Mark Scheme 4732 January 2007

Note: "3 sfs" means an answer which is equal to, or rounds to, the given answer. If such an answer is seen and then later rounded, apply ISW. Penalize over-rounding only once in paper, except qu 8(ii).

| Penalize ove | r-rounding only once in paper, except qu 8(ii). | | | |
|--------------|--|----------|---|--|
| 1i | r-rounding only once in paper, except qu 8(ii). $ \frac{1 - {3 \choose 10} + {1 \choose 5} + {2 \choose 5}}{{1 \choose 10}} $ | M1 A1 | 2 | or $(^3/_{10} + ^1/_5 + ^2/_5) + p = 1$ |
| ii | $\frac{\frac{10}{3}}{\frac{10}{10} + 2 \times \frac{1}{5} + 3 \times \frac{2}{5}}$ $\frac{\frac{19}{10}}{\frac{19}{10}}$ oe | M1 A1 | 2 | ÷4or6⇒ M0A0 |
| Total | | 4 | | |
| 2i | $x = 20; y = 11; x^2 = 96; y^2 = 31; xy$ | | | |
| 21 | =52) $S_{xx} = 16$ or 3.2 | B1 B1 | | |
| | $S_{yy} = 6.8$ or 1.36 | B1 | | |
| | $S_{xy} = 8 \qquad \text{or } 1.6$ | M1 | | $dep -1 \le r \le 1$ |
| | r = 8 or 1.6 | 1,11 | | ft their S's $(S_{xx} \& S_{yy} + ve)$ for M1 only |
| | $\sqrt{(16x6.8)}$ $\sqrt{(3.2x1.36)}$ = 0.767 (3 sfs) | A1 | 5 | it then s is (S _{XX} et syy) + (s) for 1.11 sing |
| ii | Small sample oe | B1f | 1 | |
| Total | | 6 | | |
| 3i | 120 | B1 | 1 | not just 5! |
| iia | $3 \times 4! \text{ or } 72 (\div 5!)$ | M1 | | not just 3. |
| 11a | $\frac{3 \times 4!}{3 \cdot 5}$ oe $(-5!)$ | A1 | 2 | oe, eg ⁷² / ₁₂₀ |
| b | Starts 1 or 21 (both) | M1 | | $12,13,14,15$, (≥ 2 of these incl 21, or allow 1 extra) |
| D | $\frac{1}{5} + \frac{1}{5} \times \frac{1}{4}$ | | | can be implied by wking |
| | | M1 | 3 | or $5x 3!$ or $4! + 3!$ (÷5!) |
| 7D 4 1 | $= \frac{1}{4}$ oe | A1 | 3 | complement: full equiv steps for Ms |
| Total | | 6 | | |
| 4ia | W & Y oe | B1 | 1 | |
| b | | B1 | 1 | |
| | X oe | | | |
| ii | Geo probs always decrease | B1 | 1 | Geo not fixed no. of values |
| | or Geo has no upper limit to x or $x \neq 0$ | | | diags have fixed no of trials not Geo has +ve skew |
| iii | | B1 | | indep |
| | $ \mathbf{w} $ | B1dep |) | allow Bin probs rise then fall |
| | | 2 | | |
| | Bin probs cannot fall then rise | | | |
| To401 | or bimodal | <u></u> | | |
| Total 5: | 140×106 9 | 5 | | |
| 5i | $2685 - \frac{140 \times 106.8}{8}$ or $2685 - \frac{140 \times 106.8}{8}$ | M | | Compatable in any assess famous a famous |
| | $\frac{8}{3500 - \frac{140^2}{8}} = \frac{012083 - \frac{140^2}{8}}{8 \times 17.5 \times 13.35}$ | M1 | | Correct sub in any correct formula for b (incl. $(x - \bar{x})$ etc) |
| | $= {}^{136}/_{175} \text{ or } 0.777 (3 \text{ sfs})$ | A1 | | |
| | $y - \frac{106.8}{8} = 0.777(x - \frac{140}{8})$ | M1 | | or $a = {}^{106.8}/_8 - 0.777 x^{140}/_8$ ft b for M1 |
| | $y=0.78x-0.25$ or better or $y = {}^{136}/{}_{175}x - {}^{1}/{}_{4}$ | A1 | 4 | ≥ 2 sfs sufficient for coeffs |
| ii | $0.78 \times 12 - 0.25$ | M1 | | M1: ft their equn |
| | = 9.1 (2 sfs) | A1f | 2 | A1: dep const term in equn |
| iiia | Reliable | B1 | | Just "reliable" for both: B1 |
| b | Unreliable because extrapolating oe | B1 | 2 | |
| Total | | 8 | | |
| 1 Utal | <u> </u> | 0 | | |

| 6i | $Geo(^2/_3)$ stated | M1 | | or implied by $\binom{1}{3}^n x^2/_3$ |
|----|------------------------------------|------------|---|---------------------------------------|
| | $(^{1}/_{3})^{3} \times ^{2}/_{3}$ | M1 | | |
| | $= \frac{2}{81}$ or 0.0247 (3 sfs) | A 1 | 3 | |

| ii | $(1/3)^3$ | M1 | | or $^{2}/_{3}+^{1}/_{3}x^{2}/_{3}+(^{1}/_{3})^{2}x^{2}/_{3}:M2$ |
|------------|---|----------------------|---|---|
| | $(1 - (1/3)^3)^3$ | M1 | | one term omitted or extra or wrong: M1 |
| | 2 (73) | 1,11 | | $1 - {\binom{1}{3}}^4$ or $1 - {\binom{2}{3}}^{+1}/{3}x^2/{3} + {\binom{1}{3}}^2x^2/{3}$):M1 |
| | ²⁶ / ₂₇ or 0.963 (3 sfs) | A1 | 3 | - (+3) (+3++3+3+(+3)+3) |
| iii | 1 / 2/3 | M1 | | |
| | = 3/2 oe | A1 | 2 | |
| Total | | 8 | | |
| 7i | $^{2}/_{9}$ or $^{7}/_{9}$ oe seen | B1 | | |
| | $\frac{3}{9}$ or $\frac{6}{9}$ oe seen | B1 | | |
| | $^{1}/_{8}$ or $^{7}/_{8}$ oe seen | B1 | | |
| | Correct structure | B1 | | ie 8 correct branches only, |
| | A 11 | D.1 | _ | ignore probs & values |
| | All correct | B1 | 5 | including probs and values, |
| | 3, 7, 7, 3, 7, 6, | 7.70 | | but headings not req'd |
| ii | $\sqrt{3/_{10} x^{7/_9} + 7/_{10} x^{3/_9} + 7/_{10} x^{6/_9}}$ | M2 | | or $^{3}/_{10}x^{7}/_{9} + ^{7}/_{10}$ or $1 - ^{3}/_{10}x^{2}/_{9}$ |
| | 14/ 00 0 0 22 00 | A 1 | 3 | M1: one correct prod or any prod $+ \frac{1}{10}$ |
| iii | $\frac{14}{15}$ or 0.933 oe $\frac{3}{10}$ x $\frac{2}{9}$ x $\frac{7}{8}$ + $\frac{7}{10}$ x $\frac{6}{9}$ | A1 M2 | 3 | $\int \int $ |
| 111 | / ₁₀ X / ₉ X / ₈ + / ₁₀ X / ₉ | IVIZ | | M1: one correct prod |
| | $^{21}/_{40}$ or 0.525 oe | A1 | 3 | cao |
| | No ft from diag except: with replacement: | | | re: B1 (ii) $^{91}/_{100}$: B2 (iii) 0.553: B2 |
| Total | 100 it from diag except. With replacement. | 11 | | (II) / ₁₀₀ . B 2 (III) 0.333. B 2 |
| 8i | Med = 2 | B1 | - | cao |
| 01 | LQ = 1 or $UQ = 4$ | M1 | | or if treat as cont data: |
| | | | | read cf curve or interp at 25 & 75 |
| | IQR = 3 | A1 | 3 | cao |
| ii | Assume last value = 7 (or eg 7.5 or 8 or 8.5) | B1 | | stated, & not contradicted in wking |
| | | | | eg 7-9 or 7,8, 9 Not just in wking |
| | xf attempted ≥ 5 terms | M1 | | allow "midpts" in xf or x^2f |
| | | | | |
| | 2.6 or 3 sf ans that rounds to 2.6 | A1 | | |
| | $x^2 f$ or $(x-m)^2 f \ge 5$ terms | M1 | | |
| | $\sqrt{(x^2f/100-m^2)}$ or | | | |
| | $\sqrt{(x-m)^2f}/100$ fully correct but ft m | M1 | | 1 M2 |
| | 1.6 or 1.7 or 3 sf ans that rounds to 1.6 or 1.7 | A1 | | dep M3 |
| | | | 6 | penalize > 3 sfs only once |
| iii | Median less affected by extremes or | B1 | 1 | or median is an integer or mean not int. |
| | outliers etc (NOT anomalies) | | | or not affected by open-ended interval |
| | Small change in var'n leads to lge change in IQR | | | general comment acceptable |
| iv | UQ for W only just 4, hence IQR exaggerated | | | for Old Moat LQ only just 1 & UQ only just 3 |
| | orig data shows variations are similar | B1 | 1 | |
| v | | | | |
| • | | | 2 | |
| Total | | (| | |
| v Total | orig data shows variations are similar OM % (or y) decr (as x incr) oe Old Moat | B1 B1 B1 13 | 2 | oe specific comment essential ranks reversed in OM or not rev in W NIS |

| 9i | $^{11}\text{C}_5 \times (^{1}/_{4})^{6} \times (^{3}/_{4})^{5}$ | M1 | | or $462 \times (^{1}/_{4})^{6} \times (^{3}/_{4})^{5}$ | |
|----------------|---|------------|---|--|--|
| 1 | 0.0268 (3 sfs) | A1 | 2 | | |
| ii | $q^{11} = 0.05$ or $(1-p)^{11} = 0.05$ | M1 | | (any letter except p) ¹¹ = 0.05 oe | |
| | $\sqrt[11]{0.05}$ | M1 | | oe or inv $\log(\frac{\log 0.05}{11})$ | |
| | q = 0.762 or 0.7616 | A1 | | 11 | |
| | p = 0.238 (3 sfs) | A1f | 4 | ft dep M2 | |
| iii | $11 \times p \times (1-p) = 1.76$ oe | M1 | | not $11pq = 1.76$ | |
| | $11p - 11p^2 = 1.76$ or $p - p^2 = 0.16$ | A 1 | | any correct equn after mult out | |
| | $11p^2 - 11p + 1.76 = 0$ or $p^2 - p + 0.16 = 0$ | A1 | | or equiv with $= 0$ | |
| | $(25p^2 - 25p + 4 = 0)$ | | | | |
| | (5p-1)(5p-4) = 0 | | | or correct fact'n or subst'n for their quad | |
| | or $p = 11 - \sqrt{(11^2 - 4x11x1.76)}$ | M1 | | equ'n eg $p = \frac{1 \pm \sqrt{(1-4x0.16)}}{}$ | |
| | 2 x 11 | | | 2 | |
| | p = 0.2 or 0.8 | A1 | 5 | | |
| Total | | 11 | | | |
| | | | | | |
| Total 72 marks | | | | | |