Mark Scheme (Results)

November 2019

Pearson Edexcel GCSE (9-1)
In Mathematics (1MA1)
Higher (Calculator) Paper 3H

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## General marking guidance

These notes offer general guidance, but the specific notes for examiners appertaining to individual questions take precedence
1 All candidates must receive the same treatment. Examiners must mark the last candidate in exactly the same way as they mark the first.
Where some judgement is required, mark schemes will provide the principles by which marks will be awarded; exemplification/indicative content will not be exhaustive. When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the response should be sent to review.

2 All the marks on the mark scheme are designed to be awarded; mark schemes should be applied positively. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme. If there is a wrong answer (or no answer) indicated on the answer line always check the working in the body of the script (and on any diagrams), and award any marks appropriate from the mark scheme.

Questions where working is not required: In general, the correct answer should be given full marks.
Questions that specifically require working: In general, candidates who do not show working on this type of question will get no marks - full details will be given in the mark scheme for each individual question.

3 Crossed out work
This should be marked unless the candidate has replaced it with
an alternative response.
4 Choice of method
If there is a choice of methods shown, mark the method that leads to the answer given on the answer line.
If no answer appears on the answer line, mark both methods then award the lower number of marks.
5 Incorrect method
If it is clear from the working that the "correct" answer has been obtained from incorrect working, award 0 marks. Send the response to review for your Team Leader to check.

6 Follow through marks
Follow through marks which involve a single stage calculation can be awarded without working as you can check the answer, but if ambiguous do not award.
Follow through marks which involve more than one stage of calculation can only be awarded on sight of the relevant working, even if it appears obvious that there is only one way you could get the answer given.

7 Ignoring subsequent work
It is appropriate to ignore subsequent work when the additional work does not change the answer in a way that is inappropriate for the question or its context. (eg. an incorrectly cancelled fraction when the unsimplified fraction would gain full marks).
It is not appropriate to ignore subsequent work when the additional work essentially makes the answer incorrect (eg. incorrect algebraic simplification).

## 8 Probability

Probability answers must be given as a fraction, percentage or decimal. If a candidate gives a decimal equivalent to a probability, this should be written to at least 2 decimal places (unless tenths)
Incorrect notation should lose the accuracy marks, but be awarded any implied method marks.
If a probability fraction is given then cancelled incorrectly, ignore the incorrectly cancelled answer.
9 Linear equations
Unless indicated otherwise in the mark scheme, full marks can be gained if the solution alone is given on the answer line, or otherwise unambiguously identified in working (without contradiction elsewhere). Where the correct solution only is shown substituted, but not identified as the solution, the accuracy mark is lost but any method marks can be awarded (embedded answers).

10 Range of answers
Unless otherwise stated, when an answer is given as a range (e.g $3.5-4.2$ ) then this is inclusive of the end points (e.g 3.5, 4.2) and all numbers within the range.

11 Number in brackets after a calculation
Where there is a number in brackets after a calculation E.g. $2 \times 6(=12)$ then the mark can be awarded either for the correct method, implied by the calculation or for the correct answer to the calculation.

## 12 Use of inverted commas

Some numbers in the mark scheme will appear inside inverted commas E.g. "12" $\times 50$; the number in inverted commas cannot be any number - it must come from a correct method or process but the candidate may make an arithmetic error in their working.

13 Word in square brackets
Where a word is used in square brackets E.g. [area] $\times 1.5$ : the value used for [area] does not have to come from a correct method or process but is the value that the candidate believes is the area. If there are any constraints on the value that can be used, details will be given in the mark scheme.

Misread
If a candidate misreads a number from the question. Eg. uses 252 instead of 255 ; method or process marks may be awarded provided the question has not been simplified. Examiners should send any instance of a suspected misread to review.

## Guidance on the use of abbreviations within this mark scheme

M method mark awarded for a correct method or partial method
P process mark awarded for a correct process as part of a problem solving question
A accuracy mark (awarded after a correct method or process; if no method or process is seen then full marks for the question are implied but see individual mark schemes for more details)

C communication mark awarded for a fully correct statement(s) with no contradiction or ambiguity

B unconditional accuracy mark (no method needed)
oe or equivalent
cao correct answer only
ft follow through (when appropriate as per mark scheme)
sc special case
dep dependent (on a previous mark)
indep independent
awrt answer which rounds to
isw ignore subsequent working

| Paper: 1MA1/3H |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Question | Answer | Mark | Mark scheme | Additional guidance |
| $1 \quad \text { (a) }$ <br> (b) | $x^{2}-4 x-45$ $3 x(3 x+2)$ | M1 <br> A1 <br> B2 <br> (B1 | for 3 of 4 terms correct or 4 terms correct ignoring signs <br> cao <br> for $3 x(3 x+2)$ <br> for $3\left(3 x^{2}+2 x\right)$ or $x(9 x+6)$ or $3 x(a x+b)$ where $a$ and $b$ are integers or $(3 x+2)$ as a factor ) | 3 terms correct can be implied, eg $x^{2}-4 x+c$ |
| 2 <br> (a) <br> (b) | $157.668(255)$ $157.7$ | M1 <br> A1 <br> B1 | for 836.4 or 5.304(809139) or 28.141 or a truncated or rounded version of 157.668255 to no less than 3 sf for $157.668(255)$ <br> ft from part (a) provided answer to (a) has at least 5 sf | Answer must be given to at least 3 decimal places rounded or truncated Accept a clear indication of the decimal point. Check first 3 decimal places only |
| 3 | 35 to 42 | M1 <br> A1 | for drawing a suitable line of best fit or for a line from $x=34$ or for a point marked on the grid at $(34, y), y$ in the range 33 to 44 <br> answer in the range 35 to 42 | Line at $x=34$ does not have to be full length of grid but should be in or reach the data set. Acceptable values for the data set are $y=33$ to $y=44$ |


| Paper: 1MA1/3H |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Question | Answer | Mark | Mark scheme | Additional guidance |  |
| 4 | 18.6 | M1 | for finding 4 products within intervals (including end points) | $\operatorname{Min} f x$ | $\operatorname{Max} f x$ |
|  |  |  |  | 5 | 10 |
|  |  |  |  | 20 | 30 |
|  |  |  |  | 105 | 140 |
|  |  |  |  | 160 200 <br> $\Sigma " f x "$ must come from 4 products $f x$ within intervals (including end points) |  |
|  |  | M1 |  | $\Sigma " f x "$ must come from 4 products $f x$ within intervals (including end points) |  |
|  |  | A1 | for 18.6(111...) |  |  |
| 5 | 37000 | B1 | cao |  |  |
| 6 | 50 | B1 | for finding the time difference, eg, 1 hr 18 mins or 78 mins oe | Allow 1.18 for this mark 118 scores B0 |  |
|  |  | P1 | for correct process to convert minutes to hours, eg $18 \div 60(=0.3)$ or $78 \div 60(=1.3)$ <br> or for a correct process to convert speed in miles per minute to mph eg "0.833.." $\times 60$ | For a conversion of time or speed |  |
|  |  | P1 | for using speed $=$ distance $\div$ time eg, $65 \div[$ time $]$ or $65 \div 78(=0.833$.. $)$ | [time] is what the candidate clearly indicates as time difference |  |
|  |  | A1 | cao |  |  |
|  |  |  | SCB2 for $83(.333 \ldots)$ seen as the answer |  |  |


| Paper: 1MA1/3H |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Question | Answer | Mark | Mark scheme | Additional guidance |
| 7 (a) | $3.246 \times 10^{7}$ | B1 | cao |  |
| (b) | 0.00496 | B1 |  |  |
| (c) | No with explanation | C1 | No and explanation that B is bigger as the power of 10 is bigger. <br> Acceptable examples <br> She is incorrect as $10^{8}$ is smaller than $10^{9}$ <br> No, because B has more digits than A <br> No, $A$ is millions but $B$ is billions <br> No, if you subtract A from B the answer is positive (but if you subtract <br> $B$ from $A$ the answer is negative) <br> $A=621200000, B=4730000000$, $B$ is bigger <br> No because she did not take into account standard form <br> No as when you find the ordinary number $B$ is greater than $A$ <br> Not acceptable examples <br> Yes... <br> $\mathrm{A}=5$ zeros after the number where as $\mathrm{B}=7$ zeros after the number <br> No as $4.73 \times 10^{9}$ is one more than $6.212 \times 10^{8}$ <br> 6.212 is to the power of 8 and 4.73 is to the power of 9 so there is an extra digit <br> Asma is wrong because she has more numbers behind the decimal point which means that it will be bigger than A <br> No B has more zeros | Decision eg "No" may be seen by the question. "She is incorrect" is equivalent to "no" |


| Paper: 1MA1/3H |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Question | Answer | Mark | Mark scheme | Additional guidance |
| 8 | 45 | P1 | for $180-117(=63)$ <br> or states, or uses, exterior angle $+x=117$ | Angles may be shown on the diagram. <br> Any angle labelled correctly as 63 and not contradicted scores this mark |
|  |  | P1 | for process to find the exterior or the interior angle of the pentagon, eg $360 \div 5(=72)$ or $180-(360 \div 5)(=108)$ or $((5-2) \times 180) \div 5$ (=108) | Exterior $=108$ or interior $=72$ does not score the mark |
|  |  | P1 | for a complete process to find $x$, eg 180 - " 72 " - " 63 " or " 108 " - " 63 " or 117 -" 72 " |  |
|  |  | A1 | cao | An answer of 45 with no supporting working scores 0 |
| 9 | Enlargement | B2 <br> (B1 | vertices at $(2.5,1)(2.5,6)(5,6)$ <br> for triangle of the correct size and orientation in the wrong position <br> or a correct enlargement of a different scale factor centre $(0,1)$ <br> or correct orientation with 2 of 3 vertices correct) |  |
| $10 \quad(\mathrm{a})$ | 8.5 | M1 | for multiplying both sides by 7 as a first step eg $9+x=7(11-x)$ or dividing each term on the left hand side by $7 \operatorname{eg} \frac{9}{7}+\frac{x}{7}=11-x$ | $\times 7$ written near the equation is not enough for this mark |
|  |  | M1 | (dep M1) for method to isolate the $x$ terms on one side |  |
|  |  | A1 |  |  |
|  | $4(y+3)$ | B1 | $4(y+3)$ or $4 y+12$ |  |


| Paper: 1MA1/3H |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Question | Answer | Mark | Mark scheme | Additional guidance |
| 11 | 0.1709 | M1 <br> M1 <br> A1 | for one product, $0.07 \times 0.98(=0.0686)$ or $0.93 \times 0.11(=0.1023)$ or $0.07 \times 0.02(=0.0014)$ or $0.93 \times 0.89(=0.8277)$ <br> for a fully correct method, eg $0.07 \times 0.98+0.93 \times 0.11$ or $1-(0.07 \times 0.02)-(0.93 \times 0.89)$ oe | If all products shown, award this mark |
| 12 | Box plot | M1 <br> M1 <br> A1 | for correctly identifying one of the LQ (188), median (197) or UQ (209) from the stem leaf <br> for showing a box and at least 3 correctly plotted values from 173, 188, 197, 209, 219 <br> for a fully correct box plot | May be implied by one of these values being correctly plotted. |
| 13 | 739 | P1 <br> P1 <br> P1 <br> A1 | process to find the volume of C, eg $\pi \times 3^{2} \times 25(=706.8583471$ or $225 \pi$ ) <br> process to find the volume of $A$ or the volume of $B$, eg "706.8..." $\times \frac{2}{2+13}(=94.24777961$ or $30 \pi)$ <br> or " $706.8 \ldots$ " $\times \frac{13}{2+13}(=612.6105675$ or $195 \pi)$ <br> or process to work with density and ratio, $\operatorname{eg}(2 \times 1.21+13 \times 1.02)(=15.68)$ <br> process to find the mass of C, eg " $30 \pi$ " $\times 1.21(=114.0398133)+$ " $195 \pi " \times 1.02(=624.8627788)$ <br> or " $225 \pi$ " $\times$ " 15.68 " $\div(2+13)$ <br> for an answer in the range 738.5 to 739 | For use of 3.14 <br> Volume of C is 706.5 <br> Volume of A is 94.2 <br> Volume of B is 612.3 <br> Mass of A is 113.982 <br> Mass of B is 624.546 <br> Do not award accuracy mark if the figure is from obvious incorrect working |




| Paper: 1MA1/3H |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Question | Answer | Mark | Mark scheme | Additional guidance |
| 17 | 2.7 and -0.7 | M1 | for $x^{2}-3=2 x-1$ oe or $x^{2}-3-2 x+1(=0)$ or completing the square eg $(y=)(x-1)^{2}-1-2$ |  |
|  |  | M1 | (dep M1) draws graph of $y=2 x-1$ or drawing the translated graph or describing the translation in words or $-1.7+1(=-0.7)$ or $1.7+1(=2.7)$ | Line segments required <br> For 1.7 allow from 1.6 to 1.8 <br> For -1.7 allow from -1.8 to -1.6 |
|  |  | M1 | shows the points of intersection clearly for the given quadratic graph and linear graph or for one correct solution from appropriate supportive working | Points indicated or attempt to read off $x$-axis at the appropriate points - maybe indicated by dashes |
|  |  | A1 | for $x$ in the range 2.6 to 2.8 and -0.6 to -0.8 <br> SCB2 for plotting $y=2 x+1$ and values for x in the range -1.1 to -1.3 and 3.1 to 3.3 | No marks will be awarded for correct answers only |
| 18 | 1.95 | P1 | for correct substitution into the cosine rule, eg $3.4^{2}=6.1^{2}+6.2^{2}-2 \times 6.1 \times 6.2 \times \cos B C A$ | Can be any angle within triangle $A B C$ |
|  |  | P1 | for a full process to find $B C A$ eg $(\cos B C A=) \frac{6.1^{2}+6.2^{2}-3.4^{2}}{2 \times 6.1 \times 6.2}$ or $(B C A=) 32(.08046913 \ldots)$ | P2 can be awarded for $B C A=32(.08046913 \ldots)$ |
|  |  | P1 | correct substitution into the sine rule, $\operatorname{eg} \frac{D C}{\sin \left(" 32.08 \ldots . . " \times \frac{2}{5}\right)}=\frac{6.2}{\sin \left(180-" 32.08 \ldots "-\left(" 32.08 \ldots . . " \times \frac{2}{5}\right)\right.}$ |  |
|  |  | P1 | for complete process to find $D C \operatorname{eg}(D C=) \frac{6.2 \times \sin " 12.832 "}{\sin " 135.088 "}$ |  |
|  |  | A1 | Answer in the range 1.94 to 1.951 | Must not come from incorrect processing |


| Paper: 1MA1/3H |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Question | Answer | Mark | Mark scheme | Additional guidance |
| 19 | 3.4 | M1 <br> M1 <br> A1 | for drawing a suitable tangent at $t=6$ for a full method to find the gradient of the tangent at $t=6$, eg $20 \div 5.8$ answer in the range 3.05 to 3.7 | Use of change in $y$ over change in $x$ Answers of $\frac{10}{6}$ oe scores no marks |
| 20 | $n^{2}-2 n$ | M1 <br> A1 | for correct deduction from differences, eg 2 nd difference of 2 implies $1 n^{2}$ <br> or gives a quadratic expression which includes the term $1 n^{2}$ or states $1,4,9,16,25$ and deduces $2,4,6,8,10$ oe |  |
| 21 | $\frac{1}{81}$ | M1 <br> A1 | for finding the probability of heads eg $\sqrt[4]{\frac{16}{81}}\left(=\frac{2}{3}\right)$ or for finding the probability of tails $1-\sqrt[4]{\frac{16}{81}}\left(=\frac{1}{3}\right)$ oe | Seeing a probability of $\frac{2}{3}$ or $\frac{1}{3}$ is enough for this mark |


| Paper: 1MA1/3H |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Question | Answer | Mark | Mark scheme | Additional guidance |
| 22 | $7 x$ | M1 | multiplication by reciprocal, eg $\frac{7(x-2)}{(x-2)(x+6)} \times \frac{x(x+6)(x-6)}{x-6}$ | Independent mark, may be awarded at any point |
|  |  | M1 | for factorising the numerator or denominator of the $1^{\text {st }}$ fraction, eg $\frac{7(x-2)}{(x-2)(x+6)}$ or $\frac{7(x-2)}{x^{2}+4 x-12}$ or $\frac{7 x-14}{(x-2)(x+6)}$ |  |
|  |  | M1 | for factorising the denominator of the second fraction, $\operatorname{eg} \frac{x-6}{x(x+6)(x-6)}\left(=\frac{1}{x(x+6)}\right)$ |  |
|  |  | A1 | completing the algebra to reach $7 x$ |  |
| 23 | 264 | P1 | correct substitution into the volume formula, eg $56.8=\frac{1}{3} \times \pi \times r^{2} \times 3.6$ |  |
|  |  | P1 | completes process to find base radius or the value of $\mathrm{r}^{2}$, eg $r=$ $\sqrt{\frac{56.8 \times 3}{\pi \times 3.6}}(=3.88158 \ldots) \text { or } \mathrm{r}^{2}=\frac{56.8}{1.2 \pi}(=15.066)$ |  |
|  |  | P1 | Uses Pythagoras to find the sloping length, eg $\sqrt{ } 3.88 \ldots{ }^{2}+3.6^{2}(=5.29 \ldots .$. |  |
|  |  | P1 | process to find an equation in $A O B$, eg $\pi \times$ " 3.88 " $\times$ " 5.29 " $=\frac{A O B}{360} \times \pi$ $\times$ " 5.29 " ${ }^{2}$ <br> or $\frac{A O B}{360} \times \pi \times 2 \times$ " $5.29 "=2 \times \pi \times " 3.88$ " <br> or $\frac{A O B}{360} \times " 5.29 "=" 3.88 "$ | $A O B$ does not need to be the subject of the equation |
|  |  | A1 | answer in the range 263.9 to 264.1 |  |


| Paper: 1MA1/3H |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Question | Answer | Mark | Mark scheme | Additional guidance |
| 24 | 4:3 | P1 | Process to find a missing vector using the given ratios as fractions, eg. $\frac{1}{3}$ of $\overrightarrow{O X}\left(=\frac{1}{3} \mathbf{a}\right)$ or. $\frac{1}{4}$ of $\overrightarrow{O Y}\left(=\frac{1}{4} \mathbf{b}\right)$ |  |
|  |  | P1 | for a process to use $\overrightarrow{Z O}=\overrightarrow{Y X}=\mathbf{a}-\mathbf{b}$ oe |  |
|  |  | P1 | for a process to find either $\overrightarrow{Z P}$ or $\overrightarrow{Z R}$ in terms of $\mathbf{a}$ and $\mathbf{b}$, eg. either $\overrightarrow{Z P}=\mathbf{a}-\mathbf{b}+\frac{1}{3} \mathbf{a}$ or $\overrightarrow{Z R}=\mathbf{a}-\mathbf{b}+\frac{1}{4} \mathbf{b}$ | The award of this mark implies the first two process marks. |
|  |  | P1 | for a process to write $\overrightarrow{Z P}$ and $\overrightarrow{Z R}$ as multiples of the same vector, eg. multiplying both by 12 to get the ratio, $\frac{4}{3}(\mathbf{a}-0.75 \mathbf{b})$ and $\mathbf{a}-0.75 \mathbf{b}$ respectively |  |
|  |  | A1 | oe |  |

## Modifications to the mark scheme for Modified Large Print (MLP) papers: 1MA1 3H

Only mark scheme amendments are shown where the enlargement or modification of the paper requires a change in the mark scheme.
The following tolerances should be accepted on marking MLP papers, unless otherwise stated below:
Angles: $\pm 5^{\circ}$
Measurements of length: $\pm 5 \mathrm{~mm}$


| PAPER: 1MA1/3H |  |  |  |
| :---: | :---: | :---: | :---: |
| Question |  | Modification | Mark scheme notes |
| 9 |  | Wording added 'It shows triangle A and triangle B on a coordinate grid.' Diagram enlarged. Label removed from inside triangle. Shading removed. Enlargement drawn at $(2.5,1),(2.5,6)(5,6)$ Triangles labelled as 'triangle A' and 'triangle B'. Cross removed from $(0,1)$ on the diagram. Grid cut at 7 on the x axis and 6 on the y axis. Grid cut before the $x$ and $y$ axes labels. <br> Question wording now 'Describe fully the transformation that maps triangle A onto triangle B.' Three answer lines provided. Braille only: Two labelled shapes, triangle A and triangle B. | Amended mark scheme as follows: <br> B1 for "enlargement scale factor 2.5" <br> B1 for "centre $(0,1)$ <br> Award B0 for any mention of a different transformation. |
| 10 | (a) | MLP only: $x$ changed to $y$. | Standard mark scheme but note letter change. |
| 11 |  | Diagram enlarged. | Standard mark scheme |
| 12 |  | Diagrams enlarged. Key moved above and to the left of the stem and leaf diagram. Horizontal line added to the base of the stem and leaf diagram. <br> Wording changed to 'Look at Diagram 1 and Diagram 2 for Question 12... Diagram 1 shows a stem and leaf diagram. Diagram 2 shows a grid.' <br> Wording added 'below Diagram 1'. <br> Numbers in the stem and leaf changed (see table below) | Amended mark scheme: <br> P1 for correctly identifying one of the LQ (185), median (195) or UQ (205) from the stem leaf M1 for showing a box and at least 3 correctly plotted values from 175,185 , 195, 205, 215 <br> A1 for a fully correct box plot |

## PAPER: 1MA1/3H



| PAPER: 1MA1/3H |  | Modification | Mark scheme notes |
| :---: | :--- | :--- | :---: |
| Question |  | Diagrams enlarged and model and shape may be provided. <br> 23 <br> Sector $O A C B$ labelled as Diagram 1 and the cone labelled as Diagram 2. <br> Add wording 'Diagram 1 shows a sector $O A C B \ldots$ Diagram 2 shows a hollow cone...' <br> There may be a model of the hollow cone and a cut out shape of the sector $O A C B$. <br> Wording added 'The formulae are shown above Diagram 1 and Diagram 2 in the Diagram Book.' <br> Dashed lines made longer and thicker. |  |
| 24 |  | Diagram enlarged. | Standard mark scheme |

