

Paper 4 (Calculator)

# Higher Tier 

Friday 12 November 2010 - Morning
Time: 1 hour 45 minutes
Materials required for examination
Ruler graduated in centimetres and millimetres, protractor, compasses,
pen, HB pencil, eraser, calculator.
Tracing paper may be used.

## Instructions to Candidates

In the boxes above, write your centre number, candidate number, your surname, initials and signature.
Check that you have the correct question paper.
Answer ALL the questions. Write your answers in the spaces provided in this question paper.
You must NOT write on the formulae page.
Anything you write on the formulae page will gain NO credit.
If you need more space to complete your answer to any question, use additional answer sheets.

## Information for Candidates

The marks for individual questions and the parts of questions are shown in round brackets: e.g. (2). There are 28 questions in this question paper. The total mark for this paper is 100 .
There are 28 pages in this question paper. Any blank pages are indicated.
Calculators may be used.
If your calculator does not have a $\pi$ button, take the value of $\pi$ to be 3.142 unless the question instructs otherwise.

Advice to Candidates
Show all stages in any calculations
Work steadily through the paper. Do not spend too long on one question.
If you cannot answer a question, leave it and attempt the next one.
Return at the end to those you have left out.
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## GCSE Mathematics (Linear) 1380

Formulae: Higher Tier
You must not write on this formulae page.
Anything you write on this formulae page will gain NO credit.

Volume of a prism $=$ area of cross section $\times$ length


Volume of sphere $=\frac{4}{3} \pi r^{3}$
Surface area of sphere $=4 \pi r^{2}$


In any triangle ABC


Sine Rule $\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}$
Cosine Rule $a^{2}=b^{2}+c^{2}-2 b c \cos A$

Area of triangle $=\frac{1}{2} a b \sin C$

3. There are 20 beads in box A.

4


$\qquad$ 6

8. The table shows some information about the ages, in years, of 60 people.

| Age (in years) | Frequency |
| :---: | :---: |
| 0 to 9 | 6 |
| 10 to 19 | 13 |
| 20 to 29 | 12 |
| 30 to 39 | 9 |
| 40 to 49 | 7 |
| 50 to 59 | 3 |
| 60 to 69 | 10 |

(a) Write down the modal class.
$\qquad$

Luke says
'The median lies in the class 30 to 39 '
Luke is wrong
(b) Explain why.
$\qquad$
$\qquad$
(1)

(c) On the grid, draw a frequency polygon for the information in the table.

| 9. Use your calculator to work out $\frac{13.7+5.86}{2.54 \times 3.17}$ <br> Write down all the figures on your calculator display. You must give your answer as a decimal. |  | Leave blank <br> Q9 |
| :---: | :---: | :---: |
|  | (Total 2 marks) |  |
| 10. $-3<k \leqslant 2$ <br> $k$ is an integer. <br> (a) Write down all the possible values of $k$. <br> (b) Solve the inequality $\frac{2 x}{3}<10$ | (2) <br> (2) <br> (Total 4 marks) | Q10 |
|  |  |  |


| 11. Here are four containers. |
| :--- |
| Water is poured into each container at a constant rate. |
| Here are four graphs. |
| The graphs show how the depth of the water in each container changes with time. |


| Depth of |
| :--- |
| water |

Match each graph with the correct container.
Depth of
water

10

| 12. A shop sells small boxes and large boxes for storing CDs. | Leave |
| :--- | :--- | :--- |
| A small box stores $x$ CDs. <br> A large box stores $y$ CDs. <br> Ethan buys 7 small boxes. <br> He also buys 5 large boxes. <br> Ethan can store a total of $T$ CDs in these boxes. <br> Write down a formula for $T$ in terms of $x$ and $y$. |  |

14. The diagram shows a solid prism made from centimetre cubes.

(a) On the centimetre square grid, draw the front elevation of the solid prism from the direction shown by the arrow.

(b) On the centimetre square grid below, draw the plan of the solid prism.

(2)
15. 200 students in Year 11 took a mathematics test.

Kamini wants to find out whether students in Year 11 like mathematics.

For her sample she asks the 20 students who got the highest marks in the test.
This is not a good sample to use.
(a) Write down one reason why.
$\qquad$
$\qquad$

She uses this question on her questionnaire.

(b) Write down one thing that is wrong with this question.
$\qquad$
$\qquad$

Kamini also wants to find out how many hours students spend on their mathematics homework.
(c) Design a suitable question that Kamini could use on her questionnaire. You must include some response boxes.


19. There are 100 teachers at Maria's school.

Maria found out the age of each teacher.
The table gives information about her results.

| Age ( $\boldsymbol{A}$ years) | Frequency |
| :---: | :---: |
| $20<A \leqslant 30$ | 26 |
| $30<A \leqslant 40$ | 35 |
| $40<A \leqslant 50$ | 21 |
| $50<A \leqslant 60$ | 12 |
| $60<A \leqslant 70$ | 6 |

(a) Complete the cumulative frequency table.

| Age ( $A$ years) | Cumulative Frequency |
| :---: | :---: |
| $20<A \leqslant 30$ | 26 |
| $20<A \leqslant 40$ |  |
| $20<A \leqslant 50$ |  |
| $20<A \leqslant 60$ |  |
| $20<A \leqslant 70$ |  |

(b) On the grid opposite, draw a cumulative frequency graph for your table.
(c) Use your graph to find an estimate for the median age.
$\qquad$
(d) Use your graph to find an estimate for the number of these teachers who are older than 56 years old.
$\qquad$



[^0]22. (a) Complete the table of values for $y=x^{3}-7$

| $x$ | -2 | -1 | 0 | 1 | 2 | 3 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ |  | -8 |  |  |  | 20 |

(b) On the grid, draw the graph of $y=x^{3}-7$ for values of $x$ from -2 to 3


| (Total 4 marks) |  |
| :---: | :---: |
|  |  |


25. (a) Expand and simplify $(2 x+4 y)(4 x-5 y)$
(2)
(b) Simplify fully $\frac{(x+10)^{5}}{(x+10)^{4}}$
(1)
(c) Simplify fully $\frac{x^{2}-25}{x^{2}+7 x+10}$
For all values of $x, \quad x^{2}+6 x-2=(x+p)^{2}+q$
(d) Find the value of $p$ and the value of $q$.

$$
p=.
$$

(2)

| (Total 8 marks) |  |
| :---: | :---: |
|  |  |


27. The graph of $y=\mathrm{f}(x)$ is shown on the grids.
(a) On this grid, sketch the graph of $y=\mathrm{f}(x-3)$

(2)
(b) On this grid, sketch the graph of $y=-\mathrm{f}(x)$


|  | (Total 4 marks) |
| :--- | :--- |
|  |  |

28. 

[^0]:    18

