

4722 Core Mathematics 2

1	(i) $2(1 - \cos^2 x) = 5\cos x - 1$ $2\cos^2 x + 5\cos x - 3 = 0$ A.G.	M1 A1	Use $\sin^2 x = 1 - \cos^2 x$ 2 Show given equation correctly

	(ii) $(2\cos x - 1)(\cos x + 3) = 0$ $\cos x = \frac{1}{2}$ $x = 60^\circ$ $x = 300^\circ$	M1 M1 A1 A1√	Recognise equation as quadratic in $\cos x$ and attempt recognisable method to solve Attempt to find x from root(s) of quadratic Obtain 60° or $\frac{\pi}{3}$ or 1.05 rad 4 Obtain 300° only (or $360^\circ -$ their x) and no extra in range SR answer only is B1 B1
6			

2	(i) $\int (6x - 4)dx = 3x^2 - 4x + c$ $y = 3x^2 - 4x + c \Rightarrow 5 = 12 - 8 + c$ $\Rightarrow c = 1$ Hence $y = 3x^2 - 4x + 1$	M1* A1 M1dep* A1	Attempt integration (inc. in power for at least one term) Obtain $3x^2 - 4x$ (or unsimplified equiv), with or without $+ c$ Use (2, 5) to find c 4 Obtain $y = 3x^2 - 4x + 1$

	(ii) $3p^2 - 4p + 1 = 5$ $3p^2 - 4p - 4 = 0$ $(p - 2)(3p + 2) = 0$ $p = -\frac{2}{3}$	M1* M1dep* A1	Equate their y (from integration attempt) to 5 Attempt to solve three term quadratic 3 Obtain $p = -\frac{2}{3}$ (allow any variable) from correct working; condone $p = 2$ still present, but A0 if extra incorrect solution
7			

3	(i) $(2 - x)^7 = 128 - 448x + 672x^2 - 560x^3$	M1 A1 A1 A1	Attempt (at least) two relevant terms – product of binomial coeff, 2 and x (or expansion attempt that considers all 7 brackets) Obtain $128 - 448x$ Obtain $672x^2$ 4 Obtain $-560x^3$

	(ii) $-560 \times (\frac{1}{4})^3 = -\frac{35}{4}$	M1 A1	Attempt to use coeff of x^3 from (i), with clear intention to cube $\frac{1}{4}$ 2 Obtain $-\frac{35}{4}$ (w^6), (allow $\frac{35}{4}$ from $+560x^3$ in (i))
6			

4	(i)	$\int_3^5 \log_{10}(2+x) dx \approx \frac{1}{2} \times \frac{1}{2} \times (\log 5 + 2 \log 5.5 +$	M1	Attempt y-coords for at least 4 of the correct 5 x-coords only
		$2 \log 6 + 2 \log 6.5 + \log 7)$	M1	Use correct trapezium rule, any h , to find area between $x = 3$ and $x = 5$
		≈ 1.55	M1	Correct h (soi) for their y-values
			A1	Obtain 1.55

	(ii)	$\int_3^5 \log_{10}(2+x)^{\frac{1}{2}} dx = \frac{1}{2} \int_3^5 \log_{10}(2+x) dx$	B1√	Divide by 2, or equiv, at any stage to obtain 0.78 or 0.77,
		$\approx \frac{1}{2} \times 1.55$		following their answer to (i)
		≈ 0.78	B1	Explicitly use $\log \sqrt{a} = \frac{1}{2} \log a$ on a single term
6				
5		$\int_1^3 \{(11-9x^{-2}) - (x^2+1)\} dx = [9x^{-1} - \frac{1}{3}x^3 + 10x]_1^3$	M1	Attempt subtraction (correct order) at any point
		$= (3-9+30) - (9-\frac{1}{3}+10)$	M1	Attempt integration – inc. in power for at least one term
		$= 24 - 18\frac{2}{3}$	A1	Obtain $\pm (-\frac{1}{3}x^3 + 10x)$ or $11x$ and $\frac{1}{3}x^3 + x$
		$= 5\frac{1}{3}$	M1	Obtain remaining term of form kx^{-1}
		OR	A1	Obtain $\pm 9x^{-1}$ or any unsimplified equiv
		$[11x+9x^{-1}]_1^3 - [\frac{1}{3}x^3+x]_1^3$	M1	Use limits $x = 1, 3$ – correct order & subtraction
		$= [(33+3) - (11+9)] - [(9+3) - (\frac{1}{3}+1)]$	A1	Obtain $5\frac{1}{3}$, or exact equiv
		$= 16 - 10\frac{2}{3}$		
		$= 5\frac{1}{3}$		
7				
6	(i)	$f(-3) = 0 \Rightarrow -54 + 9a - 3b + 15 = 0$	M1	Attempt $f(-3)$ and equate to 0, or equiv method
		$3a - b = 13$	A1	Obtain $3a - b = 13$, or unsimplified equiv
		$f(2) = 35 \Rightarrow 16 + 4a + 2b + 15 = 35$	M1	Attempt $f(2)$ and equate to 35, or equiv method
		$2a + b = 2$	A1	Obtain $2a + b = 2$, or unsimplified equiv
		Hence $a = 3, b = -4$	M1	Attempt to solve simultaneous eqns
			A1	Obtain $a = 3, b = -4$

(ii)	f(x) = (x+3)(2x ² - 3x + 5)		M1	Attempt complete division by (x+3), or equiv
			A1	Obtain $2x^2 - 3x + c$ or $2x^2 + bx + 5$, from correct $f(x)$
		ie quotient is $(2x^2 - 3x + 5)$	A1	Obtain $2x^2 - 3x + 5$ (state or imply as quotient)
9				

7	(i) $13^2 = 10^2 + 14^2 - 2 \times 10 \times 14 \times \cos \theta$ $\cos \theta = 0.4536$ $\theta = 1.10$ A.G.	M1 A1	2	Attempt to use correct cosine rule in ΔABC Obtain 1.10 radians (allow 1.1 radians) SR B1 only for verification of 1.10, unless complete method

	(ii) arc $EF = 4 \times 1.10 = 4.4$ perimeter = $4.4 + 10 + 13 + 6$ $= 33.4$ cm	B1 M1 A1	3	State or imply $EF = 4.4$ cm (allow 4×1.10) Attempt perimeter of region - sum of arc and three sides with attempt to subtract 4 from at least one relevant side Obtain 33.4 cm

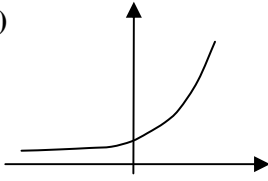
	(iii) area $AEF = \frac{1}{2} \times 4^2 \times 1.1$ $= 8.8$ area $ABC = \frac{1}{2} \times 10 \times 14 \times \sin 1.1$ $= 62.4$ hence total area = 53.6 cm^2	M1 A1 M1 A1 A1	5	Attempt use of $(\frac{1}{2})r^2\theta$, with $r = 4$ and $\theta = 1.10$ Obtain 8.8 Attempt use of $(\frac{1}{2})absin\theta$, sides consistent with angle used Obtain 62.4 or better (allow 62.38 or 62.39) Obtain total area as 53.6 cm^2
				10
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8	(i) $u_5 = 8 + 4 \times 3$ $= 20$ A.G.	M1 A1	2	Attempt $a + (n - 1)d$ or equiv inc list of terms Obtain 20

	(ii) $u_n = 3n + 5$ ie $p = 3, q = 5$	B1 B1	2	Obtain correct expression, poss unsimplified, eg $8 + 3(n - 1)$ Obtain correct $3n + 5$, or $p = 3, q = 5$ stated

	(iii) arithmetic progression	B1	1	Any mention of arithmetic

	(iv) $\frac{2N}{2}(16 + (2N - 1)3) - \frac{N}{2}(16 + (N - 1)3) = 1256$ $26N + 12N^2 - 13N - 3N^2 = 2512$ $9N^2 + 13N - 2512 = 0$ $(9N + 157)(N - 16) = 0$ $N = 16$	M1 M1 M1* M1dep* A1	5	Attempt S_N , using any correct formula (inc $\sum (3n + 5)$) Attempt S_{2N} , using any correct formula, with $2N$ consistent (inc $\sum (3n + 5)$) Attempt subtraction (correct order) and equate to 1256 Attempt to solve quadratic in N Obtain $N = 16$ only, from correct working
				OR: alternative method is to use $^n/2 (a + l) = 1256$ M1 Attempt given difference as single summation with N terms M1 Attempt $a = u_{N+1}$ M1 Attempt $l = u_{2N}$ M1 Equate to 1256 and attempt to solve quadratic A1 Obtain $N = 16$ only, from correct working
				10

9 (i)



M1 Reasonable graph in both quadrants
 A1 Correct graph in both quadrants

B1 3 State or imply (0, 6)

(ii) $9^x = 150$

$$x \log 9 = \log 150$$

$$x = 2.28$$

M1 Introduce logarithms throughout, or equiv with \log_9

M1 Use $\log a^b = b \log a$ and attempt correct method to find x

A1 3 Obtain $x = 2.28$

(iii) $6 \times 5^x = 9^x$

$$\log_3 (6 \times 5^x) = \log_3 9^x$$

$$\log_3 6 + x \log_3 5 = x \log_3 9$$

$$x(2 - \log_3 5) = 1 + \log_3 2$$

$$x = \frac{1 + \log_3 2}{2 - \log_3 5} \quad \mathbf{A.G.}$$

M1 Form eqn in x and take logs throughout (any base)

M1 Use $\log a^b = b \log a$ correctly on $\log 5^x$ or $\log 9^x$ or legitimate combination of these two

M1 Use $\log ab = \log a + \log b$ correctly on $\log (6 \times 5^x)$ or $\log 6$

M1 Use $\log_3 9 = 2$ or equiv (need base 3 throughout that line)

A1 5 Obtain $x = \frac{1 + \log_3 2}{2 - \log_3 5}$ convincingly (inc base 3 throughout)

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