| Q 1 |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| (a) <br> (i) | Impulse has magnitude $2 \times 9=18 \mathrm{~N} \mathrm{~s}$ speed is $\frac{18}{6}=3 \mathrm{~m} \mathrm{~s}^{-1}$. | $\begin{aligned} & \text { B1 } \\ & \text { B1 } \end{aligned}$ |  | 2 |
| (ii) | $\begin{aligned} & \text { PCLM } \rightarrow \\ & 3 \times 6-1 \times 2=8 v \\ & v=2 \text { so } 2 \mathrm{~m} \mathrm{~s}^{-1} \text { in orig direction of } \mathrm{A} \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { E1 } \end{aligned}$ | Use of PCLM + combined mass RHS <br> All correct <br> Must justify direction (diag etc) | 3 |
| (iii) | $\rightarrow 2 \times 2-2 \times-1=6 \mathrm{Ns}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \end{aligned}$ | Attempted use of $m \mathbf{v}$ - mu for 6 N s dir specified (accept diag) | 2 |
| (iv) <br> (A) |  | B1 | Accept masses not shown | 1 |
| (B) | $\begin{aligned} & \text { PCLM } \rightarrow \\ & 2 \times 8+10 \times 1.8=8 v+10 \times 1.9 \\ & v=1.875 \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { A1 } \end{aligned}$ | PCLM. All terms present Allow sign errors only | 3 |
| (C) | $\begin{aligned} & \text { NEL } \frac{1.9-1.875}{1.8-2}=-e \\ & \text { so } e=0.125 \end{aligned}$ | M1 <br> A1 <br> F1 | Use of NEL with their $v$ <br> Any form. FT their $v$ <br> FT their $v$ (only for $0<e \leq 1$ ) | 3 |
| (b) | Using $v^{2}=u^{2}+2 a s$ $v=\sqrt{2 \times 10 \times 9.8}=14$ <br> rebounds at $14 \times \frac{4}{7}$ $=8 \mathrm{~m} \mathrm{~s}^{-1}$ <br> No change to the horizontal component Since both horiz and vert components are $8 \mathrm{~m} \mathrm{~s}^{-1}$ the angle is $45^{\circ}$ | B1 <br> M1 <br> F1 <br> B1 <br> A1 | Allow $\pm 14$ <br> Using their vertical component <br> FT from their 14. Allow $\pm$ <br> Need not be explicitly stated <br> cao | 5 |
|  |  | 19 |  |  |


| Q2 |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| (i) | $\theta=\frac{\pi}{2}$ <br> gives CG $=\frac{8 \sin \frac{\pi}{2}}{\frac{\pi}{2}}=\frac{16}{\pi}$ $\left(-\frac{16}{\pi}, 8\right)$ justified | B1 <br> E1 <br> E1 |  |  |
| (ii) | $(8 \pi+72)\binom{\bar{x}}{\bar{y}}=8 \pi\binom{-\frac{16}{\pi}}{8}+72\binom{36}{0}$ $\binom{\bar{x}}{\bar{y}}=\binom{25.3673 . . .}{2.06997 . . .}=\binom{25.37}{2.07} \text { (4 s. f.) }$ | $\begin{aligned} & \text { M1 } \\ & \text { B1 } \\ & \text { A1 } \\ & \text { A1 } \\ & \text { E1 } \\ & \text { E1 } \end{aligned}$ | Method for c.m. <br> Correct mass of 8 . or equivalent <br> $1^{\text {st }}$ RHS term correct <br> $2^{\text {nd }}$ RHS term correct <br> [If separate cpts award the A1s for $x$ - and $y$ - cpts correct on RHS] | 6 |
| (iii) | $\tan \alpha=\frac{13.93}{25.37}$ $\alpha=28.7700 \ldots \text { so } 28.8^{\circ} \text { (3 s. f.) }$ | B1 <br> M1 <br> M1 <br> A1 <br> A1 | General position and angle (lengths need not be shown) <br> Angle or complement attempted. arctan or equivalent. <br> Attempt to get 16 - 2.0699... <br> Obtaining 13.93... cao <br> Accept use of 2.0699... but not 16 . <br> cao | 5 |
| (iv) | c. w. moments about A $12 \times 13.93-16 F=0$ so $F=10.4475$.. | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { A1 } \end{aligned}$ | [FT use of 2.0699...] <br> Moments about any point, all forces present <br> (1.5525... if 2.0699... used) | 3 |
|  |  | 17 |  |  |


| Q 3 |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| (i) | Moments c.w. about B $\begin{aligned} & 200 \times 0.6-0.8 R_{\mathrm{A}}=0 \\ & R_{\mathrm{A}}=150 \text { so } 150 \mathrm{~N} \end{aligned}$ <br> Resolve or moments $R_{\mathrm{B}}=50 \text { so } 50 \mathrm{~N}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { M1 } \\ & \text { F1 } \end{aligned}$ | Accept about any point. Allow sign errors. | 4 |
| (ii) | Moments c.w. about D $\begin{aligned} & -0.8 R_{\mathrm{C}}+1.2 \times 200=0 \\ & R_{\mathrm{C}}=300 \uparrow \end{aligned}$ <br> Resolve or moments $R_{\mathrm{D}}=100 \downarrow$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { M1 } \\ & \text { A1 } \\ & \text { E1 } \end{aligned}$ | Or equiv. Accept about any point. All terms present. No extra terms. Allow sign errors. <br> Neglect direction <br> Or equiv. All terms present. No extra terms. <br> Allow sign errors. <br> Neglect direction <br> Both directions clearly shown (on diag) | 5 |
| (iii) | Moments c.w. about P $0.4 \times 200 \cos \alpha-0.8 R_{\mathrm{Q}}=0$ $R_{\mathrm{Q}}=96 \text { so } 96 \mathrm{~N}$ <br> resolve perp to plank $R_{\mathrm{P}}=200 \cos \alpha+R_{\mathrm{Q}}$ $R_{\mathrm{P}}=288 \text { so } 288 \mathrm{~N}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { A1 } \\ & \text { M1 } \\ & \text { A1 } \\ & \text { A1 } \end{aligned}$ | Or equiv. Must have some resolution. All terms present. No extra terms. Allow sign errors. Correct <br> [No direction required but no sign errors in working] <br> Or equiv. Must have some resolution. All terms present. No extra terms. Allow sign errors. Correct <br> [No direction required but no sign errors in working] | 6 |
| (iv) | Need one with greatest normal reaction So at P <br> Resolve parallel to the plank $\begin{aligned} & F=200 \sin \alpha \\ & \text { so } F=56 \end{aligned}$ $\begin{aligned} & \mu=\frac{F}{R} \\ & \left.=\frac{56}{288}=\frac{7}{36}(=0.194 \text { (3 s. f. })\right) \end{aligned}$ | B1 <br> B1 <br> M1 <br> A1 | FT their reactions <br> Must use their $F$ and $R$ <br> cao | 4 |
|  |  | 19 |  |  |


| Q 4 |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| (i) | either $\begin{aligned} & 0.5 \times 20 \times 0.5^{2}+20 \times 9.8 \times 4 \\ & =786.5 \mathrm{~J} \end{aligned}$ <br> or $\begin{aligned} & a=1 / 32 \\ & T-20 g=20 \times 1 / 32 \\ & T=196.625 \end{aligned}$ <br> WD is $4 T=786.5$ so 786.5 J | M1 <br> B1 <br> B1 <br> A1 <br> B1 <br> M1 <br> A1 <br> A1 | KE or GPE terms <br> KE term <br> GPE term <br> cao <br> N2L. All terms present. <br> cao | 4 |
| (ii) | $20 \mathrm{~g} \times 0.5=10 \mathrm{~g}$ so 98 W | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { A1 } \end{aligned}$ | Use of $P=F v$ or $\Delta \mathrm{WD} / \Delta t$ All correct | 3 |
| (iii) | GPE lost is $35 \times 9.8 \times 3=1029 \mathrm{~J}$ <br> KE gained is $0.5 \times 35 \times\left(3^{2}-1^{2}\right)=140 \mathrm{~J}$ <br> so WE gives WD against friction is $1029-140=889 \mathrm{~J}$ | $\begin{aligned} & \text { B1 } \\ & \text { M1 } \\ & \text { A1 } \\ & \text { M1 } \\ & \text { A1 } \end{aligned}$ | $\Delta \mathrm{KE}$ <br> The 140 J need not be evaluated Use of WE equation cao | 5 |
| (iv) | $\begin{aligned} & \text { either } \\ & 0.5 \times 35 \times 3^{2}+35 \times 9.8 \times 0.1 x=150 x \\ & \begin{array}{l} x=1.36127 \ldots \text { so } 1.36 \mathrm{~m}(3 \mathrm{~S} . \text { F. }) \\ \text { or } \\ 35 g \times 0.1-150=35 a \\ a=-3.3057 \ldots \\ 0=9-2 a x \\ x=1.36127 \ldots \text { so } 1.36 \mathrm{~m} \mathrm{( } \text { ( S. F. }) \end{array} \end{aligned}$ | M1 B1 B1 A1 A1 M1 A1 A1 M1 A1 | WE equation. Allow 1 missing term. No extra terms. <br> One term correct (neglect sign) <br> Another term correct (neglect sign) <br> All correct except allow sign errors <br> cao <br> Use of N2L. Must have attempt at weight component. No extra terms. <br> Allow sign errors, otherwise correct <br> cao <br> Use of appropriate uvast or sequence cao | 5 |
|  |  | 17 |  |  |

