

3.

$$f(x) = (3x - 2)(x - k) - 8$$

where k is a constant.

(a) Write down the value of $f(k)$.

(1)

When $f(x)$ is divided by $(x - 2)$ the remainder is 4

(b) Find the value of k .

(2)

(c) Factorise $f(x)$ completely.

(3)



4. (a) Complete the table below, giving values of $\sqrt{2^x + 1}$ to 3 decimal places.

x	0	0.5	1	1.5	2	2.5	3
$\sqrt{2^x + 1}$	1.414	1.554	1.732	1.957			3

(2)

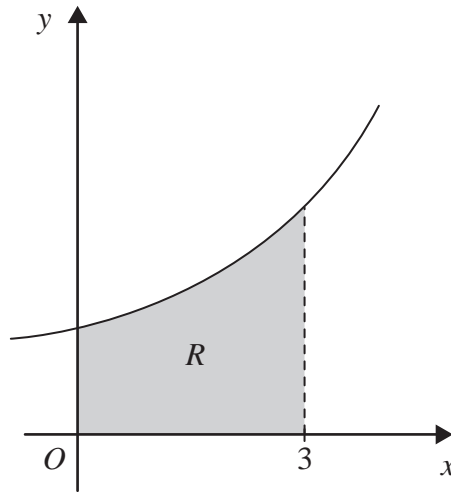


Figure 1

Figure 1 shows the region R which is bounded by the curve with equation $y = \sqrt{2^x + 1}$, the x -axis and the lines $x = 0$ and $x = 3$

(b) Use the trapezium rule, with all the values from your table, to find an approximation for the area of R .

(4)

(c) By reference to the curve in Figure 1 state, giving a reason, whether your approximation in part (b) is an overestimate or an underestimate for the area of R .

(2)

- 5.** The third term of a geometric sequence is 324 and the sixth term is 96
- (a) Show that the common ratio of the sequence is $\frac{2}{3}$ (2)
 - (b) Find the first term of the sequence. (2)
 - (c) Find the sum of the first 15 terms of the sequence. (3)
 - (d) Find the sum to infinity of the sequence. (2)



9.

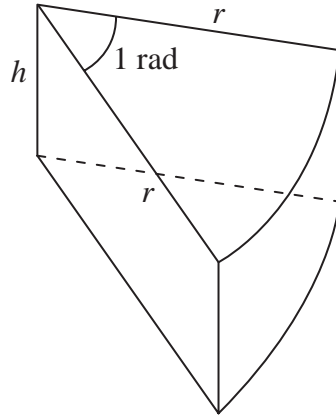


Figure 2

Figure 2 shows a closed box used by a shop for packing pieces of cake. The box is a right prism of height h cm. The cross section is a sector of a circle. The sector has radius r cm and angle 1 radian.

The volume of the box is 300 cm^3 .

(a) Show that the surface area of the box, $S \text{ cm}^2$, is given by

$$S = r^2 + \frac{1800}{r} \tag{5}$$

(b) Use calculus to find the value of r for which S is stationary. (4)

(c) Prove that this value of r gives a minimum value of S . (2)

(d) Find, to the nearest cm^2 , this minimum value of S . (2)



