

Mark Scheme (Results)

June 2011

IGCSE Mathematics (4MAO) Paper 3H

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Question	Working	Answer	Mark		Notes	
Number 1. (a)	24.4					
1. (a)	$\frac{24.1}{0.6}$ - 38.44 = 40.166 38.44		2	M1	for 0.6 or $\frac{3}{5}$	
					or 40.166 (4 figures c truncated)	orrect rounded or
					or $40\frac{1}{6}$ or 38.44 or 38	<u>11</u> 25
		1.726666667		A1	Accept if first 4 figures truncated)	correct (rounded or
					Also accept 1.72 $\frac{25}{150}$	
(b)		1.73	1	B1	ft from (a) if answer to more than 3 sf	(a) is a decimal with
						Total 3 marks
Question	Working	Answer	Mark		Notes	
Number						(alternative method)
2 .	(5 – 2) × 180 or 3 × 180		4	M1		360-(83+66+53+96)
	or $(2 \times 5 - 4) \times 90$ or 6×90					Condone 1
	or 360 + 180					incorrect ext angle
	540			A1	540 seen scores M1A1	62
	"540" - (97 + 114 + 127 + 84)			M1	dep on first M1	180 - "62"
		118		A1	cao	•
						Total 4 marks

IGCSE Mathematics (4MA0) Paper 3H Summer 2011

Question Number	Working	Answer	Mark		Notes
3. (a)		w(w - 9)	2	B2	Award B2 also for $(w \pm 0)(w - 9)$ B1 for factors which, when expanded & simplified, give two terms, one of which is correct except B0 for $(w + 3)(w - 3)$ SC B1 for $w(w - 9w)$
(b)	3x = -6 or $3x = 1 - 7$ or $5x - 2x = -6$ oe		3	M2	for correct rearrangement with x terms on one side and numbers on the other AND correct collection of terms on at least one side M1 for $5x - 2x = 1 - 7$ oe ie correct rearrangement with x terms on one side and numbers on the other
		-2		A1	cao dep on M2
(c)	y ² + 3y - 7y - 21		2	M1	for 3 correct terms out of 4 or for 4 correct terms ignoring signs or for $y^2 - 4y + n$ for any nonzero value of n
		$y^2 - 4y - 21$		A1	cao
			·		Total 7 marks

Question Number	Working	Answer	Mark	Notes
4. (a)	1 - (0.6 + 0.3)		2	M1
		0.1		A1 Also accept $\frac{1}{10}$ or 10%
(b)	30 × 0.6		2	M1
		18		A1 cao Do not accept $\frac{18}{30}$
				Total 4 marks

	T				
Question	Working	Answer	Mark		Notes
Number	_				
5.	$\frac{10}{12} \text{ and } \frac{9}{12}$ $\text{eg } \frac{10-9}{12}, \ \frac{10}{12} - \frac{9}{12}$		2	B2	B1 for $\frac{10}{12}$ or $\frac{9}{12}$ Also accept $\frac{5\times2}{6\times2}$ or $\frac{3\times3}{4\times3}$ Alternative method B1 for both fractions correctly expressed as equivalent fractions with denominators that are common multiples of 6 and 4 eg $\frac{20}{24}$ and $\frac{18}{24}$ or $\frac{5\times4}{6\times4}$ and $\frac{3\times6}{4\times6}$ B1 (dep on first B1) for evaluation as a correct fraction which is equivalent to $\frac{1}{12}$ eg $\frac{2}{24}$ SC B1 for multiplying both sides by 12 ie 10 - 9 = 1
1	1	1			Total 2 marks

Question Number	Working	Answer	Mark		Not€	es
6. (a)		Rotation	3	B1	Accept 'rotate', 'rotated' etc	These marks are independent but
		90° clockwise		B1	Also accept quarter turn clockwise, -90° or 270°	award no marks if the answer is not a single transformation
		(0, 0)		B1	Also accept origin, O	
(b)	vertices (4,4), (4,2), (5,2)	R correct	2	B2	Condone omiss B1 for 2 correc	
						Total 5 marks

Question Number	Working	Answer	Mark	Notes
7.	3+5+7 or 15		3	M1 15 may be denominator of fraction or coefficient in an equation such as 15x = 90
	90 ÷ (3+5+7) or 90 ÷ "15" or 6 or $\frac{7}{15}$ oe			M1 dep
		42		A1 Also award for 18:30:42
				Total 3 marks

Question Number	Working	Answer	Mark		Note	es
8. (i)		3, 5, 7, 11	2	B1	cao	
(ii)		2, 3, 5, 7, 9, 11		B1	cao (B0 if 3 or 5 or 7 or 11 repeated)	Brackets not necessary
						Total 2 marks

Question Number	Working		Answer	Mark		Notes	
9.	eg $\frac{5}{100} \times 8000 = 400$ $\frac{5}{100} \times (8000 + "400")$ = 420 $\frac{5}{100} \times (8000 + "400" + "420")$ = 441 8000 + "400" + "420" + "441"	OR 8000 × 1.05 ³		3		M1 for eg $\frac{5}{100} \times 8000 \text{ or } 400$ M1 for completing method	OR M2 for 8000×1.05 ³ (M1 for 8000×1.05 or 8400 or 8000×1.05 ² or 8000×1.05 ⁴)
						Accept (1 + 0.05) a to 1.05 throughout	•
						SC If no other mark award M1 for 8000> or 9200	
			9261		A1	Cao	
							Total 3 marks

Question Number	Working	Answer	Mark	Notes
10.		$C = \frac{3d+7}{2}$ oe	3	B3 B2 for $\frac{3d+7}{2}$ oe B2 for $C = 3d+7 \div 2$ oe B1 for $3d+7 \div 2$ B1 for $C = 1$ linear expression in d
				Total 3 marks

Question Number	Working	Answer	Mark		Notes
11. (a)	1 × 8 + 3 × 14 + 5 × 26 + 7 × 17 + 9 × 10 + 1 or 8 + 42 + 130 + 119 + 90 + 55	1 × 5	3	M1	for finding at least four products $f \times x$ consistently within intervals (inc end points) and summing them
				M1	(dep) for use of halfway values
		444		A1	Cao
(b)		8 22 48 65 75 80	1	B1	Cao
(c)		Points correct	2	B1	$\pm \frac{1}{2}$ sq ft from sensible table
		Curve or line segments		B1	ft from points if 4 or 5 correct or if points are plotted consistently within each interval at the correct heights Accept curve which is not joined to the origin
(d)	5.2 indicated on cf graph		2	M1	for 5.2 indicated on cf graph
		approx 36-40 from correct graph		A1	If M1 scored, ft from cf graph If M1 not scored, ft only from correct curve & if answer is correct ($\pm \frac{1}{2}$ sq tolerance), award M1 A1
					Total 8 marks

Question Number	Working	Answer	Mark		Notes
12. (a)	$\frac{BC}{5.2} = \frac{9}{6} \text{ oe}$		2	M1	for correct, relevant proportionality statement with 3 values substituted
		7.8		A1	cao
(b)	$\frac{CE}{7.2} = \frac{6}{9}$ oe or $\frac{CE}{6} = \frac{7.2}{9}$ oe or $\frac{CE}{7.2} = \frac{5.2}{"7.8"}$ oe or $\frac{CE}{5.2} = \frac{7.2}{"7.8"}$ oe		2	M1	for correct, relevant proportionality statement with 3 values substituted
		4.8		A1	cao
					Total 4 marks

Question Number	Working	Answer	Mark		Notes
13.	$\frac{20(2x-1)}{4} + \frac{20(x-1)}{5} = 2 \times 20$ or $5(2x-1) + 4(x-1) = 40$ or $\frac{5(2x-1) + 4(x-1)}{20} = 2$ or $\frac{5(2x-1)}{20} + \frac{4(x-1)}{20} = 2$ $10x - 5 + 4x - 4 = 40$ or $\frac{10x - 5 + 4x - 4}{20} = 2$ or $\frac{10x - 5}{20} + \frac{4x - 4}{20} = 2$		4	M1	for clear intention to multiply both sides by 20 or a multiple of 20 or to express LHS as a single fraction with a denominator of 20 or a multiple of 20 or to express LHS as the sum of two fractions with denominators of 20 or a multiple of 20 May be implied by first B1 expanding brackets (dep on M1)
	14x = 49 or 14x - 9 = 40			B1	dep on both preceding marks
	or $10x + 4x - 9 = 40$ or $14x - 49 = 0$				ie for a correct rearrangement of a correct equation
		3.5		A1	dep on all preceding marks
					Total 4 marks

Question	Working	Answer	Mark	Notes
Number				
14.	1.75 seen		2	M1
		8		A1
				Total 2 marks

	stion nber	Working	Answer	Mark		Notes
15.	(a)	Splits shape into rectangle & semicircle		4	M1	May be implied by working
		$\frac{\pi \times 2.7^2}{2}$ or value rounding to 11.4 or 11.5			M1	$\pi \to 11.451105$ 3.14 $\to 11.4453$ 3.142 $\to 11.45259$ Also award for equivalent multiple of π eg 3.645π, $\frac{729\pi}{200}$
		2 × 2.7 × 7.1 or 38.34			M1	Also accept 38.3
			49.8		A1	for 49.8 or for answer rounding to 49.78 or 49.79
	(b)	$P - 2L = \pi r + 2r$ oe		3	M1	for rearranging with both r terms on one side
		$P - 2L = (\pi + 2)r$ oe			M1	for factorising a correct expression (does not depend on a correct rearrangement)
			$\frac{P-2L}{\pi+2}$ oe		A1	
						Total 7 marks

	estion mber	Working	Answer	Mark	Notes
16.	(a)(i)		114	2	B1 cao
	(ii)	eg angle at the centre = 2 × angle at circumference			B1 Three key points must be mentioned 1. Angle at centre/middle/O/origin 2. Twice, double, 2× or half/ \frac{1}{2} as appropriate 3. angle at circumference/edge/perimeter (NOT e.g. angle D, angle ADB, angle at top, angle at outside)
	(b)		74	1	B1 cao
					Total 3 marks

Question Number	Working	Answer	Mark		Notes
17. (i)	$\frac{1}{7} \times \frac{2}{6}$ and no other terms		2	M1	
		$\frac{2}{42}$ or $\frac{1}{21}$ oe		A1	Also accept 0.05, 0.04, 0.047, 0.048 etc Sample space method - award 2 marks for a correct answer; otherwise no marks
(ii)	$\frac{1}{7} \times \frac{1}{6}$ or $\frac{2}{7} \times \frac{3}{6}$		3	M1	SC M1 for $\frac{1}{7} \times \frac{1}{7}$ or $\frac{2}{7} \times \frac{3}{7}$
	$\frac{1}{7} \times \frac{1}{6} + \frac{2}{7} \times \frac{3}{6}$			M1	M1 for $\frac{1}{7} \times \frac{1}{7} + \frac{2}{7} \times \frac{3}{7}$
		$\frac{7}{42}$ or $\frac{1}{6}$ oe		A1	Also accept 0.16, 0.16, 0.17, 0.166, 0.167 etc but not 0.2 Sample space method - award 3 marks for a correct answer; otherwise no marks
					Total 5 marks

Question Number	Working	Answer	Mark	Notes
18.	(BC =) 47 sin 32°		5	or for $(CD =)$ $\frac{47 \sin 32^{\circ}}{\sin 129^{\circ}}$
	24.906 at least 3 sf (may be implied by correct <i>BD</i>)			A1 or for CD = 32.048 at least 2 s (may be implied by correct BD)
	$\tan 51^\circ = \frac{"24.906"}{BD}$ or $\tan 39^\circ = \frac{BD}{BD}$			M1 or for $\cos 51^{\circ} = \frac{BD}{"32.048"}$
	$\tan 39^{\circ} = \frac{BD}{"24.906"}$ $(BD =) \frac{"24.906"}{\tan 51^{\circ}} \text{ or "24.906" } \tan 39^{\circ}$			M1 or for (<i>BD</i> =)"32.048"cos51°
		20.2		A1 for answer rounding to 20.2 (20.1686)
				Total 5 mar

Question Number	Working	Answer	Mark	Notes
19. (a)	$P = kQ^3$		3	M1 for $P = kQ^3$ but not for $P = Q^3$
	1350 = k × 3375			M1 for $1350 = k \times 3375$ Also award for $1350 = k \times 15^3$
		P = 0.4Q ³ oe		A1 $P = 0.4Q^3$ oe Award 3 marks if answer is $P = kQ^3$ oe but k is evaluated as 0.4 in part (a) or part (b)
(b)		3200	1	B1 ft from "0.4" × 8000 except for k = 1, if at least M1 scored in (a) (at least 1 d.p. accuracy in follow through)
				Total 4 marks

Question Number	Working	Answer	Mark		No	otes
20.	$a^2 \times 10^{2n}$		3	M1		
		$\frac{a^2}{10} \times 10^{2n+1}$		A1	for $\frac{a^2}{10}$ oe for $\times 10^{2n+1}$ oe	Award M1 A1 A1 for $\frac{a^2}{10} \times 10^{2n+1}$ even if M1 not awarded. Award M1 A1 A0 if $\frac{a^2}{10}$ oe seen. Award M1 A0 A1 if $\times 10^{2n+1}$ oe seen.
						Total 3 marks

Question	Working	Answer	Mark		Notes
Number 21. (a)	Use of areas to obtain a correct expression for <i>A</i> , which must be correctly punctuated. For example $(A =) 80 - 2 \times \frac{1}{2} x (10 - x) - 2 \times \frac{1}{2} x (8 - x)$ or $10 \times 8 - \frac{1}{2} x (10 - x) - \frac{1}{2} x (10 - x) - \frac{1}{2} x (8 - x) - \frac{1}{2} x (8 - x)$ or $80 - x (10 - x) - x (8 - x)$ or $80 - 2 \left(\frac{10x - x^2}{2} \right) - 2 \left(\frac{8x - x^2}{2} \right)$		3	B2	B1 for expression for area of triangle or pair of congruent triangles, for example $\frac{1}{2}x(10-x) \text{ or } \frac{1}{2}x(8-x)$ or $x(10-x)$ or $x(8-x)$ Condone omission of brackets for award of B1
	Correct simplification of a correct expression for A to obtain an expression which is equivalent to $2x^2 - 18x + 80$ For example $(A =) 80 - 10x + x^2 - 8x + x^2$ or $80 - (10x - x^2) - (8x - x^2)$ or $80 - (5x - \frac{1}{2}x^2) - (5x - \frac{1}{2}x^2) - (4x - \frac{1}{2}x^2) - (4x - \frac{1}{2}x^2)$			B1	dep on B2
(b)(i)		4 <i>x</i> –18	5	B2	B1 for 2 of 3 terms differentiated correctly
(ii)	" $4x - 18$ " = 0			M1	
		4.5 oe		A1	cao
(iii)		e coefficient of x^2 or U shape $\frac{d^2 A}{dx^2} = 4 \text{ which} > 0$		B1	
					Total 8 marks

Question Number	Working	Answer	Mark	Notes
22.	$x^2 + (2x - 3)^2 = 2$		6	M1 for correct substitution
	$x^{2} + 4x^{2} - 6x - 6x + 9 = 2$ or $x^{2} + 4x^{2} - 12x + 9 = 2$			B1 (indep) for correct expansion of $(2x-3)^2$ even if unsimplified
	$5x^2 - 12x + 7 (= 0)$			B1 for correct simplification Condone omission of '= 0'
	or $\frac{12 \pm \sqrt{4}}{10}$ or $\frac{12}{10} \pm \frac{\sqrt{4}}{10}$ or $\frac{6}{5} \pm \frac{1}{5}$			B1 for correct factorisation or for correct substitution into quadratic formula and correct evaluation of 'b² - 4ac' or for using square completion correctly as far as indicated
	$x = 1$ or $x = 1\frac{2}{5}$			A1 for both values of x dep on all preceding marks
		x = 1, y = -1 $x = 1\frac{2}{5}, y = -\frac{1}{5}$		A1 for complete, correct solutions (need not be paired) dep on all preceding marks No marks for $x = 1$, $y = -1$ with no working
				Total 6 marks

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Question	Working	Answer	Mark	Notes
Number				
23.	$2\pi r^2 + 2\pi rh$		5	M1 $\pi r^2 \pm 2\pi rh$
	$\frac{2\pi r^2 + 2\pi rh}{4\pi r^2} = 2$			Also award for $\frac{\pi r^2 + 2\pi rh}{4\pi r^2} = 2$
	4πr ²			
	$2\pi r^2 + 2\pi rh = 2 \times 4\pi r^2$ oe			M1 for $2\pi r^2 + 2\pi rh = 2 \times 4\pi r^2$ oe
				$2\pi r(r+h)$
				or $\frac{2\pi r(r+h)}{4\pi r^2}=2$
				If first M1 awarded for
				$\frac{\pi r^2 + 2\pi rh}{4\pi r^2} = 2$ award this
				${}$ = 2 award this
				second M1 also for
				$\pi r^2 + 2\pi r h = 2 \times 4\pi r^2 \text{ oe}$
	h = 3r oe			A1 If first M1 awarded for
				$\pi r^2 + 2\pi rh$
				$\frac{\pi r^2 + 2\pi rh}{4\pi r^2} = 2 \text{ and second M1}$
				$4\pi r^2$
				for $\pi r^2 + 2\pi r h = 2 \times 4\pi r^2$ oe
				Award this A1 also for $h = 3.5r$ oe
	2 "2 "			M1 dep on first two M1s
	$\frac{\pi r^2 \times "3r"}{r}$ oe			h must be of the form kr
	$-\frac{4}{3}\pi r^3$			ii must be of the form kr
	$\frac{3}{3}$			
		$\frac{9}{4}$ oe		A1
				Total 5 marks

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