

Centre Number						Candidate Number				
Surname										
Other Names										
Candidate Signature										

For Examiner's Use	
Examiner's Initials	
Pages	Mark
3	
4 – 5	
6 – 7	
8 – 9	
10 – 11	
12 – 13	
14 – 15	
16 – 17	
18 – 19	
20	
TOTAL	



General Certificate of Secondary Education
Higher Tier
November 2013

Mathematics

43603H

Unit 3

Monday 11 November 2013 9.00 am to 10.30 am

H

<p>For this paper you must have:</p> <ul style="list-style-type: none"> • a calculator • mathematical instruments. 	
---	--

Time allowed

- 1 hour 30 minutes

Instructions

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- Do all rough work in this book.
- If your calculator does not have a π button, take the value of π to be 3.14 unless another value is given in the question.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.
- The quality of your written communication is specifically assessed in Questions 4, 7 and 9. These questions are indicated with an asterisk (*).
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to this answer booklet.

Advice

- In all calculations, show clearly how you work out your answer.



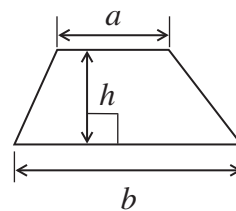
N 0 V 1 3 4 3 6 0 3 H 0 1

WMP/Nov13/43603H/E4

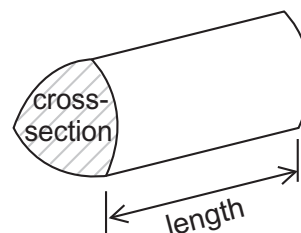
43603H

Formulae Sheet: Higher Tier

$$\text{Area of trapezium} = \frac{1}{2}(a+b)h$$

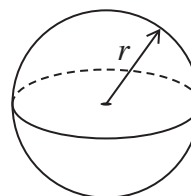


$$\text{Volume of prism} = \text{area of cross-section} \times \text{length}$$



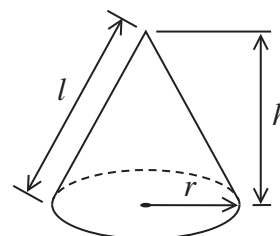
$$\text{Volume of sphere} = \frac{4}{3}\pi r^3$$

$$\text{Surface area of sphere} = 4\pi r^2$$



$$\text{Volume of cone} = \frac{1}{3}\pi r^2 h$$

$$\text{Curved surface area of cone} = \pi r l$$

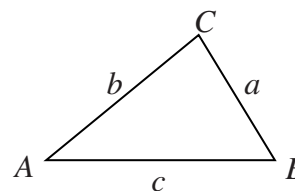


In any triangle ABC

$$\text{Area of triangle} = \frac{1}{2}ab \sin C$$

$$\text{Sine rule} \quad \frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$\text{Cosine rule} \quad a^2 = b^2 + c^2 - 2bc \cos A$$



The Quadratic Equation

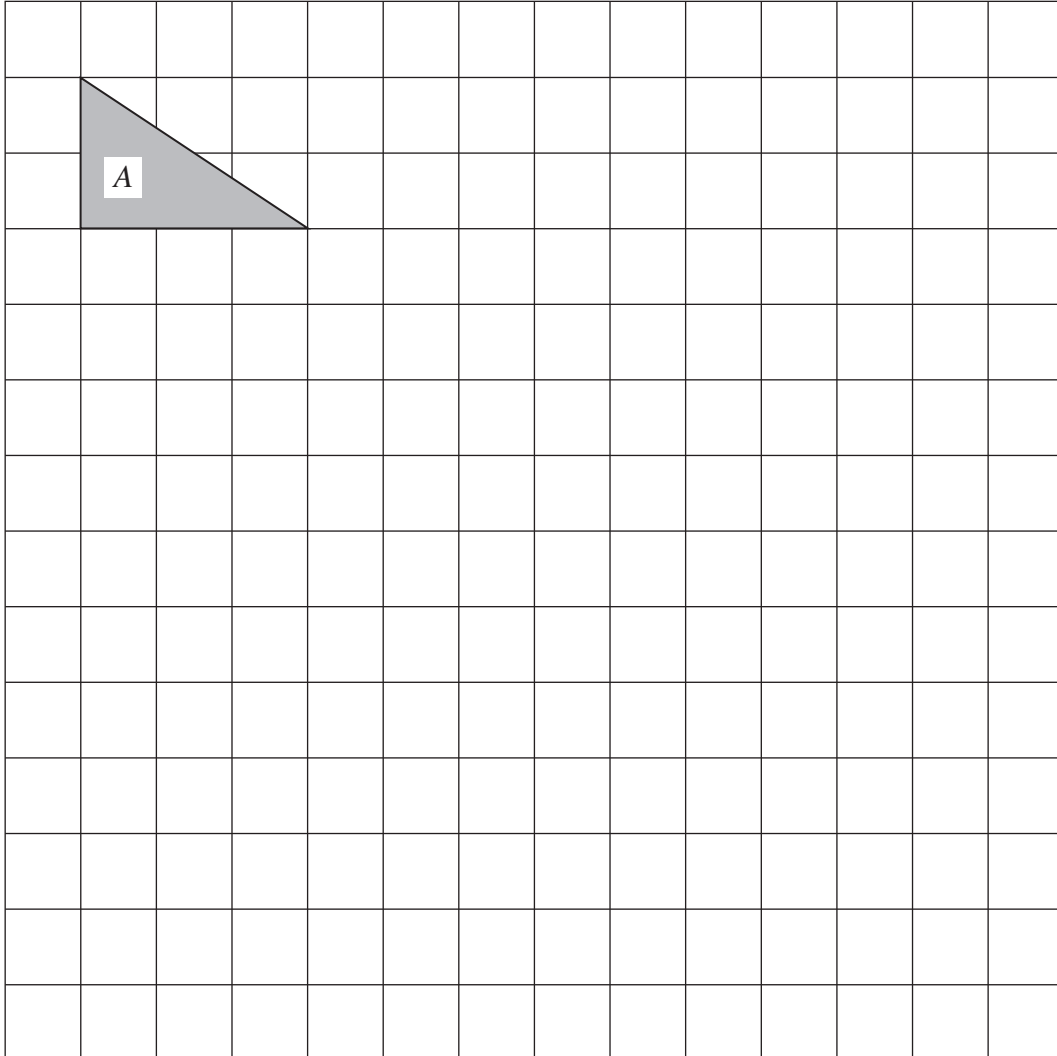
The solutions of $ax^2 + bx + c = 0$, where $a \neq 0$, are given by

$$x = \frac{-b \pm \sqrt{(b^2 - 4ac)}}{2a}$$



Answer **all** questions in the spaces provided.

1 Shape *A* on the centimetre grid is enlarged by scale factor 3.



Work out the area of the enlargement.

.....

.....

.....

.....

Answer cm² (3 marks)

3

Turn over ►

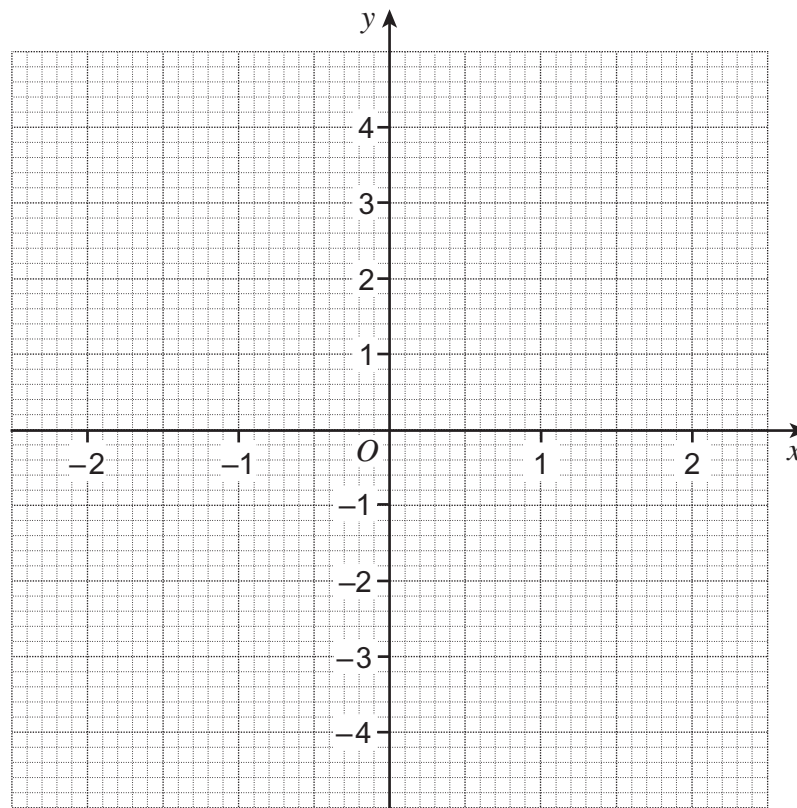


2 (a) Complete the table of values for $y = x^2$

x	-2	-1	0	1	2
y	4			1	

(2 marks)

2 (b) On the grid, draw the graph of $y = x^2$ for values of x from -2 to 2.



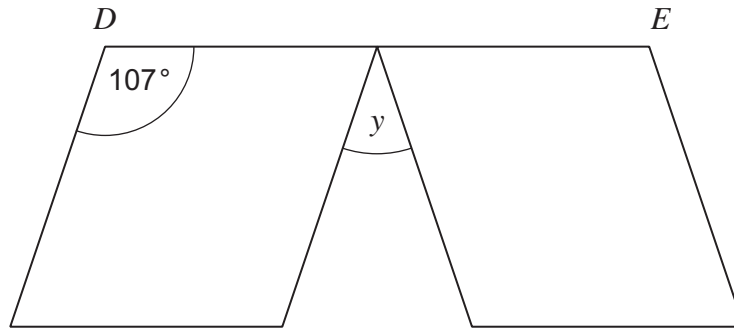
(2 marks)

2 (c) On the same grid, draw the graph of $y = x^2 - 3$ for values of x from -2 to 2.

(2 marks)



3 A rhombus is reflected as shown.
DE is a straight line.



Not drawn
accurately

Work out the size of angle *y*.
Show your working, which may be on the diagram.

.....

.....

.....

.....

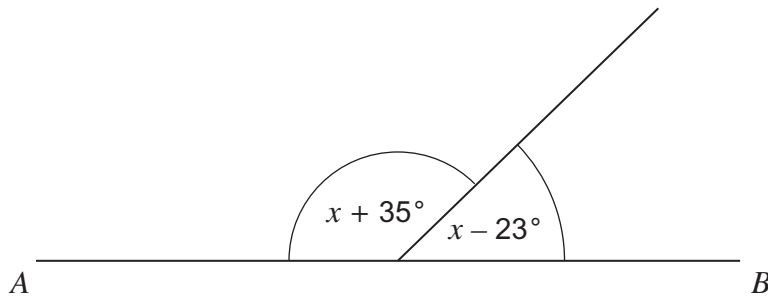
.....

.....

Answer degrees (3 marks)

Turn over for the next question



***4** AB is a straight line.Not drawn
accurately

Set up and solve an equation to work out the size of the obtuse angle.

.....

.....

.....

.....

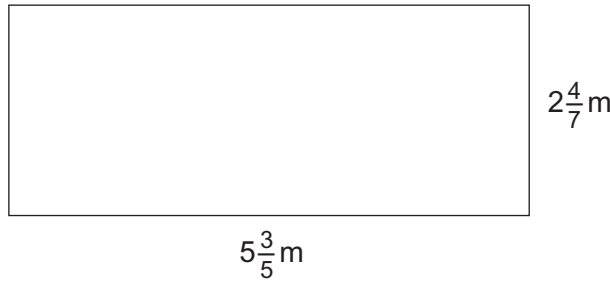
.....

.....

Answer degrees (4 marks)



5 Use a calculator to work out the perimeter of the rectangle.



Not drawn accurately

Give your answer as a mixed fraction.

.....

.....

.....

Answer m (2 marks)

6 The scale on a map is 1 : 500 000

Two towns are 8 cm apart on the map.

Work out the actual distance between the towns.
Give your answer in kilometres.

.....

.....

.....

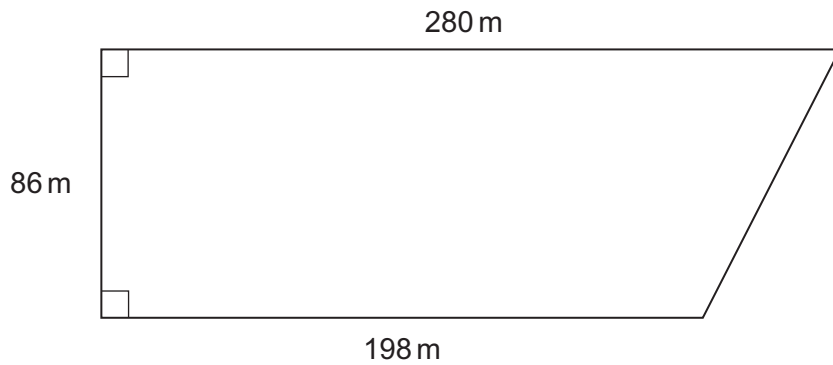
.....

Answer km (3 marks)



7 The diagram shows a field.

Not drawn accurately



7 (a) Work out the area of the field.

.....

.....

.....

Answer m² (2 marks)

*7 (b) 1 acre = 4047 square metres

A farmer keeps cows in the field.
He is allowed 7 cows per acre.

Work out the maximum number of cows he is allowed to put in the field.

.....

.....

.....

.....

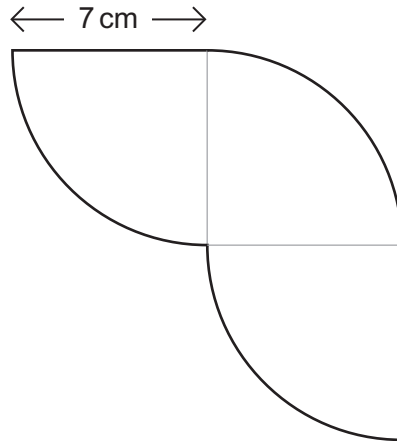
.....

.....

Answer (4 marks)



8 This shape is made from identical quarter circles.



Not drawn
accurately

Work out the perimeter of the shape.

.....

.....

.....

.....

.....

.....

Answer cm (4 marks)

Turn over for the next question



***9** Use trial and improvement to find a solution to the equation

$$x^3 + x = 25$$

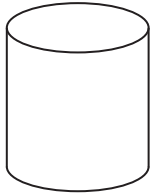
The first step is shown in the table.
Give your solution to 1 decimal place.

x	$x^3 + x$	Comment
2	10	Too small

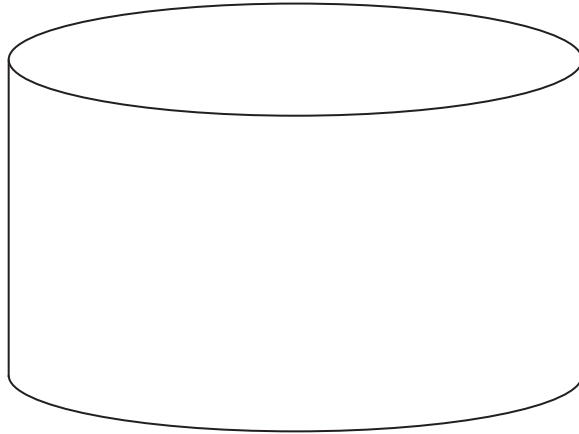
$x = \dots\dots\dots$ (4 marks)



10 The diagram shows two cylinders.



radius 4 cm
height 9 cm



radius 10 cm
height 36 cm

How many times bigger is the volume of the large cylinder than the small cylinder?
You **must** show your working.

.....

.....

.....

.....

.....

.....

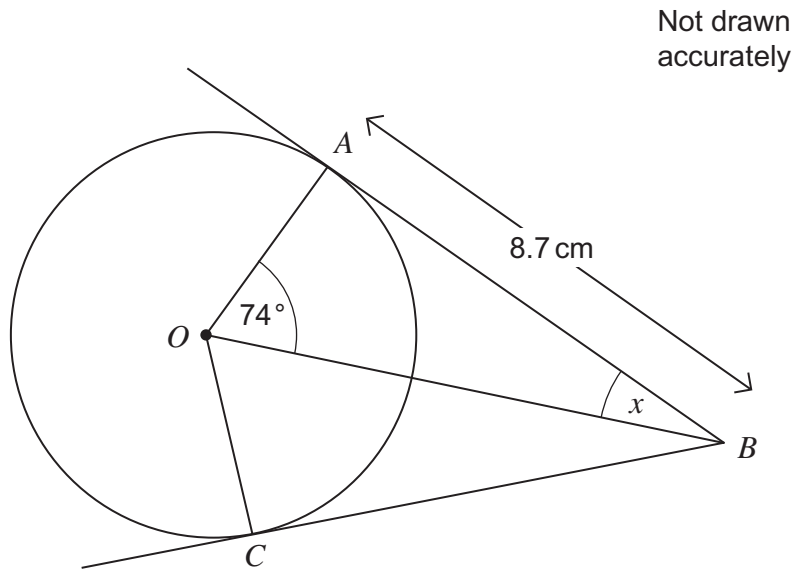
Answer (4 marks)

8

Turn over ►



11 The diagram shows a circle centre O .
 A and C are points on the circumference.
 AB and CB are tangents.



11 (a) Work out the size of angle x .

.....

Answer degrees (2 marks)

11 (b) Write down the length of BC .
 Give a reason for your answer.

Answer cm

Reason

(1 mark)



11 (c) Work out the radius of the circle.

.....

.....

.....

.....

.....

.....

Answer cm (3 marks)

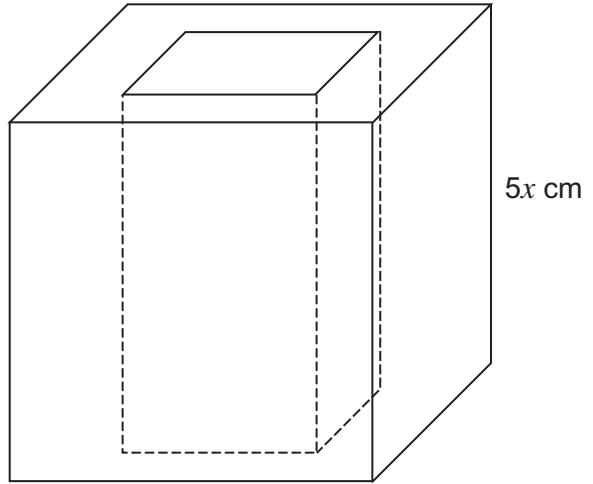
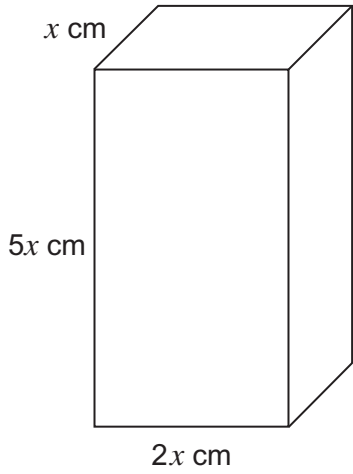
Turn over for the next question

6

Turn over ►



12 The cuboid has been cut out of the wooden cube as shown.



12 (a) Show clearly why the volume of wood remaining, in cubic centimetres, is $115x^3$.

.....

.....

.....

.....

(3 marks)

12 (b) You are given that $x = 3.5$
Work out the volume of wood remaining.

.....

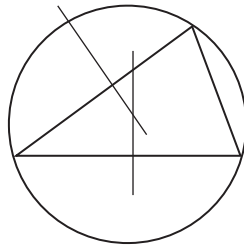
.....

Answer cm^3 (2 marks)



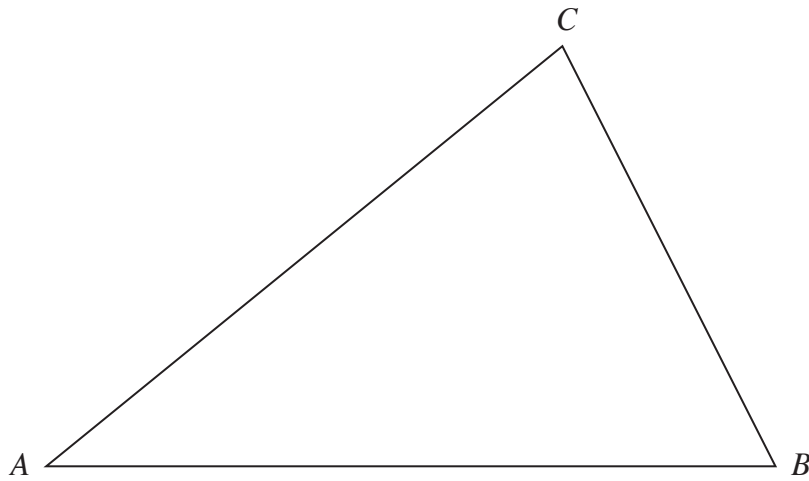
13

Use these steps to construct a circle passing through the vertices of the triangle ABC .



- Construct the perpendicular bisector of AB .
- Construct the perpendicular bisector of AC .
- Use the point of intersection of the bisectors as the centre of the circle.
- Draw the circle through A , B and C .

Show your construction arcs clearly.



(4 marks)

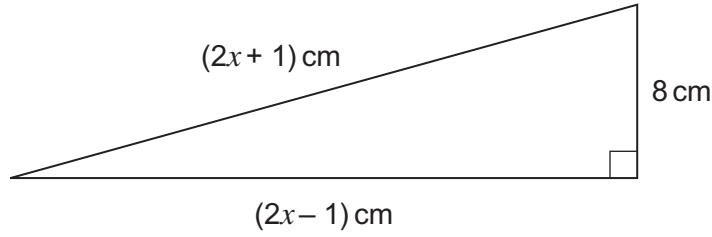
9

Turn over ►



14 Work out the value of x .

Not drawn
accurately



You **must** show your working.

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

$x =$ (5 marks)



15 y is **inversely** proportional to x .

When $y = 5$, $x = 9$

15 (a) Work out an equation connecting y and x .

.....
.....
.....

Answer (3 marks)

15 (b) Work out the value of y when $x = 15$

.....
.....
.....

Answer (2 marks)

Turn over for the next question



16 Three items were bought at a car boot sale.

Item A
Mass = 9.5 grams
Volume = 2 cm³

Item B
Mass = 57 grams
Volume = 3 cm³

Item C
Mass = 76 grams
Volume = 4 cm³

The density of gold is **approximately** 19 grams per cm³.

Which item or items **cannot** be gold?
You **must** show your working.

.....

.....

.....

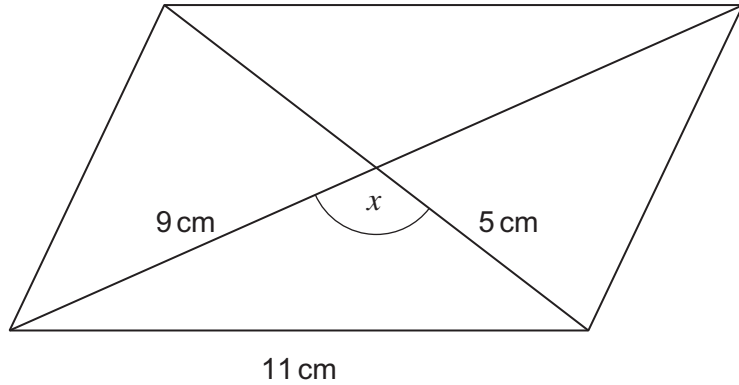
.....

.....

Answer (4 marks)



17 The diagram shows a parallelogram.



Not drawn
accurately

17 (a) Work out the size of angle x .

.....

.....

.....

.....

.....

.....

Answer degrees (3 marks)

17 (b) Work out the area of the parallelogram.

.....

.....

.....

.....

Answer cm² (3 marks)

Turn over for the next question

Turn over ►



18

A car and a lorry complete the same 240 mile journey without stopping.

The average speed of the car is x mph.

The average speed of the lorry is 12 mph slower than the car.

The lorry takes 1 hour longer than the car.

Use an algebraic method to work out the average speed of the car.

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

Answer mph (6 marks)

END OF QUESTIONS

6

