}(3 \text { s.f. }) \end{aligned}$ | $\begin{gathered} \text { M1 } \\ \text { A1 } \\ \text { B1 } \\ \text { B1 } \\ \text { M1 } \\ \text { A1 } \\ {[6]} \end{gathered}$ | Attempt at moments with resolution; allow $\cos \leftrightarrow \sin$ error. All forces present, no extra forces <br> cao <br> FT (can take moments about C) <br> FT Need not be evaluated <br> cao |
| 2 | (iii) |  | Let force be $P$. <br> a.c. moments about D. $8 \times 15-12 \times P=0$ <br> so $P=10$ on point of tipping <br> Using $F_{\max }=\mu R$ on point of slipping <br> with $R=15$ <br> gives $F_{\max }=0.65 \times 15=9.75$ <br> so slips first | M1 <br> A1 <br> M1 <br> B1 <br> A1 <br> E1 <br> [6] | Moments about $D$ with all forces present, no extra forces cao <br> cao <br> cao and WWW |


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| 3 | (a) | (i) | $300\binom{\bar{x}}{\bar{y}}=72\binom{-6}{3}+192\binom{4}{-6}+36\binom{10}{-4}$ $\begin{aligned} & \binom{\bar{x}}{\bar{y}}=\binom{696}{-1080} \\ & \text { so } \bar{x}=2.32 \\ & \bar{y}=-3.6 \end{aligned}$ | B1 <br> M1 <br> B1 <br> A1 <br> A1 <br> [5] | Correctly identifying the position of the c.m of triangle EFH $(10,-4)$ <br> A systematic method for at least 1 cpt <br> Either all $x$ or all $y$ values correct or 2 vector terms correct or allow one common error in both components, e.g. one wrong mass, misunderstanding of c.m. of triangle <br> Allow FT for either if only error is common to both |
| 3 | (a) | (ii) | centre of mass is at G $\begin{aligned} & \tan \alpha=\frac{9.6}{1.43} \\ & \text { so } \alpha=33.8376 \ldots \text { so } 33.8^{\circ}(3 \text { s.f. }) \end{aligned}$ |  | Identifying correct angle. May be implied At least 1 relevant distance found. FT (i) Use of $\arctan \frac{9.6}{14.32}$ or $\arctan \frac{14.32}{9.6}$ o.e. cao or $180^{\circ}-33.8^{\circ}$ |
| 3 | (b) | (i) | Marking given tension and thrust Marking all other forces internal to rods acting on $\mathrm{A}, \mathrm{B}$ and C (as T or C ) | $\begin{aligned} & \text { B1 } \\ & \text { B1 } \\ & \text { [2] } \end{aligned}$ | Each labelled with magnitude and correct direction <br> Need ALL forces at $A, B$ and $C$. Need pairs of arrows on $A B, A C$ and $B C$ |


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| 3 | (b) | (ii) | Equilibrium at $\mathrm{A} \uparrow$ $T_{\mathrm{AB}} \cos 30-18=0$ <br> $T_{\mathrm{AB}}=12 \sqrt{3}$. Force in AB: $12 \sqrt{3} \mathrm{~N}(\mathrm{~T})$ <br> $\mathrm{A} \leftarrow$ $\begin{aligned} & T_{\mathrm{AC}}+T_{\mathrm{AB}} \cos 60+5=0 \\ & T_{\mathrm{AC}}=-(5+6 \sqrt{3}) . \end{aligned}$ <br> Force in AC: $(5+6 \sqrt{3}) \mathrm{N}(\mathrm{C})$ <br> At $B$ in direction $A B$ $T_{\mathrm{BR}} \cos 60-T_{\mathrm{AB}}=0$ <br> so $T_{B R}=24 \sqrt{3}$ <br> At $B$ in direction $B C$ $\begin{aligned} & T_{\mathrm{BC}}-T_{\mathrm{BR}} \cos 30=0 \\ & T_{\mathrm{BC}}=36 . \text { Force in BC: } 36 \mathrm{~N}(\mathrm{~T}) \end{aligned}$ | M1 <br> A1 <br> M1 <br> F1 <br> M1 <br> F1 <br> A1 <br> [7] | Equilibrium at one pin-joint <br> 20.8 Sign consistent with tension on their diagram <br> -15.39 <br> FT their $T_{\text {AB }}$ <br> Allow FT Other methods are possible, but award this M1 only for a complete method that would lead to $T_{\mathrm{BC}}$ <br> cao WWW T/C all correct |
| 4 | (i) |  | $\begin{aligned} & 26 t=3 \times 13 \\ & t=1.5 \text { so } 1.5 \mathrm{~s} \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & {[2]} \end{aligned}$ | Use of $F t=m(v-u)$ or N2L to find $a(=26 / 3)$ and use $v=u+a t$ cao |
| 4 | (ii) |  | PCLM $\begin{aligned} & 10 \times 0+3 \times 13=10 v_{Q}+3 v_{\mathrm{P}} \\ & 39=10 v_{\mathrm{Q}}+3 v_{\mathrm{P}} \end{aligned}$ <br> NEL $\begin{gathered} \frac{v_{\mathrm{Q}}-v_{P}}{0-13}=-e \\ v_{\mathrm{Q}}-v_{P}=13 e \end{gathered}$ $\begin{gathered} v_{\mathrm{Q}}=3(1+e) \\ v_{\mathrm{P}}=3-10 e \end{gathered}$ | M1 <br> A1 <br> M1 <br> A1 <br> M1 <br> B1 <br> E1 <br> [7] | Use of PCLM <br> Any form <br> Use of NEL. Allow sign errors but not inversion <br> Any form <br> Eliminating one of $v_{\mathrm{Q}}$ or $v_{\mathrm{P}}$ OR allow substitution of given result in one equation and check both answers in other equation <br> cao; aef <br> Properly shown |


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| 4 | (iii) | Need $v_{\mathrm{P}}<0$ so $3-10 e<0$ Hence $\frac{3}{10}<e \leq 1$ | M1 <br> A1 <br> [2] | Accept $\leq$ <br> cao (Allow $e \leq 1$ omitted) Correct answer www gets $2 / 2$ |
| 4 | (iv) | When $e>\frac{3}{10}$, its speed is $10 e-3$ We require $(10 e-3)>3(1+e)$ $\text { so } 7 e>6 \text { and so } \frac{6}{7}<e \leq 1$ | M1 <br> M1 <br> A1 <br> A1 <br> [4] | FT their $v_{Q}$ SC1 for $(3-10 e)> \pm 3(1+e)$ <br> FT their $v_{Q}$ <br> cao. Allow $e>\frac{6}{7}$ (0.857) Correct answer www gets $4 / 4$ |
| 4 | (v) | Either $v_{\mathrm{Q}}=4.5 \text { and } v_{\mathrm{P}}=-2$ <br> When they collide the speed of Q is -4.5 and of $P$ is 2 <br> PCLM $10 \times-4.5+3 \times 2=13 V$ <br> so $V=-3$ and velocity is $-3 \mathrm{~m} \mathrm{~s}^{-1}$ | M1 <br> M1 <br> M1 <br> A1 <br> [4] | Substitute $e=0.5$; FT their $v_{Q}$ <br> Change signs of their velocities <br> Use of PCLM Allow sign errors <br> cao; OR $3 \mathrm{~m} \mathrm{~s}^{-1}$ to the right <br> or use argument about final LM is -ve of original LM |
|  |  | Or $10(-3(1+e))+3(10 e-3)=13 V$ $-39=13 V$ <br> so $V=-3$ and velocity is $-3 \mathrm{~m} \mathrm{~s}^{-1}$ | $\begin{aligned} & \text { M1 } \\ & \text { M1 } \\ & \text { M1 } \\ & \text { A1 } \\ & \text { [4] } \\ & \hline \end{aligned}$ | Use of PCLM; Allow sign errors ; FT their $v_{Q}$ <br> Change signs of their velocities <br> Simplify <br> cao; OR $3 \mathrm{~m} \mathrm{~s}^{-1}$ to the right |
| 4 | (vi) | $3(-3-2)=-15 \mathrm{Ns}$ | B1 <br> [1] | FT 3(their $(v)-2)$ Using $10(-3+4.5)=15$ gets B0 until it leads to correct answer |

