



GCSE Mathematics

Paper 2 Foundation Tier

Mark scheme

8300
November 2017

Version: 1.0 Final

Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts. Alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Assessment Writer.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Further copies of this mark scheme are available from aqa.org.uk

Glossary for Mark Schemes

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

If a student uses a method which is not explicitly covered by the mark scheme the same principles of marking should be applied. Credit should be given to any valid methods. Examiners should seek advice from their senior examiner if in any doubt.

| | |
|------------------------|--|
| M | Method marks are awarded for a correct method which could lead to a correct answer. |
| A | Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied. |
| B | Marks awarded independent of method. |
| ft | Follow through marks. Marks awarded for correct working following a mistake in an earlier step. |
| SC | Special case. Marks awarded for a common misinterpretation which has some mathematical worth. |
| M dep | A method mark dependent on a previous method mark being awarded. |
| B dep | A mark that can only be awarded if a previous independent mark has been awarded. |
| oe | Or equivalent. Accept answers that are equivalent. eg accept 0.5 as well as $\frac{1}{2}$ |
| [a, b] | Accept values between a and b inclusive. |
| [a, b) | Accept values $a \leq \text{value} < b$ |
| 3.14 ... | Accept answers which begin 3.14 eg 3.14, 3.142, 3.1416 |
| Use of brackets | It is not necessary to see the bracketed work to award the marks. |

Examiners should consistently apply the following principles

Diagrams

Diagrams that have working on them should be treated like normal responses. If a diagram has been written on but the correct response is within the answer space, the work within the answer space should be marked. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working, and is not, therefore, penalised.

Responses which appear to come from incorrect methods

Whenever there is doubt as to whether a student has used an incorrect method to obtain an answer, as a general principle, the benefit of doubt must be given to the student. In cases where there is no doubt that the answer has come from incorrect working then the student should be penalised.

Questions which ask students to show working

Instructions on marking will be given but usually marks are not awarded to students who show no working.

Questions which do not ask students to show working

As a general principle, a correct response is awarded full marks.

Misread or miscopy

Students often copy values from a question incorrectly. If the examiner thinks that the student has made a genuine misread, then only the accuracy marks (A or B marks), up to a maximum of 2 marks are penalised. The method marks can still be awarded.

Further work

Once the correct answer has been seen, further working may be ignored unless it goes on to contradict the correct answer.

Choice

When a choice of answers and/or methods is given, mark each attempt. If both methods are valid then M marks can be awarded but any incorrect answer or method would result in marks being lost.

Work not replaced

Erased or crossed out work that is still legible should be marked.

Work replaced

Erased or crossed out work that has been replaced is not awarded marks.

Premature approximation

Rounding off too early can lead to inaccuracy in the final answer. This should be penalised by 1 mark unless instructed otherwise.

Continental notation

Accept a comma used instead of a decimal point (for example, in measurements or currency), provided that it is clear to the examiner that the student intended it to be a decimal point.

| Question | Answer | Mark | Comments |
|----------|--|------|------------------|
| 1 | 135 | B1 | |
| 2 | 2 | B1 | |
| 3 | $\frac{3}{100}$ | B1 | |
| 4 | $A = 2B$ | B1 | |
| 5a | y^2 | B1 | |
| 5b | $4a + 11$ | B2 | B1 for each term |
| | Additional Guidance | | |
| | 4a or 11 or $4a + 11$ seen and answer eg 15a | | B1 |
| | 4a + 11 seen and then 'solves' | | B1 |
| | 11 and -11 seen (without 4a seen) | | B0 |

| Question | Answer | Mark | Comments | |
|---|---|------|--|--|
| 6 | Linear scale starting at 0 and increasing in 1s on vertical axis Vertical axis labelled frequency or f or number Title given or horizontal axis labelled (types of) bird(s) Bars labelled with four bird names (allow R, S, W, L) Four bars with equal widths Equal gaps or no gaps between four bars All heights correct | B3 | Bar chart could be horizontal B3 for all criteria met B2 for 5 or 6 criteria met B1 for 3 or 4 criteria met correct or ft their increasing scale | |
| | Additional Guidance | | | |
| | Mark intention throughout | | | |
| | If grid is blank, allow axes to be transposed | | | |
| | If axes and labels do not match the orientation of the bar chart then only the marks for criteria 3 (must be a title), 5, 6 and 7 may be awarded | | B1 max | |
| | All values not needed for axis scale eg 0 can be implied but spacing must be linear | | | |
| | Scale of 2 units per square does not meet the first criterion | | | |
| | Allow words after 'Number' on axis label eg 'Number seen', 'Number of birds'. Also allow eg Amount of birds | | | |
| | Title must include the word bird | | | |
| | Condone different gap between the vertical axis and the first bar with other gaps equal or no other gaps | | | |
| If no axis scale, bars with heights 2, 5, 3, 1 meet heights criterion | | | | |
| Points only or vertical lines can score the marks for criteria 1, 2, 3, 4 and 7 | B2 max | | | |

| Question | Answer | Mark | Comments | |
|---|---|-------|---|---|
| 7 | Alternative method 1 | | | |
| | $\pounds 2 + \pounds 1 + 50\text{p} + 20\text{p} + 20\text{p} + 5\text{p} + 2\text{p}$ or $(\pounds)3.97$ or $\pounds 1 + 50\text{p} + 2\text{p} + 1\text{p}$ or $(\pounds)1.53$ or $\pounds 2 + \pounds 1 + 50\text{p} + 20\text{p} + 20\text{p} + 5\text{p} + 2\text{p} + \pounds 1 + 50\text{p} + 2\text{p} + 1\text{p}$ or $(\pounds)5.5(0)$ or $\pounds 2 + \pounds 1 + 50\text{p} + 20\text{p} + 20\text{p} + 5\text{p} + 2\text{p} - \pounds 1 - 50\text{p} - 2\text{p} - 1\text{p}$ or $(\pounds)2.44$ | M1 | Accept incorrect or missing units Totals either set of coins or Totals all coins or Works out difference | |
| | (their 3.97 + their 1.53) \div 2 or their $(\pounds) 5.5(0) \div 2$ or $(\pounds)2.75$ or (their 3.97 – their 1.53) \div 2 or their $(\pounds) 2.44 \div 2$ or $(\pounds)1.22$ | | M1dep | oe Accept incorrect or missing units |
| | $\pounds 1, 20\text{p}$ and 2p | | A1 | oe eg $\pounds 1.00, \pounds 0.20, \pounds 0.02$ Correct units must be given |
| | Alternative method 2 | | | |
| | Moves 3 coins from Eve to Ola and correctly evaluates one set of coins | M1 | Accept incorrect or missing units | |
| | Moves a different set of 3 coins from Eve to Ola and correctly evaluates both sets of coins | M1dep | Accept incorrect or missing units | |
| | $\pounds 1, 20\text{p}$ and 2p | A1 | oe eg $\pounds 1.00, \pounds 0.20, \pounds 0.02$ Correct units must be given | |
| | Additional Guidance | | | |
| | Answer of 1, 20, 2 with some or all units incorrect or missing | | M1M1A0 | |
| Do not accept eg $\pounds 0.20\text{p}$ | | A0 | | |

| Question | Answer | Mark | Comments |
|-------------------------|--|-----------|--|
| 8 | $12.5(0) + 12.5(0) \div 2$ or $12.5(0) + 6.25$ or $12.5(0) \times 1.5$ or 18.75 | M1 | oe Cost of 2 suits |
| | 9.75×4 or $9.75 \times \frac{2}{3} \times 6$ or $6.5(0) \times 6$ or 39(.00) | M1 | oe eg $9.75 \times 6 - 9.75 \times 2$ or $58.5(0) - 19.5$ Cost of 6 dresses |
| | their 18.75 + their 39(.00) | M1dep | dep on at least M1 awarded Must be adding their suit(s) and their dress(es) May be implied by final answer |
| | 57.75 | A1 | Accept £57.75p |
| | Additional Guidance | | |
| | $6.25 + 9.75 \times 6$ | | M0M0M0dep |
| | $6.25 + 39$ | | M0M1M1dep |
| | $12.50 \times 2 + 39$ | | M0M1M1dep |
| $18.75 + 9.75 \times 2$ | | M1M0M1dep | |

| Question | Answer | Mark | Comments |
|---|---------------------------------------|-------|-------------------|
| 9 | Alternative method 1 | | |
| | 18 – 4 or 14 seen | M1 | oe eg 4 + 14 = 18 |
| | 39 – 2 × their 14 or 39 – 28 or 11 | M1dep | oe eg 14, 14, 11 |
| | 15 | A1 | |
| | Alternative method 2 | | |
| | 39 + 3 × 4 or 39 + 12 or 51 | M1 | |
| | their 51 – 2 × 18 or their 51 – 36 | M1dep | |
| | 15 | A1 | |
| | Additional Guidance | | |
| 14 may be implied by eg twins = 28 (but not just 28 seen) | | M1 | |

| | | | | |
|---|---|---------------------|---------------------------------------|----------------------|
| 10 | Fully correct table | B4 | B1 for each correct decision in a row | |
| | Additional Guidance | | | |
| | | Must be true | Cannot be true | Might be true |
| | The triangle is equilateral | | | ✓ |
| | The triangle has at least one other acute angle | ✓ | | |
| | The triangle is right-angled | | | ✓ |
| The other two angles are each less than 60° | | ✓ | | |
| Mark intention if crosses used eg if a cross is the only mark in a row assume that is the answer | | | | |
| More than one tick in a row is choice for that decision | | | B0 for that row | |

| Question | Answer | Mark | Comments |
|----------|---|------|--|
| 11 | 7 | B1 | |
| 12 | 19.5 | B1 | |
| 13a | 752 951 or 752951 or 752,951 | B1 | Allow commas even if positioning incorrect eg 75,2951 or 752'951 B1 |
| | Additional Guidance | | |
| | 752.951 | | B0 |
| 13b | 20 000 and 400 and 10 and 800 000 and Yes | B3ft | ft correct decision for their answer to (a) oe decision eg it is sensible B2 20 000 and 400 and 10 B1 20 000 or 400 or 10 |
| | Additional Guidance | | |
| | 800 000 (and Yes) with no other values | | B0 |
| | If answer to (a) is 800 000 to 1sf then the correct ft decision in (b) is Yes eg1 (a) 770 000 (b) decision should be Yes eg2 (a) 1762 (b) decision should be No eg3 (a) 752.951 (b) allow decision to be Yes or No | | |

| Question | Answer | Mark | Comments |
|---|--|------|--|
| 14a | Alternative method 1 | | |
| | Two of the three totals correct (2016 =) 136 (2015 =) 143 (2014 =) 132 or 17 + 64 + 50 + 5 and 9 + 72 + 61 + 1 and 19 + 58 + 53 + 2 | M1 | Totals may be seen by table Correct totals may be implied by means (2016 → 34, 2015 → 35.75, 2014 → 33) Addition signs must be shown for horizontal addition but may be implied by a column of numbers in their working |
| | 136 and 143 and 132 and 2015 or 34 and 35.75 and 33 and 2015 | A1 | Totals may be seen by table |
| | Alternative method 2 | | |
| | 8 and -8 and -11 and 4 or -7 and -10 and 14 and 8 and -1 or 11 | M1 | Difference between 2016 and 2015 Difference between 2015 and 2014 Differences may be seen in table |
| | -7 and 11 and 2015 | A1 | Differences may be seen in table |
| | Additional Guidance | | |
| | Differences may have consistently opposite signs for either comparison | | |
| | Ignore totals for quarters shown | | |
| | Allow Year 2 for 2015 | | |
| 136 and 143 and 132, answer 143 | | M1A0 | |
| 136 and 143 and 132, answer 143 in 2015 | | M1A1 | |
| 14b | Quarter 2 | B1 | |

| Question | Answer | Mark | Comments |
|----------|--|-------|--|
| 15 | Alternative method 1 | | |
| | 80 × 0.55 or 44 or 120 × 0.7 or 84 | M1 | oe |
| | 80 × 0.55 + 120 × 0.7 or 44 + 84 or 128 | M1dep | Correct method for both |
| | (80 + 120) × 0.65 or 130 or their 128 ÷ (80 + 120) × 100 or their 128 ÷ 2 or 64 | M1 | 65% of total marks available or their total score for Riya as a percentage of full marks |
| | 128 and 130 and No or 64 and No | A1 | oe eg No, she needed 130 but was 2 marks short oe eg 0.64 and 0.65 and No |
| | Alternative method 2 – marks not scored | | |
| | 80 × 0.45 or 36 or 120 × 0.3 or 36 | M1 | oe |
| | 80 × 0.45 + 120 × 0.3 or 36 + 36 or 72 | M1dep | Correct method for both |
| | (80 + 120) × 0.35 or 70 or their 72 ÷ (80 + 120) × 100 or their 72 ÷ 2 | M1 | 35% of total marks available or their total score for Riya as a percentage of full marks |
| | 72 and 70 and No or 36 and 35 and No | A1 | oe eg No, she failed by 2 marks oe eg 0.36 and 0.35 and No |

Alternative methods 3 and 4 and additional guidance continue on the next two pages

| Question | Answer | Mark | Comments |
|----------------|--|-------|---|
| 15 cont | Alternative method 3 | | |
| | 80×0.55 or 44 | M1 | oe |
| | $(80 + 120) \times 0.65$ or 130 | M1 | 65% of total marks available |
| | their 130 – their 44 or 86 and 120×0.7 or 84 or their 130 – their 44 or 86 and their $86 \div 120 \times 100$ or 71.6... or 72 | M1dep | dep on M1M1 |
| | 86 and 84 and No or 71.6... or 72 and 70 and No | A1 | oe eg No, she needed 2 more marks on B oe eg No, she needed 1.6% more on B |
| | Alternative method 4 | | |
| | 120×0.7 or 84 | M1 | oe |
| | $(80 + 120) \times 0.65$ or 130 | M1 | 65% of total marks available |
| | their 130 – their 84 or 46 and 80×0.55 or 44 or their 130 – their 84 or 46 and their $46 \div 80 \times 100$ or 57.5 | M1dep | dep on M1M1 |
| | 46 and 44 and No or 57.5 and 55 and No | A1 | oe eg No, she needed 2 more marks on A oe eg No, she needed 2.5% more on A |

Additional guidance continues on the next page

| Question | Answer | Mark | Comments |
|----------|--------|------|----------|
|----------|--------|------|----------|

| 15 cont | Additional Guidance | | |
|---------|--|--|--------------|
| | Build up steps for percentages must be correct or have fully correct method shown for any incorrect steps eg1 $50\% = 40$, $5\% = 16$, section A = 56 eg2 $50\% = 40$, $5\% = 80 \times 0.05 = 16$, section A = 56 | | M0 M1 |
| | Ignore % signs given with marks eg 44% | | |
| | 128 and she needs 2 more marks implies No | | M1M1M1A1 |
| | $55 + 70 = 125$ $125 \rightarrow 62.5\%$ and No | | M0M0 M1A0 |
| | Allow misread of 55% of 120 and 70% of 80 for method marks | | max M3 |

| 16 | $2 \times \pi \times 37$ or $\pi \times 74$ or 8×37 or 296 | M1 | Accept [3.14, 3.142] for π |
|----|--|----|--------------------------------------|
| | [232, 233] or 74π | A1 | May be implied by eg $74\pi + \dots$ |
| | [528, 529] or $74\pi + 296$ | A1 | |
| | Additional Guidance | | |
| | $360 - 37 \times 8$ | | M1A0A0 |
| | 37×8 or 296 seen and then eg halved or doubled | | M1 |

| Question | Answer | Mark | Comments |
|-----------------------|--|------|--|
| 17a | Alternative method 1 | | |
| | $1.8 \times -40 + 32$ or -72 | M1 | oe eg $1.8(-40) + 32$ |
| | $1.8 \times -40 + 32 = -40$ or $1.8 \times -40 = -72$ and $-72 + 32 = -40$ | A1 | oe eg $1.8(-40) + 32 = -40$ Full working must be seen oe eg $1.8 \times -40 = -72$ and $-40 - 32 = -72$ |
| | Alternative method 2 | | |
| | $\frac{-40 - 32}{1.8}$ or -72 | M1 | |
| | $\frac{-40 - 32}{1.8} = -40$ or $-40 - 32 = -72$ and $-72 \div 1.8 = -40$ | A1 | Full working must be seen oe eg $-40 - 32 = -72$ and $-40 \times 1.8 = -72$ |
| | Alternative method 3 | | |
| | $F = 1.8F + 32$ and $F - 1.8F = 32$ or $0.8F = -32$ | M1 | Forms equation in one variable and collects terms correctly using any letter oe eg $1.8F - F = -32$ or $-0.8F = 32$ |
| | $(F =) -32 \div 0.8$ and $F = -40$ | A1 | Full working must be seen oe eg $(F =) 32 \div -0.8$ and $F = -40$ |
| | Additional Guidance | | |
| | Ignore units | | |
| | 72 does not imply M1 | | |
| Only $-72 + 32 = -40$ | | M1A0 | |

| Question | Answer | Mark | Comments |
|------------|---|----------|----------|
| 17b | No and 5 or No and correctly evaluated counter example | B1 | |
| | Additional Guidance | | |
| | No, anything between -17°C and 0°C is positive in Fahrenheit | B1 | |
| | No, anything between 0°F and 32°F is negative in Celsius | B1 | |
| | Unless the range from -17°C to 0°C is given, then the counter example must be evaluated correctly | | |
| | No because 1.8×-15 is -27 , and $32 - 27 = 4$ | B0 | |
| | Any temperature in Celsius between $-17\frac{7}{9}^{\circ}\text{C}$ and 0°C can be used as a counter-example eg1 $1.8 \times -10 + 32 = 14$ so No eg2 $1.8 \times -1 + 32 = 30.2$ so No | B1 B1 | |
| | No because 14°F is -10°C | B1 | |
| | Accept No because $-10 = 14$ | B1 | |
| | No because -15 is positive in Fahrenheit | B0 | |

| Question | Answer | Mark | Comments |
|----------|--------|------|----------|
|----------|--------|------|----------|

| | | | |
|---|---|--------|--|
| 18 | Alternative method 1 | | |
| | 6×4 or 24 stated or implied as target total of the four cards | M1 | Indicating 1, 5, 7 and 11 are the chosen four cards implies M2 |
| | $1 + 5 + 7 + 9 + 11$ or 33 | M1 | |
| | 9 | A1 | |
| | Alternative method 2 | | |
| | $1, 5, 7, 9 \rightarrow (1 + 5 + 7 + 9) \div 4$ or $1, 5, 7, 11 \rightarrow (1 + 5 + 7 + 11) \div 4$ or $1, 5, 9, 11 \rightarrow (1 + 5 + 9 + 11) \div 4$ or $1, 7, 9, 11 \rightarrow (1 + 7 + 9 + 11) \div 4$ or $5, 7, 9, 11 \rightarrow (5 + 7 + 9 + 11) \div 4$ | M1 | $1, 5, 7, 9 \rightarrow 22 \div 4$ or $1, 5, 7, 11 \rightarrow 24 \div 4$ or $1, 5, 9, 11 \rightarrow 26 \div 4$ or $1, 7, 9, 11 \rightarrow 28 \div 4$ or $5, 7, 9, 11 \rightarrow 32 \div 4$ |
| | $1, 5, 7, 9 \rightarrow 5.5$ or $1, 5, 7, 11 \rightarrow 6$ or $1, 5, 9, 11 \rightarrow 6.5$ or $1, 7, 9, 11 \rightarrow 7$ or $5, 7, 9, 11 \rightarrow 8$ | A1 | |
| | 9 | A1 | with no error in the mean of 1, 5, 7, 11 |
| | Additional Guidance | | |
| | Use the alternative scheme that awards the better mark | | |
| $33 - 24$ | | M1M1A0 | |
| $1 + 5 + 7 + 11 = 28, 28 \div 4 = 6,$ answer 9 (with no other work) | | M1A0A0 | |

| | | | |
|-----|---|----|----------|
| 19a | $120 \div (1 + 4)$ or $120 \div 5$ or 24 or 96 | M1 | oe |
| | 24 : 96 | A1 | in order |
| | Additional Guidance | | |
| | 96 : 24 | | M1A0 |
| | $120 \div 5$ and $120 \div 4$ is choice unless intention is clear | | M0A0 |
| | Further cancelling after 24 : 96 seen eg 1 : 4 | | M1A0 |

| Question | Answer | Mark | Comments |
|----------|---|-------|--|
| 19b | $1.75 : 1$ or $1\frac{3}{4} : 1$ or $\frac{7}{4} : 1$ | B1 | |
| 20 | Alternative method 1 | | |
| | 1350×0.02 or 27 | M1 | 1350×1.02 or 1377 implies M1M1dep |
| | 1350 + their 27 or 1377 | M1dep | |
| | their 1377 \times 12 or 16 524 | M1 | Monthly pay \times 12 |
| | 47×37.5 or 1762.5 | M1 | May be seen as pay \div 47 \div 37.5 |
| | 9.37... or 9.38 | A1 | Allow 9.40 with method Accept eg £9.38p but not 9.4 |
| | Alternative method 2 | | |
| | 1350×12 or 16 200 | M1 | Monthly pay \times 12 |
| | their 16 200 \times 0.02 or 324 | M1dep | |
| | their 16 200 + their 324 or their 16 200 \times 1.02 or 16 524 | M1dep | dep on M1M1 |
| | 47×37.5 or 1762.5 | M1 | May be seen as pay \div 47 \div 37.5 |
| | 9.37... or 9.38 | A1 | Allow 9.40 with method Accept eg £9.38p but not 9.4 |

Alternative methods 3 and 4 and additional guidance continue on the next two pages

| Question | Answer | Mark | Comments |
|----------------|--|-------|--|
| 20 cont | Alternative method 3 | | |
| | 1350×12 or 16 200 | M1 | |
| | 47×37.5 or 1762.5 | M1 | May be seen as pay \div 47 \div 37.5 |
| | their 16 200 \div their 1762.5 or 9.19... and their 9.19... \times 0.02 or 0.18... | M1dep | Increase per hour dep on M1M1 |
| | their 9.19... + their 0.18... | M1dep | dep on M1M1M1 |
| | 9.37... or 9.38 | A1 | Allow 9.40 with method Accept eg £9.38p but not 9.4 |
| | Alternative method 4 | | |
| | 47×37.5 or 1762.5 | M1 | |
| | their 1762.5 \div 12 or 146.87(5) or 146.88 | M1dep | Hours per month |
| | $1350 \div$ their 146.87(5) or 9.19... and their 9.19... \times 0.02 or 0.18... | M1dep | Increase per hour |
| | their 9.19... + their 0.18... | M1dep | |
| | 9.37... or 9.38 | A1 | Allow 9.40 with method Accept eg £9.38p but not 9.4 |

Additional guidance continues on the next page

| Question | Answer | Mark | Comments |
|----------|--------|------|----------|
|----------|--------|------|----------|

| | | | |
|----------------|---|-------------------|-------------|
| 20 cont | Additional Guidance | | |
| | Build up steps for 2% or 102% must be correct or have fully correct method shown for any incorrect steps eg1 1% = 135, 2% = 270, monthly pay = 1620 eg2 1% = 135, 2% = 2 × 135 = 270, monthly pay = 1620 eg3 1% = 1350 ÷ 100 = 135, 2% = 270, monthly pay = 1620 | | |
| | If correct methods or values are seen ignore choice of methods | | |
| | 27 or 16 200 or 1762.5 | | at least M1 |
| | 1377 or 324 | at least M1M1 | |
| | 16 524 | at least M1M1M1 | |
| | 1377 ÷ 4 = 344.25 344.25 ÷ 37.5 = 9.18 (unless other correct values seen elsewhere in working) | M1M1dep M0M0A0 | |

| | | | | | | | | | | | | |
|----------------------------|--|------|---|---|----|----|----|------|------|------|------|---|
| 21a | <table border="1" style="margin-left: auto; margin-right: auto;"> <tr><td style="text-align: center;">K</td><td style="text-align: center;">L</td><td style="text-align: center;">M</td></tr> <tr><td style="text-align: center;">84</td><td style="text-align: center;">54</td><td style="text-align: center;">62</td></tr> <tr><td style="text-align: center;">0.42</td><td style="text-align: center;">0.27</td><td style="text-align: center;">0.31</td></tr> </table> | K | L | M | 84 | 54 | 62 | 0.42 | 0.27 | 0.31 | B2 | oe B1 0.27 oe for relative frequency of L or 0.31 oe for relative frequency of M or B1ft ft their 62 ÷ 200 for relative frequency of M |
| | K | L | M | | | | | | | | | |
| 84 | 54 | 62 | | | | | | | | | | |
| 0.42 | 0.27 | 0.31 | | | | | | | | | | |
| Additional Guidance | | | | | | | | | | | | |
| | <table border="1" style="margin-left: auto; margin-right: auto;"> <tr><td style="text-align: center;">K</td><td style="text-align: center;">L</td><td style="text-align: center;">M</td></tr> <tr><td style="text-align: center;">84</td><td style="text-align: center;">54</td><td style="text-align: center;">68</td></tr> <tr><td style="text-align: center;">0.42</td><td style="text-align: center;">0.2</td><td style="text-align: center;">0.34</td></tr> </table> | K | L | M | 84 | 54 | 68 | 0.42 | 0.2 | 0.34 | B1ft | |
| K | L | M | | | | | | | | | | |
| 84 | 54 | 68 | | | | | | | | | | |
| 0.42 | 0.2 | 0.34 | | | | | | | | | | |

| Question | Answer | Mark | Comments |
|------------|--|------|--------------|
| 21b | Alternative method 1 | | |
| | 500 × 0.42 or $84 \times \frac{500}{200}$ or 84 × 2 + 84 ÷ 2 or 168 + 42 | M1 | oe |
| | 210 | A1 | |
| | Alternative method 2 | | |
| | 300 × 0.42 + 84 or 126 + 84 | M1 | oe |
| | 210 | A1 | |
| | Additional Guidance | | |
| | $\frac{210}{500}$ | | M1A0 |
| | Embedded answer eg 210 ÷ 500 = 0.42, answer 0.42 | | M1A0 |
| | Misread of working out L or M (must see method) eg L: 500 × their 0.27 or $54 \times \frac{500}{200}$ eg M: 500 × their 0.31 or their $62 \times \frac{500}{200}$ | | M1A0 |
| | Build up steps must be correct or have fully correct method shown for any incorrect steps eg1 200 = 84, 400 = 164, 100 = 42, Answer 206 eg2 200 = 84, 400 = 84 × 2 = 164, 100 = 42, Answer 206 | | M0A0 M1A0 |

| Question | Answer | Mark | Comments |
|--|---|------------------|--|
| 22 | 64 000 000 ÷ 95 000 or 673.(...) or 674 or $\frac{12\ 800}{19}$ or 82 000 000 ÷ 140 000 or 585.(...) or 586 or $\frac{4100}{7}$ | M1 | oe population ÷ area Accept a pair of consistent divisions eg 64 ÷ 95 or 0.673... or 0.674 and 82 ÷ 140 or 0.585... or 0.586 |
| | 673.(...) or 674 or 670 and 585.(...) or 586 or 590 or $\frac{89\ 600}{133}$ and $\frac{77\ 900}{133}$ | A1 | Correct comparable values from consistent divisions eg 0.674 and 0.586 Accept 700 with division seen for UK Accept 600 with division seen for Germany |
| | Comparable values and correct conclusion | A1ft | eg 673 and 585 and greater for UK 0.673 and 0.585 and greater for UK ft M1A0 and comparable values Ignore further work |
| | Additional Guidance | | |
| | Comparable values means both must be in the same form eg fractions with common denominators | | |
| | 64 000 000 ÷ 95 000 = 67.4 82 000 000 ÷ 140 000 = 585.7 Germany is higher | M1 A0 A1ft | |
| | Ignore subtraction of results | | |
| | 673 and 585 and UK has more people per square mile | M1A1A1ft | |
| | 673 and 585 and Germany has more space for their population | M1A1A1ft | |
| | 673 and 585 and UK's population is less spread out | M1A1A1ft | |
| 673 and 585 and UK is more than Germany | M1A1A1ft | | |
| 673 and 585 and UK is 78 more than Germany (ignore further work) | M1A1A1ft | | |

Additional guidance continues on the next page

| Question | Answer | Mark | Comments |
|----------------|--|------|----------|
| 22 cont | 673 and 585 and the difference is 88 | | M1A1A0ft |
| | 673 and 585 and UK population is bigger | | M1A1A0ft |
| | 673 and 586 and UK | | M1A1A0ft |
| | 673 and 585 and Germany has more space | | M1A1A0ft |
| | 673 > 585 (unless links to countries in working) | | M1A1A0ft |
| | $\frac{12\,800}{19}$ and $\frac{4100}{7}$ and UK is greater (fractions not comparable) | | M1A0A0ft |
| 23 | Number of televisions sold | B1 | |

| Question | Answer | Mark | Comments | |
|-----------------------------------|--|------|--|--|
| 24 | Enlargement | B1 | | |
| | Scale factor (\times) $\frac{1}{3}$ | B1 | | |
| | Centre (5, 1) | B1 | | |
| | Additional Guidance | | | |
| | Enlarge (\times) $\frac{1}{3}$ (5, 1) | | B1B1B1 | |
| | Reduction or makes bigger or unenlargement or increase or negative enlargement | | 1st B0 | |
| | Any other transformation mentioned or implied such as reflection, rotation or translation loses the mark for enlargement eg enlarged and moved up 4 or enlarged and $\begin{pmatrix} -2 \\ 2 \end{pmatrix}$ | | 1st B0 | |
| | Do not accept $\div 3$ for scale factor | | 2nd B0 | |
| 25(a) | Correct product using a point on the curve or correct division using a point on the curve | B1 | eg $2 \times 12 (= 24)$ or $3 \times 8 (= 24)$ or $5 \times 4.8 (= 24)$ or $6 \times 4 (= 24)$ or $10 \times 2.4 (= 24)$ or $24 \div 2 = 12$ or $24 \div 6 = 4$ | |
| | Additional Guidance | | | |
| | $1 \times 24 (= 24)$ | | B0 | |
| | $12 + 12 (= 24)$ | | B0 | |
| | $3 \times 4 \times 2 = 24$ | | B0 | |
| | For multiplication, 24 does not have to be shown | | | |
| | Ignore any units seen | | | |
| | Ignore any lines on the graph | | | |
| | $8 \times 3 = 24$ and $12 + 12 = 24$ (choice) | | B0 | |
| area 6 and length 4 and volume 24 | | B0 | | |

| Question | Answer | Mark | Comments |
|----------|---|-------|----------|
| 25(b) | Alternative method 1 | | |
| | Reading from 5 on the graph to give [4.7, 4.9] | M1 | |
| | $\frac{1}{2} \times 6 \times h = [4.7, 4.9]$ or $[4.7, 4.9] \div (\frac{1}{2} \times 6)$ | M1dep | oe |
| | [1.56, 1.64] | A1 | |
| | Alternative method 2 | | |
| | $24 \div 5$ or 4.8 or $\frac{1}{2} \times 6 \times h$ or $\frac{1}{2} \times 6 \times h \times 5$ | M1 | oe |
| | $\frac{1}{2} \times 6 \times h = 24 \div 5$ or $24 \div 5 \div (\frac{1}{2} \times 6)$ or $\frac{1}{2} \times 6 \times h \times 5 = 24$ or $15h = 24$ or $24 \div (\frac{1}{2} \times 6 \times 5)$ or $24 \div 15$ | M1dep | oe |
| | 1.6 | A1 | |
| | Additional Guidance | | |
| | | | |

| Question | Answer | Mark | Comments |
|----------|--|------|----------|
| 26a | $\frac{3}{4} \times \frac{3}{4} \times 15$ or $\frac{3}{4} \times 15$ or 11.25 and $\frac{3}{4} \times$ their 11.25 | M1 | oe |
| | 8.4(375) or 8.44 or 8.438 or $\frac{135}{16}$ or $8\frac{7}{16}$ | A1 | |
| | Additional Guidance | | |
| | 8.43 or 8.437 | | M1A1 |
| | 8.4 seen, answer 8 | | M1A1 |
| | $\frac{3}{4}$ of 11.25 (unless correctly evaluated) | | M0 |
| | $\frac{3}{4} \times 8.4375$, answer 6.328 (further work) | | M1A0 |
| | 11.25 + 8.4375, answer 19.6875 (further work) | | M1A0 |

| Question | Answer | Mark | Comments |
|------------|--|------|--|
| 26b | Alternative method 1 | | |
| | Ticks second box and [7.425, 7.5375] or Ticks second box and correctly evaluates $\frac{2}{3} \times$ their 11.25 | B2ft | ft correct box ticked for comparing with their answer to (a) B1ft [7.425, 7.5375] with no or incorrect decision or Correctly evaluates $\frac{2}{3} \times$ their 11.25 with no or incorrect decision |
| | Alternative method 2 | | |
| | Ticks second box and valid comparison | B2 | eg $\frac{8}{12}$ and $\frac{9}{12}$ 0.66... or 0.67 and 0.75 66.(...)% or 67% and 75% $\frac{9}{16}$ and $\frac{8}{16}$ clear diagrams showing $\frac{2}{3}$ and $\frac{3}{4}$ B1 Ticks second box and incomplete comparison eg $\frac{8}{12}$ and $\frac{3}{4}$ two thirds is less than three quarters $\frac{3}{4} \times \frac{3}{4} = \frac{9}{16}$ and $\frac{3}{4} \times \frac{2}{3} = \frac{6}{12}$ or Valid comparison (that would score B2) with no or incorrect decision |

Additional guidance continues on the next page

| Question | Answer | Mark | Comments |
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| Additional Guidance | | | |
|----------------------------|---|--|------|
| 26b cont | In Alt 1 only follow through their answer to (a) for the comparison, the working for $\frac{2}{3}$ of their 11.25 must be correct | | |
| | (a) answer 6.5 (b) Ticks first box and 7.5 seen | | B2ft |
| | Accept 0.66... or 0.67 for $\frac{2}{3}$ | | |
| | Using 0.6 for $\frac{2}{3}$ | | B0 |

| | | | |
|-----------|---|------|--|
| 27 | Alternative method 1 | | |
| | $12x - 8$ | M1 | May be seen in a grid |
| | their $12x - 2x = -5 +$ their 8 or $10x = 3$ or their $-8 + 5 = 2x -$ their 12x or $-3 = -10x$ | M1 | Collecting two terms in x and two constant terms correctly oe eg $10x - 3 = 0$ |
| | 0.3 or $\frac{3}{10}$ | A1ft | ft M1M0 or M0M1 with exactly one error |
| | Alternative method 2 | | |
| | $\frac{x}{2} - \frac{5}{4}$ | M1 | |
| | $3x -$ their $\frac{x}{2} =$ their $-\frac{5}{4} + 2$ or $\frac{5}{2}x = \frac{3}{4}$ or $-2 +$ their $\frac{5}{4} =$ their $\frac{x}{2} - 3x$ or $-\frac{3}{4} = -\frac{5}{2}x$ | M1 | Collecting two terms in x and two constant terms correctly oe eg $\frac{5}{2}x - \frac{3}{4} = 0$ |
| | 0.3 or $\frac{3}{10}$ | A1ft | ft M1M0 or M0M1 with exactly one error |

Additional guidance continues on the next page

| Question | Answer | Mark | Comments |
|----------|--------|------|----------|
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| 27 cont | Additional Guidance | | |
|---------|---|--|------------------|
| | $12x - 2 = 2x - 5$ $10x = -3$ $x = -0.3$ | | M0 M1 A1ft |
| | $12x - 8 = 2x - 5$ $10x = -5$ $x = \frac{-5}{10}$ | | M1 M0 A1ft |
| | $12x - 8 = 2x - 5$ $14x = 3$ $x = \frac{3}{14}$ | | M1 M0 A1ft |
| | $12x - 8 = 2x - 5$ $14x = -13$ $x = -\frac{13}{14}$ (two errors) | | M1 M0 A0ft |
| | $12x - 8 = 8x - 20$ | | M1M0A0 |
| | Any ft answer must be exact or rounded or truncated to at least 2 dp | | |
| | The last two marks can be implied without the collection of terms seen eg $12x - 6 = 2x - 5$ and answer 0.1 | | M0M1A1ft |
| | Collecting terms before the bracket has been expanded | | Zero |

| 28 | $3 \ 6 \ 9 \ \dots$ or $23 + 12$ or $1.5n^2 \dots$ | M1 | |
|----|---|----|------|
| | 35 | A1 | |
| | Additional Guidance | | |
| | Answer line blank with 35 as next term in sequence | | M1A1 |
| | Answer line has attempt at term to term rule or nth term but 35 seen | | M1A0 |
| | 35 seen on dotted line in sequence but a different answer given eg 50 | | M1A0 |

| Question | Answer | Mark | Comments | |
|--|---|------|---|--|
| 29 | $\tan x = \frac{3}{7}$ or $\tan^{-1} \frac{3}{7}$ or $\sin x = \frac{3(\sin 90)}{\sqrt{3^2 + 7^2}}$ or $\sin x = \frac{3(\sin 90)}{\sqrt{58}}$ or $\cos x = \frac{7}{\sqrt{3^2 + 7^2}}$ or $\cos x = \frac{7}{\sqrt{58}}$ or $90 - \tan^{-1} \frac{7}{3}$ or $90 - [66.7, 66.81]$ or $90 - 67$ | M1 | oe eg $\cos x = \frac{7^2 + (\sqrt{7^2 + 3^2})^2 - 3^2}{2 \times \sqrt{3^2 + 7^2} \times 7}$ Any letter | |
| | [23, 23.3] | | A1 | |
| | Additional Guidance | | | |
| | $\tan = \frac{3}{7}$ or $\tan \frac{3}{7}$ or $\tan^{-1} = \frac{3}{7}$ (unless recovered) | M0 | | |
| | Answer [23, 23.3] (possibly coming from scale drawing) | M1A1 | | |
| | If using sine rule must rearrange to $\sin x =$ for M1 | | | |
| | If using cosine rule must rearrange to $\cos x =$ for M1 | | | |
| | Allow [0.42, 0.43] for $\frac{3}{7}$ | | | |
| | Allow 2.33... for $\frac{7}{3}$ | | | |
| Allow [7.6, 7.62] for $\sqrt{3^2 + 7^2}$ | | | | |