## A-LEVEL Mathematics

Paper 3<br>Mark scheme

Specimen

Version 1.2

Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts. Alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Assessment Writer.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Further copies of this mark scheme are available from aqa.org.uk

## Mark scheme instructions to examiners

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## General

The mark scheme for each question shows:

- the marks available for each part of the question
- the total marks available for the question
- marking instructions that indicate when marks should be awarded or withheld including the principle on which each mark is awarded. Information is included to help the examiner make his or her judgement and to delineate what is creditworthy from that not worthy of credit
- a typical solution. This response is one we expect to see frequently. However credit must be given on the basis of the marking instructions.

If a student uses a method which is not explicitly covered by the marking instructions the same principles of marking should be applied. Credit should be given to any valid methods. Examiners should seek advice from their senior examiner if in any doubt.

## Key to mark types

\(\left.\begin{array}{ll}\hline M \& mark is for method <br>
dM \& mark is dependent on one or more M marks and is for method <br>

\hline R \& mark is for reasoning\end{array}\right]\)| mark is dependent on M or m marks and is for accuracy |
| :--- |
| A | | mark is independent of M or m marks and is for method and |
| :--- |
| B |

## Key to mark scheme abbreviations

| CAO | correct answer only |
| :--- | :--- |
| CSO | correct solution only |
| ft | follow through from previous incorrect result |
| 'their' | Indicates that credit can be given from previous incorrect result |
| AWFW | anything which falls within |
| AWRT | anything which rounds to |
| ACF | any correct form |
| AG | answer given |
| SC | special case |
| OE | or equivalent |
| NMS | no method shown |
| PI | possibly implied |
| SCA | substantially correct approach |
| sf | significant figure(s) |
| dp | decimal place(s) |

Examiners should consistently apply the following general marking principles

## No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award full marks. However, the obvious penalty to students showing no working is that incorrect answers, however close, earn no marks.

Where a question asks the student to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns full marks, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains no marks.

Otherwise we require evidence of a correct method for any marks to be awarded.

## Diagrams

Diagrams that have working on them should be treated like normal responses. If a diagram has been written on but the correct response is within the answer space, the work within the answer space should be marked. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working, and is not, therefore, penalised.

## Work erased or crossed out

Erased or crossed out work that is still legible and has not been replaced should be marked. Erased or crossed out work that has been replaced can be ignored.

## Choice

When a choice of answers and/or methods is given and the student has not clearly indicated which answer they want to be marked, only the last complete attempt should be awarded marks.

| Q | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :---: | :---: | :---: | :---: |
| 1 | Circles correct answer | A01.1b | B1 | 18 |
|  | Total |  | 1 |  |
| 2(a) | Makes clear attempt to use the cosine rule | A03.1a | M1 | $\begin{align*} & 6^{2}=3^{2}+5^{2}-2 \times 3 \times 5 \cos \theta \\ & \cos \theta=\frac{3^{2}+5^{2}-6^{2}}{30}=-\frac{1}{15} \\ & \therefore \sin \theta=\sqrt{1-\left(-\frac{1}{15}\right)^{2}} \\ & \sin \theta=\frac{4 \sqrt{14}}{15} \tag{AG} \end{align*}$ |
|  | Uses trig identity with 'their' $\cos \theta$ | A01.1a | M1 |  |
|  | Constructs rigorous argument leading to correct result AG <br> Only award if they have a completely correct solution, which is clear, easy to follow and contains no slips | AO2.1 | R1 |  |
| (b) | Writes down correct angle | AO2.2a | B1 | 1.64 |
| (c) | Uses 'their' angle in $\frac{1}{2} r^{2} \theta$ | A01.1a | M1 | $A=\frac{1}{2} \times 5^{2} \times 1.64$ |
|  | Correct area <br> FT use of incorrect obtuse angle provided both M1 marks awarded in part (a) and M1 awarded in (c) | A01.1b | A1F | $=20.5 \mathrm{~m}^{2}$ |
|  | Total |  | 6 |  |


| Q | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :---: | :---: | :---: | :---: |
| 3(a) | Translates proportionality into a differential equation involving $\frac{\mathrm{d} A}{\mathrm{~d} t}, A$ and a constant of proportionality. | AO3.3 | M1 | $\begin{aligned} & \frac{\mathrm{d} A}{\mathrm{~d} t} \propto A \\ & \Rightarrow \frac{\mathrm{~d} A}{\mathrm{~d} t}=k A \\ & \Rightarrow \int \frac{1}{A} \mathrm{~d} A=\int k \mathrm{~d} t \\ & \Rightarrow \ln A=k t+c \\ & \Rightarrow A=\mathrm{e}^{k t+c} \\ & \Rightarrow A=B \mathrm{e}^{k t} \quad \text { AG } \end{aligned}$ |
|  | Separates variables | A01.1a | M1 |  |
|  | Integrates both of 'their' sides correctly | A01.1b | A1F |  |
|  | Constructs a rigorous mathematical argument that supports use of the given model. AG <br> Only award if they have a completely correct solution, which is clear, easy to follow and contains no slips. | AO2.1 | R1 |  |
| (b)(i) | States correct value of $B$ | A01.1b | B1 | $B=0.25 \text { or } B=\frac{1}{4}$ |
| (b)(ii) | Uses $t=20$ and $A=0.5$ to find $k$ | A03.1b | M1 | $\begin{aligned} & \text { When } t=20, A=0.5 \\ & \Rightarrow 0.5=0.25 \mathrm{e}^{20 k} \\ & \Rightarrow 20 k=\ln 2 \\ & \Rightarrow k=\frac{1}{20} \ln 2 \\ & \Rightarrow A=\frac{1}{4}\left(\mathrm{e}^{\ln 2}\right)^{\frac{t}{20}} \\ & \Rightarrow A=2^{-2} \times 2^{\frac{t}{20}} \\ & \Rightarrow A=2^{\frac{t}{20}-2} \quad \text { AG } \end{aligned}$ |
|  | Finds correct value of $k$ | A01.1b | A1 |  |
|  | Substitutes 'their' $k$ to get A in terms of $t$ | A01.1a | M1 |  |
|  | Constructs rigorous and convincing argument to show $A=2^{\frac{t}{20}-2}$ <br> Using correct notation throughout. AG | AO2.1 | R1 |  |
| (b)(iii) | Uses the model to set up correct equation and attempt to find $t$ | AO3.4 | M1 | $\begin{aligned} & 2 \pi=2^{\frac{t}{20}-2} \\ & t=93.03 \text { days } \end{aligned}$ |
|  | Finds correct value of $t$ | A01.1b | A1 |  |
| (c) | States any sensible and relevant limitation of the model that is specified in terms of the pond, area, weed, rate of change or time. | A03.5b | E1 | Model predicts that the area of weed will increase without limit and this is not possible since the area of the pond is $4 \pi$ |
| (d) | Any sensible and relevant refinement to the model that is specified in terms of the pond, area, weed, rate of change or time | AO3.5c | E1 | Introduce a limiting factor such as fish eating weed or rate of growth decreases as surface area covered |
|  | Total |  | 13 |  |


| Q | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :---: | :---: | :---: | :---: |
| 4 | Selects a method of integration, which could lead to a correct solution. Evidence of integration by parts <br> OR an attempt at integration by inspection. | A03.1a | M1 | $\begin{aligned} & u=\ln 2 x ; \quad \frac{\mathrm{d} v}{\mathrm{~d} x}=x^{3} \\ & \frac{\mathrm{~d} u}{\mathrm{~d} x}=\frac{1}{x} ; \quad v=\frac{x^{4}}{4} \\ & {\left[\frac{x^{4}}{4} \ln (2 x)\right]_{1}^{2}-\int_{1}^{2} \frac{x^{3}}{4} \mathrm{~d} x} \\ & {\left[\frac{x^{4}}{-} \ln (2 x)-\frac{x^{4}}{2}\right]^{2}} \end{aligned}$ |
|  | Applies integration by parts formula correctly <br> OR correctly differentiates an expression of the form $A x^{4} \ln 2 x$ | A01.1b | A1 | $\begin{aligned} & =\left(\frac{2^{4}}{4} \ln (4)-\frac{2^{4}}{16}\right)-\left(\frac{1}{4} \ln (2)-\frac{1}{16}\right) \\ & \frac{31}{4} \ln 2-\frac{15}{16} \end{aligned}$ |
|  | Obtains correct integral, condone missing limits. | A01.1b | A1 | so $p=\frac{31}{4} \quad q=-\frac{15}{16}$ |
|  | Substitutes correct limits into 'their' integral | A01.1a | M1 | ALT $\frac{\mathrm{d}}{\mathrm{~d} x}\left(x^{4} \ln 2 x\right)=4 x^{3} \ln 2 x+x^{4} \cdot \frac{1}{x}$ |
|  | Obtains correct $p$ and $q$ <br> FT use of incorrect integral provided both M1 marks have been awarded | A01.1b | A1F | $\begin{aligned} & \therefore \int_{1}^{2} x^{3} \ln 2 x \mathrm{~d} x=\left[\frac{1}{4}\left(x^{4} \ln 2 x-\frac{x^{4}}{4}\right)\right]_{1}^{2} \\ & =\left(\frac{2^{4}}{4} \ln (4)-\frac{2^{4}}{16}\right)-\left(\frac{1}{4} \ln (2)-\frac{1}{16}\right) \\ & \frac{31}{4} \ln 2-\frac{15}{16} \\ & p=\frac{31}{4} \quad q=-\frac{15}{16} \end{aligned}$ |
|  | Total |  | 5 |  |


|  | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :---: | :---: | :---: | :---: |
| 5(a) | Uses binomial expansion, with at least two terms correct, may be un-simplified | A01.1a | M1 | $(1+6 x)^{\frac{1}{3}} \approx 1+\frac{1}{3} \cdot 6 x+\frac{1}{3} \cdot \frac{-2}{3} \cdot \frac{(6 x)^{2}}{2}$ |
|  | Obtains correct simplified answer | A01.1b | A1 | $(1+6 x)^{\frac{1}{3}} \approx 1+2 x-4 x^{2}$ |
| (b) | Determines the correct value for $x$ and substitutes this into 'their' answer to part (a) | A03.1a | M1 | $x=0.03$ |
|  | Obtains correct approximation for 'their' answer to part (a) <br> FT allowed only if M1 from part (a) and M1 from part (b) have been awarded | A01.1b | A1F | $\begin{aligned} \sqrt[3]{1.18} & \approx 1+2(0.03)-4(0.03)^{2} \\ & \approx 1.0564 \end{aligned}$ |
| (c) | Explains the limitation of the expansion found in part (a) with reference to $x=\frac{1}{2}$ | AO2.4 | E1 | Although $\left(1+6 \times \frac{1}{2}\right)^{\frac{1}{3}}=\sqrt[3]{4}$ $x=\frac{1}{2}$ cannot be used since the expansion is only valid for $\|x\|<\frac{1}{6}$ |
|  | Total |  | 5 |  |


| Q | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :---: | :---: | :---: | :---: |
| 6 | Uses partial fractions with linear denominators $\frac{6 x+1}{6 x^{2}-7 x+2}=\frac{A}{a x+b}+\frac{B}{c x+d}$ | A03.1a | M1 | $\begin{aligned} & \frac{6 x+1}{6 x^{2}-7 x+2}=\frac{A}{3 x-2}+\frac{B}{2 x-1} \\ & A(2 x-1)+B(3 x-2)=6 x+1 \end{aligned}$ |
|  | Obtains correct linear denominators | A01.1b | B1 | $x=\frac{2}{3}, A\left(\frac{1}{3}\right)=5 \text { so } A=15$ |
|  | Obtains at least one numerator correct (using any valid method, eg equating coefficients or substitution of values) | A01.1b | A1 | $\begin{aligned} & x=\frac{1}{2}, \quad B\left(-\frac{1}{2}\right)=4 \text { so } B=-8 \\ & \int_{1}^{2} \frac{15}{3 x-2}-\frac{8}{2 x-1} \mathrm{~d} x \\ & \quad=[5 \ln (3 x-2)-4 \ln (2 x-1)]_{1}^{2} \end{aligned}$ |
|  | Obtains partial fractions completely correct | A01.1b | A1 | $\begin{aligned} & =5 \ln (4)-4 \ln (3)-(5 \ln (1) 4 \ln (1)) \\ & =10 \ln (2)-4 \ln (3) \end{aligned}$ |
|  | Integrates 'their' partial fractions, must include logs $p \ln (a x+b)+q \ln (c x+d)$ | A01.1a | M1 |  |
|  | 'Their' integral correct (ignore limits) | A01.1b | A1F |  |
|  | Substitutes limits into 'their' integral | A01.1a | M1 |  |
|  | Correct final answer in correct form CAO | A01.1b | A1 |  |
|  | Total |  | 8 |  |


| Q | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :---: | :---: | :---: | :---: |
| 7(a) | Finds $2^{\text {nd }}$ derivative and sets up an inequality | A03.1a | M1 | $\begin{aligned} & \frac{\mathrm{d} y}{\mathrm{~d} x}=-2 x \mathrm{e}^{-x^{2}} \\ & \frac{\mathrm{~d}^{2} y}{\mathrm{~d} x^{2}}=-2 \mathrm{e}^{-x^{2}}+4 x^{2} \mathrm{e}^{-x^{2}} \\ & -2 \mathrm{e}^{-x^{2}}+4 x^{2} \mathrm{e}^{-x^{2}}<0 \\ & 4 x^{2}-2<0 \\ & -\frac{\sqrt{2}}{2}<x<\frac{\sqrt{2}}{2} \end{aligned}$ |
|  | Obtains correct first derivative | A01.1b | A1 |  |
|  | Obtains second derivative correct from 'their' first derivative | A01.1b | A1F |  |
|  | Deduces correct final inequality (could use set notation) | AO2.2a | A1 |  |
| (b) | Uses trapezium rule | A01.1a | M1 | $\begin{aligned} \int_{0.1}^{0.5} \mathrm{e}^{-x^{2}} \mathrm{~d} x & \approx \\ \approx & \frac{0.1}{2}\left(\mathrm{e}^{-0.01}+\mathrm{e}^{-0.25}\right. \\ & \left.+2\left(\mathrm{e}^{-0.04}+\mathrm{e}^{-0.09}+\mathrm{e}^{-0.16}\right)\right) \\ & \approx 0.3611 \end{aligned}$ |
|  | Trapezium rule entries all correct | A01.1b | A1 |  |
|  | Finds correct value | A01.1b | A1 |  |
| (c) | References area being completely within concave section So... | AO2.4 | E1 | $[0.1,0.5] \subset\left[-\frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2}\right]$ <br> $\therefore$ area is completely within concave section <br> Hence trapezia lie below curve and give an under-estimate for the area |
|  |  |  |  |  |
|  | Trapezia all fall completely underneath the curve therefore underestimate (only award this mark if previous E1 has been awarded) | AO2.4 | E1 |  |
| (d) | Uses suitable rectangle to obtain over-estimate | A03.1a | B1 | Using a rectangle with the left hand edge the same height as the curve will produce an overestimate <br> Area of rectangle $=$ $\begin{aligned} & 0.4 \times \mathrm{e}^{-0.1^{2}}=0.396 \ldots \\ & \therefore \quad 0.36<A<0.40 \\ & \text { So } A=0.4 \text { to } 1 \mathrm{dp} \end{aligned}$ |
|  | Explains that this rectangle lies above the curve | AO2.4 | E1 |  |
|  | Constructs rigorous mathematical argument about accuracy, which leads to required result <br> Only award if they have a completely correct solution, which is clear, easy to follow and contains no slips. | AO2.1 | R1 |  |
|  | Total |  | 12 |  |


| Q | Marking Instructions | AO | Marks | Typical Solution |
| ---: | :--- | :---: | :---: | :--- |
| $\mathbf{8 ( a )}$ | Circles correct answer | AO1.2 | B1 | The 2065 households in the village |
| (b) | Circles correct answer | AO1.2 | B1 | Simple random |
| 9(a) | Finds value for $p$ | AO1.1a | M1 | $p=\frac{1680}{2400}=0.7$ |
|  | Finds correct probability <br> from calculator | AO1.1b | A1 | Using $X \sim$ B(25,0.7), <br> $\mathrm{P}(X=22)=0.0243$ |
| (b) | Explains the reason why <br> the model may no longer <br> apply in context | AO3.5b | E1 | It is likely that all the houses (and <br> gardens) will be of similar types, and <br> hence similar owners, so not likely to <br> be independent as binomial model <br> requires. |
|  |  | $\mathbf{2}$ |  |  |


| Q | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :--- | :---: | :---: | :--- |
| $\mathbf{1 0 ( a )}$ | Indicates that 'Semi- <br> skimmed milk' is part of <br> the whole' Skimmed milks' <br> category. | AO2.4 | E1 | In Figure 2, the vertical axis represents <br> 'Skimmed milks' whereas in Figure 1 <br> the vertical axis represents 'Semi- <br> skimmed milk' that is just one part of <br> the' Skimmed milks' category. Hence, <br> for each region, the recorded values for <br> 'Semi-skimmed milk' will always be <br> lower that the ones for 'Skimmed milks'. |
| (b)(i) | States: strong positive <br> correlation between <br> purchases of 'Semi- <br> skimmed milk' and <br> 'Liquid wholemilk, full <br> price' for most regions. | AO2.5 | B1 | Regions A, B, D, F, G, H and J indicate <br> strong positive correlation between <br> purchases of 'Semi-skimmed milk' and <br> 'Liquid wholemilk, full price'. |
| Identifies regions C and E <br> as outliers | AO3.2b | E1 | Regions C and E do not follow the <br> same pattern as the other regions in <br> terms of purchases of skimmed milk <br> and wholemilk <br> or regions C and E can be excluded as <br> they appear to be outliers. |  |
|  | AO3.2b |  |  |  |


| Q | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :--- | :---: | :---: | :--- |
| 10(b)(ii) | States that there is <br> evidence of negative <br> correlation between <br> purchases of 'Mineral or <br> spring water' and <br> 'Skimmed milk'. | AO3.1b | B1 | Scatter graph indicates evidence of <br> negative correlation between <br> consumption of 'Mineral or spring water' <br> and 'Skimmed milks'. |
|  | The correlation is <br> between water and milk <br> purchases within the <br> regions and not between <br> purchases made by <br> individual people so <br> Bilal's claim is not proven | AO2.3 | E1 | Bilal's claim is not supported because <br> the correlation in figure 2 is between <br> water and milk purchases within the <br> regions and he is assuming that <br> individuals will follow a similar pattern <br> but the data does not tell us anything <br> about individuals, it refers to average <br> purchases made within the nine <br> regions. |
| (c) | Identifies London | AO2.2b | B1 | London |
|  | Gives valid reason based <br> on knowledge of the LDS | AO2.4 | E1 | Having studied the LDS I have <br> identified a clear trend: London is a <br> frequent outlier in most categories |
|  | 7 |  |  |  |


| Q | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :--- | :---: | :---: | :--- |
| 11(a) | Finds correct value of $k$ | AO1.1b | B 1 | $k=\frac{1}{16}$ |
| (b) | Selects relevant probability | AO1.1a | M 1 | $\mathrm{P}(\geq 2$ checkouts staffed) <br> $\frac{3}{16}+k=\frac{3}{16}+\frac{1}{16}=\frac{1}{4}$ |
|  | Finds correct probability | AO1.1b | A1F | ALT <br> FT 'their' value of $k$ found in part (a) |
|  |  | $\mathrm{P}(\geq 2$ checkouts staffed $)$ <br> $1-\frac{3}{4}=\frac{1}{4}$ |  |  |


| Q | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :---: | :---: | :---: | :---: |
| 12(a) | States both hypotheses correctly for one-tailed test | AO2.5 | B1 | $X=$ number of Christmas holidays without illness since January 2007 $X \sim B(7, p)$ <br> $\mathrm{H}_{0} \quad p=0.65$ <br> $\mathrm{H}_{1} p<0.65$ |
|  | States model used (condone <br> 0.009 rather than 0.056 ) PI | A01.1b | M1 | Under null hypothesis, $X \sim \mathrm{~B}(7,0.65)$ |
|  | Using calculator, 0.056 or better | A01.1b | A1 | $\mathrm{P}(X \leq 2)=0.0556$ |
|  | Evaluates binomial model by comparing $\mathrm{P}(X \leq 2)$ with 0.05 PI | A03.5a | M1 | $0.0556>0.05$ |
|  | Infers $\mathrm{H}_{0}$ accepted PI | AO2.2b | A1 | Accept $\mathrm{H}_{0}$ |
|  | Concludes correctly in context. 'not sufficient evidence' or equivalent required | A03.2a | E1 | There is not sufficient evidence that the John's rate of illness has decreased |
| (b) | States one correct assumption(s) regarding validity of model | A03.5b | E1 | Assumption 1 <br> The probability of illness remains constant throughout one's life Validity <br> Not fully valid, as age has an impact on the immune system <br> OR <br> Assumption 2 <br> Annual results (of illness) are independent of one another Validity (Largely) valid. Trials are sufficiently far apart that an illness spanning two Christmases is unlikely. <br> OR <br> Assumption 3 <br> There are only two states, well and ill <br> Validity <br> Unclear. Grey area exists. eg does a mild sore throat count as ill? |
|  | States corresponding correct description(s) of likelihood of validity in context | AO2.4 | E1 |  |
|  | States second correct assumption(s) regarding validity of model | AO3.5b | E1 |  |
|  | States corresponding correct description(s) of likelihood of validity in context | AO2.4 | E1 |  |
|  | Max two assumptions with description of validity |  |  |  |
|  |  |  |  |  |
|  | Total |  | 10 |  |


| Q | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :--- | :---: | :---: | :--- |
| 13(a)(i) | Finds mean | AO1.1b | B1 | Mean $=\bar{X}=\frac{3046.14}{100}=30.46(14)$ |


| Q | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :---: | :---: | :---: | :---: |
| 14(a)(i) | States both hypotheses using correct language | AO2.5 | B1 | $\begin{aligned} & \mathrm{H}_{0}: \mu=123 \\ & \mathrm{H}_{1}: \mu \neq 123 \end{aligned}$ |
|  | Finds test statistic | A01.1a | M1 | $\text { Test statistic }=\frac{127-123}{\frac{70}{\sqrt{12144}}}$ |
|  | Obtains correct test statistic | A01.1b | A1 | $\begin{aligned} & =6.30 \\ & \text { Critical } z \text { values } \pm 1.96 \\ & 6.30>1.96 \end{aligned}$ |
|  | Infers $\mathrm{H}_{0}$ rejected by comparison of ts with cv | AO2.2b | A1 |  |
|  | Concludes correctly in context, including 'some evidence' | A03.2a | E1 | Reject $\mathrm{H}_{0}$ there is evidence (at the $5 \%$ level) to suggest the mean expenditure on bread had changed from 2012 to 2013 |
| ALT | States both hypotheses using correct language | AO2.5 | B1 | $\begin{aligned} & \mathrm{H}_{0}: \mu=123 \\ & \mathrm{H}_{0}: \mu \neq 123 \end{aligned}$ |
|  | Attempts to find $p$ value for z-test | A01.1a | M1 | $\begin{array}{\|l} \hline \text { From calculator, } \\ \mathrm{P}(X<127)=3.045 \times 10^{-10} \\ 3.045 \times 10^{-10}<0.025 \end{array}$ |
|  | Finds correct $p$ value | A01.1b | A1 |  |
|  | Infers $\mathrm{H}_{0}$ rejected by comparison of $p$ with 0.025 | AO2.2b | A1 |  |
|  | Concludes correctly in context, including 'some evidence' | AO3.2a | E1 | Reject $\mathrm{H}_{0}$ - there is evidence (at the $5 \%$ level) to suggest the mean expenditure on bread had changed from 2012 to 2013 |
| (a)(ii) | Uses Normal model to find critical values PI | AO3.4 | M1 | $\begin{aligned} & 123 \pm 1.96 \times \frac{70}{\sqrt{12144}} \\ & \min =121.75 \text { and } \max =124.25 \end{aligned}$ |
|  | Obtains correct critical values Correct accuracy required for this mark Disallow integer answers | A01.1b | A1 |  |
| (b)(i) | States valid reason for statement 1 'not supported' | AO2.4 | R1 | The conclusion implies that the mean changed, not that it increased by a specific amount, so the statement is not supported |
|  | Infers that model/test used would not imply the statement | AO2.2b | R1 |  |
| (b)(ii) | States valid reason for statement 2 'not supported' | AO2.4 | R1 | The conclusion implies that there is evidence that the mean has changed, but expenditure increase may be due to price changes, so statement is not supported |
|  | Infers that model/test used would not imply the statement | AO2.2b | R1 |  |
|  | Total |  | 11 |  |


| Q | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :---: | :---: | :---: | :---: |
| 15 | Uses conditional probability, either (1) or (2) | A03.1b | M1 | $\begin{equation*} \frac{\mathrm{P}(A \cap B)}{\mathrm{P}(A)}=\frac{1}{4} \tag{1} \end{equation*}$ $\Rightarrow \mathrm{P}(A)=4 \mathrm{P}(A \cap B)$ |
|  | Obtains both equations <br> (1) and (2) correctly | A01.1b | A1 | $\begin{aligned} & \frac{\mathrm{P}(A \cap B)}{\mathrm{P}(B)}=\frac{1}{10} \\ & \Rightarrow \mathrm{P}(B)=10 \mathrm{P}(A \cap B) \end{aligned}$ |
|  | Evaluates $\mathrm{P}(A \cup B)$ correctly PI | A01.1b | B1 | $\mathrm{P}(A \cup B)=1-\frac{122}{200}=\frac{39}{100}$ |
|  | Uses addition law | A01.1a | M1 | $\mathrm{P}(A)+\mathrm{P}(B)-\mathrm{P}(A \cap B)=\frac{39}{100}{ }^{(3)}$ |
|  | Combines the three equations | A01.1a | M1 | $4 \mathrm{P}(A \cap B)+10 \mathrm{P}(A \cap B)-\mathrm{P}(A \cap B)=\frac{39}{100}$ |
|  | Obtains correct probability, as a fraction or decimal | AO2.2b | A1 | $\mathrm{P}(A \cap B)=\frac{3}{100}$ |
| ALT | Produces a relevant Venn diagram | A03.1b | M1 | OR $200$ |
|  | Labels Venn diagram correctly | A01.1b | A1 |  |
|  | Forms correct equation to find $x$ PI | A01.1b | B1 | $9 x+x+3 x=200-122$ |
|  | Combines terms | A01.1a | M1 | $13 x=78$ |
|  | Solves equation | A01.1a | M1 | $x=6$ |
|  | Obtains correct probability | AO2.2b | A1 | $\mathrm{P}(A \cap B)=\frac{6}{200} \text { or } 0.03$ |
| Total |  |  | 6 |  |
|  | TOTAL |  | 100 |  |

