Ques	on Scheme	Marks	AOs
1	Use Impulse-momentum principle	M1	2.1
	$2\mathbf{i} - \mathbf{j} = 0.5\mathbf{v} - 0.5(4\mathbf{i} + \mathbf{j})$	A1	1.1b
	$\frac{1}{2}\mathbf{v} = 4\mathbf{i}  \frac{1}{2}\mathbf{j} = \mathbf{j},  \mathbf{v}  8\mathbf{i}  \mathbf{j}  (\mathbf{m} \ \mathbf{s}^{-1})$	A1	1.1b
	Use of KE = $\frac{1}{2}m \mathbf{v} ^2 - \frac{1}{2}m \mathbf{u} ^2$	M1	2.1
	$=\frac{1}{2} \times 0.5 \times \left\{ (64+1) - (16+1) \right\}$	A1	1.1b
	$=\frac{1}{4} \times 48 = 12$ (J) *	A1*	1.1b
		(6)	
		(6 1	marks)
Note			
M1:	Difference of terms & dimensionally correct		
A1:	Correct unsimplified equation		
A1:	200		
M1:	Must be a difference of two terms		
	Must be dimensionally correct		

## Paper 3C/4C: Further Mechanics 1 Mark Scheme

A1: Correct unsimplified equation

A1\*: Complete justification of given answer

Question	Scheme	Marks	AOs
2(a)	$R = 5g\cos\alpha \left(=5g \times \frac{4\sqrt{3}}{7} = 48.497\right)$	M1	3.4
	Force due to friction = $\mu \times 5g \cos \alpha$	M1	3.4
	Work-Energy equation	M1	3.4
	$\frac{1}{2} \times 5 \times 64 = 5 \times 9.8 \times 14 \sin \alpha + 14 \mu R$	A1	1.1b
	$\mu = 0.0913 \text{ or } 0.091$	A1	1.1b
		(5)	
(b)	Appropriate refinement	B1	3.5c
		(1)	
		(6 n	narks)

## Notes:

(a)

- M1: Condone sin/cos confusion
- M1: Use of  $\mu \times$  their R
- M1: Must be using work-energy. Requires all terms Condone sin/cos confusion, sign errors and their *R*
- **A1:** Correct in  $\theta$  and  $\mu R$
- A1: Accept 0.0913 or 0.091

(b)

- **B1:** e.g.
  - do not model the parcel as a particle and therefore take air resistance into account - take into account the dimensions/uniformity of the parcel

Questio	n Scheme	Marks	AOs		
3(a)	Use NEL to find the speed of particle after the first impact = $eu = \frac{3}{4}u\frac{\pi}{2}$	B1	3.4		
	Impulse = $\lambda mu = mv - mu = \pm \left[\frac{3}{4}mu - (-mu)\right]$	M1	3.1b		
	$\lambda = \frac{7}{4}$	A1	1.1b		
		(3)			
(b)	Use NEL to find the speed of the particle after the second impact = $\frac{3}{4} \times \frac{3}{4}u = \frac{9}{16}u$	B1	3.4		
	Use of $s = vt$ to find total time	M1	3.1b		
	$7 = \frac{2}{u} + \frac{4}{\frac{3}{4}u} + \frac{2}{\frac{9}{16}u} \left( = \frac{2}{u} + \frac{16}{3u} + \frac{32}{9u} \right)$	A1	1.1b		
	Solve for <i>u</i> : $63u = 18 + 48 + 32$	M1	1.1b		
	$u = \frac{98}{63} = \frac{14}{9} (= 1.5)$	A1	1.1b		
		(5)			
			narks)		
Notes:					
M1: M A1: ca	sing Newton's experimental law as a model to find the speed after the fi ust be a difference of two terms, taking account of the change in direction		on		
M1: No A1: Ut	Using NEL as a model to find the speed after the second impact Needs to be used for at least one stage of the journey Ur equivalent Solve their linear equation for <i>u</i>				
	1		Accept 1.56 or better		

Question	Scheme	Marks	AOs
4(a)	Complete strategy to find the kinetic energy after the second impact	M1	3.1b
	Parallel to AB after collision: $u\cos 60^{\circ}$	M1	3.1b
	Perpendicular to <i>AB</i> after collision: $\frac{1}{\sqrt{3}}u\sin 60^\circ$	M1	3.4
	Components of velocity after first impact: $\frac{u}{2}$ , $\frac{u}{2}$	A1	1.1b
	Parallel to <i>BC</i> after collision: $\frac{u}{2} \left( u \times \frac{1}{\sqrt{3}} \sin 60^{\circ} \right)$	M1	3.1b
	Perpendicular to <i>BC</i> after collision: $\sqrt{\frac{2}{5}} \times \frac{u}{2} \left( = \frac{1}{\sqrt{10}} u \right)$ $\left( \sqrt{\frac{2}{5}} \times u \cos 60^{\circ} \right)$	M1	3.4
	Components of velocity after second impact: $\frac{u}{2}$ , $\frac{u}{\sqrt{10}}$	A1	1.1b
	Final KE = $\frac{1}{2}m\left(\frac{u^2}{4} + \frac{u^2}{10}\right) \left(=\frac{mu^2}{2} \times \frac{7}{20}\right)$		
	Fraction of initial KE = $\frac{\frac{mu^2}{2} \times \frac{7}{20}}{\frac{mu^2}{2}} = \frac{7}{20} = 35\%$ *	A1*	2.2a
		(8)	
(b)	The answer is too large - rough surface means resistance so final speed will be lower	B1	3.5a
		(1)	
		(9 ו	marks)
Notes:			
M1:UseA1:BotM1:UseM1:UseA1:BotM1:Cor	Use of CLM parallel to the wall. Condone sin/cos confusion Use NEL as a model to find the speed perpendicular to the wall. Condone sin/cos confusion Both components correct with trig substituted (seen or implied) Use of CLM parallel to the wall. Condone sin/cos confusion Use NEL as a model to find the speed perpendicular to the wall. Condone sin/cos confusion Both components correct with trig substituted (seen or implied) Correct expression for total KE using their components after 2nd collision Obtain <b>given answer</b> with sufficient working to justify it		
(b) B1: Clea	ar explanation of how the modelling assumption has affected the outcome		

Ques	tion	Scheme	Marks	AOs
5(a	ı)	Use of $P = Fv$ : $F = \frac{12000}{20}$	B1	3.3
		Equation of motion: $F - (200 + 2v) = 600a$	M1	3.4
		600 - 240 = 600a	A1ft	1.1b
		$360 = 600a, a = 0.6 \text{ (m s}^{-2}\text{)}$	Al	1.1b
			(4)	
<b>(b</b> )	)	Equation of motion:	M1	3.3
		12000 (200 2 ) (200 1 0 (20 0 0 5	A1	1.1b
		$\frac{12000}{w} - (200 + 2w) - 600g\sin\theta = -600 \times 0.05$	A1	1.1b
		3 term quadratic and solve: $2w^2 + 590w - 12000 = 0$	M1	1.1b
		$w = \frac{-590 + \sqrt{590^2 + 96000}}{4}  19.1 (\text{m s}^{-1})$	A1	1.1b
			(5)	
			(9)	marks)
Notes	5:			
(a) B1: M1: A1ft: A1:	Use Mus	or equivalent the model to form the equation of motion t include all terms .Condone sign errors ect for their F		
(b) M1: A1:	All t All c	the model to form the equation of motion erms needed. Condone sign errors and sin/cos confusion correct A1A1		
M1:	One error A1A0 Dependent on the preceding M1. Use the equation of motion to form a 3-term quadratic in $w$ only			
A1:	Acce	ept 19. Do not accept more than 3 s.f.		

Question	Scheme	Marks	AOs
6(a)	3j vi A(2m) 3i+3j B(3m) -5i+2j		
	Overall strategy to find $\mathbf{V}_A$	M1	3.1a
	Velocity of A perpendicular to loc after collision = $3j$ (m s <sup>-1</sup> )	B1	3.4
	CLM parallel to loc	M1	3.1a
	$2m \times 3 - 3m \times 5 = 3mw - 2mv$ (-9 = 3w-2v)	A1	1.1b
	Correct use of impact law	M1	3.1a
	$v + w = \frac{1}{4}(3+5) (=2)$	A1	1.1b
	Solve for $w$ 3w-2v = -9 2v+2w = 4		
	$\mathbf{v}_B = -\mathbf{i} + 2\mathbf{j} \ (\mathrm{m \ s}^{-1}),$	Alft	1.1b
( <b>•</b> )		(7)	
(b)	$\cos\theta = \frac{(-5\mathbf{i}+2\mathbf{j})\cdot(-\mathbf{i}+2\mathbf{j})}{\sqrt{29}\sqrt{5}}$	M1	3.1a
	$\theta = 41.63^{\circ} = 42^{\circ}$ (nearest degree)	A1	1.1b
	Alternative method: $\tan^{-1} 2 - \tan^{-1} \frac{2}{5} = 41.63^{\circ} = 42^{\circ}$		
	(nearest degree)		
		(2)	
Notes:		(9)	marks)
(a)         M1:       Corr         B1:       Use         M1:       Use         A1:       Corr         M1:       Mus         A1:       Corr         A1:       Corr         A1:       Corr         A1:       Corr         A1:       Corr	rect overall strategy to form sufficient equations and solve for $\mathbf{v}_A$ the model to find the component of $\mathbf{v}_A$ perpendicular to the line of CLM to form equation in $v$ and $w$ . Need all 4 terms, dimensionally rect unsimplified st be used the right way round rect unsimplified orrect. Follow their 2j		
(b) M1: Con A1: cao	nplete method for finding the required angle. Follow their $v_B$		

Question	Scheme	Marks	AOs
7(a)	In equilibrium $\Rightarrow$ no resultant vertical force	M1	2.1
	$\frac{3mgx}{a} = mg$	A1	1.1b
	$x = \frac{a}{3}$ , $d = \frac{4}{3}a$ *	A1*	2.2a
		(3)	
(b)	Equation of motion:	M1	3.1a
	$\frac{3mga}{a} - mg = m\ddot{x}$	A1	1.1b
	$\ddot{x} = 2g$	Al	1.1b
		(3)	
(c)	Max speed at equilibrium position	B1	3.1a
	Work energy & use of EPE = $\frac{\lambda x^2}{2a}$	M1	3.1a
	$\frac{3mga^2}{2a} = \frac{3mg\left(\frac{a}{3}\right)^2}{2a} + \frac{1}{2}mv^2 + mg\frac{2a}{3}$	A1 A1	1.1b 1.1b
	$\frac{1}{2}v^{2} = ga\left(\frac{3}{2} - \frac{1}{6} - \frac{2}{3}\right) = \frac{2}{3}ga, \qquad v = \sqrt{\frac{4ga}{3}}$	A1	1.1b
		(5)	
(d)	At max ht. $KE = 0$ . $EPE$ lost = GPE gained	M1	3.1a
	$\frac{3mga^2}{2a} = mgh$	A1	1.1b
	$OB = \frac{a}{2}$	A1	1.1b
		(3)	
	1	(14 r	narks)

Ques	tion 7 notes:
(a)	
M1:	Use $T = \frac{\lambda x}{a}$ to form equation for equilibrium
A1:	Correct unsimplified equation
A1*:	Requires sufficient working to justify given answer
	plus a 'statement' that the required result has been achieved
(b)	
M1:	Use $T = \frac{\lambda x}{a}$ to form equation of motion
	Need all 3 terms. Condone sign errors
A1:	Correct unsimplified equation
A1:	cao
(c)	
B1:	Seen or implied
M1:	Form work-energy equation. All 4 terms needed
	Condone sign errors
A1:	Correct unsimplified equation A1A1
	One error in the equation A1A0
A1:	сао
(d)	
M1:	Form energy equation
A1:	Correct unsimplified equation
A1:	cao

Question	Scheme	Marks	AOs
8(a)	$\xrightarrow{2u}$ $\overleftarrow{u}$		
	$ \begin{pmatrix} P \\ 2m \end{pmatrix} \qquad \qquad$		
	$\langle w \rangle$		
	Complete overall strategy to find v	M1	3.1a
	Use of CLM	M1	3.1a
	$2m \times 2u - 5m \times u = 5m \times v - 2m \times w , (-u = 5v - 2w)$	A1	1.1b
	Use of Impact law:	M1	3.1a
	v + w = e(2u + u)	A1	1.1b
	Solve for v: $ \begin{array}{rcl} -u &= 5v - 2w \\ 6eu &= 2v + 2w \end{array} $		
	$7v = u(6e-1)  \left(v = \frac{u}{7}(6e-1)\right)$	A1	1.1b
	Direction of $Q$ reversed: $v > 0$	M1	3.4
	$\Rightarrow 1 \ge e > \frac{1}{6}$	A1	1.1b
		(8)	
(b)	$e = \frac{1}{3} \implies v = \frac{u}{7},  w = \frac{6u}{7}$	B1	2.1
	Equation for KE lost	M1	2.1
	$\frac{1}{2} \times 2m \left( 4u^2 - \frac{36u^2}{49} \right) + \frac{1}{2} \times 5m \left( u^2 - \frac{u^2}{49} \right)$	A1	1.1b
	2  (m  49)  2  (m  49)	A1	1.1b
	$\frac{1}{2}mu^2\left(8-\frac{72}{49}+5-\frac{5}{49}\right) = \frac{40mu^2}{7}  *$	A1*	2.2a
		(5)	
(c)	Increase $e \Rightarrow$ more elastic $\Rightarrow$ less energy lost	B1	2.2a
		(1)	
		(14	marks)

Ques	tion 8 notes:
(a)	
M1:	Complete strategy to form sufficient equations in v and w and solve for v
M1:	Use CLM to form equation in v and w
	Needs all 4 terms & dimensionally correct
A1:	Correct unsimplified equation
M1:	Use NEL as a model to form a second equation in v and w. Must be used the right way round
A1:	Correct unsimplified equation
A1:	for v or 7v correct
M1:	Use the model to form a correct inequality for their v
A1:	Both limits required
(b)	
B1:	Or equivalent statements
M1:	Terms of correct structure combined correctly
A1:	Fully correct unsimplified A1A1
	One error on unsimplified expression A1A0
A1*:	cso. plus a 'statement' that the required result has been achieved
(c)	
B1:	"less energy lost" or equivalent