

ADVANCED SUBSIDIARY GCE
MATHEMATICS
Core Mathematics 1

4721

Candidates answer on the Answer Booklet

OCR Supplied Materials:

- 8 page Answer Booklet
- List of Formulae (MF1)

Other Materials Required:

None

Friday 9 January 2009
Morning

Duration: 1 hour 30 minutes



INSTRUCTIONS TO CANDIDATES

- Write your name clearly in capital letters, your Centre Number and Candidate Number in the spaces provided on the Answer Booklet.
- Use black ink. Pencil may be used for graphs and diagrams only.
- Read each question carefully and make sure that you know what you have to do before starting your answer.
- Answer **all** the questions.
- Do **not** write in the bar codes.
- Give non-exact numerical answers correct to 3 significant figures unless a different degree of accuracy is specified in the question or is clearly appropriate.
- **You are not permitted to use a calculator in this paper.**

INFORMATION FOR CANDIDATES

- The number of marks is given in brackets [] at the end of each question or part question.
- **You are reminded of the need for clear presentation in your answers.**
- The total number of marks for this paper is **72**.
- This document consists of **4** pages. Any blank pages are indicated.



**No calculator can
be used for this
paper**

- 1 Express $\sqrt{45} + \frac{20}{\sqrt{5}}$ in the form $k\sqrt{5}$, where k is an integer. [3]
- 2 Simplify
- (i) $(\sqrt[3]{x})^6$, [1]
- (ii) $\frac{3y^4 \times (10y)^3}{2y^5}$. [3]
- 3 Solve the equation $3x^{\frac{2}{3}} + x^{\frac{1}{3}} - 2 = 0$. [5]
- 4 (i) Sketch the curve $y = \frac{1}{x^2}$. [2]
- (ii) The curve $y = \frac{1}{x^2}$ is translated by 3 units in the negative x -direction. State the equation of the curve after it has been translated. [2]
- (iii) The curve $y = \frac{1}{x^2}$ is stretched parallel to the y -axis with scale factor 4 and, as a result, the point $P(1, 1)$ is transformed to the point Q . State the coordinates of Q . [2]
- 5 Find $\frac{dy}{dx}$ in each of the following cases:
- (i) $y = 10x^{-5}$, [2]
- (ii) $y = \sqrt[4]{x}$, [3]
- (iii) $y = x(x+3)(1-5x)$. [4]
- 6 (i) Express $5x^2 + 20x - 8$ in the form $p(x+q)^2 + r$. [4]
- (ii) State the equation of the line of symmetry of the curve $y = 5x^2 + 20x - 8$. [1]
- (iii) Calculate the discriminant of $5x^2 + 20x - 8$. [2]
- (iv) State the number of real roots of the equation $5x^2 + 20x - 8 = 0$. [1]

- 7 The line with equation $3x + 4y - 10 = 0$ passes through point $A(2, 1)$ and point $B(10, k)$.
- (i) Find the value of k . [2]
 - (ii) Calculate the length of AB . [2]
- A circle has equation $(x - 6)^2 + (y + 2)^2 = 25$.
- (iii) Write down the coordinates of the centre and the radius of the circle. [2]
 - (iv) Verify that AB is a diameter of the circle. [2]
- 8
- (i) Solve the equation $5 - 8x - x^2 = 0$, giving your answers in simplified surd form. [3]
 - (ii) Solve the inequality $5 - 8x - x^2 \leq 0$. [2]
 - (iii) Sketch the curve $y = (5 - 8x - x^2)(x + 4)$, giving the coordinates of the points where the curve crosses the coordinate axes. [5]
- 9 The curve $y = x^3 + px^2 + 2$ has a stationary point when $x = 4$. Find the value of the constant p and determine whether the stationary point is a maximum or minimum point. [7]
- 10 A curve has equation $y = x^2 + x$.
- (i) Find the gradient of the curve at the point for which $x = 2$. [2]
 - (ii) Find the equation of the normal to the curve at the point for which $x = 2$, giving your answer in the form $ax + by + c = 0$, where a , b and c are integers. [4]
 - (iii) Find the values of k for which the line $y = kx - 4$ is a tangent to the curve. [6]



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