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Candidate surname

Other names

Centre Number

Candidate Number

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## Pearson Edexcel Level 3 GCE

Time 1 hour 30 minutes

Paper  
reference

**9FM0/4A**

### Further Mathematics

Advanced

**PAPER 4A: Further Pure Mathematics 2**

**You must have:**

Mathematical Formulae and Statistical Tables (Green), calculator

Total Marks

**Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebraic manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

#### Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

#### Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 10 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

#### Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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3.

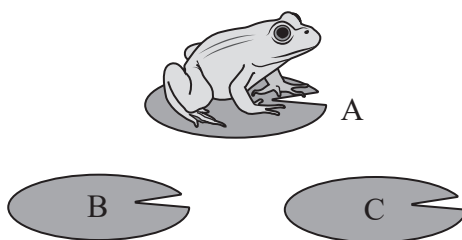


Figure 1

There are three lily pads on a pond. A frog hops repeatedly from one lily pad to another.

The frog starts on lily pad A, as shown in Figure 1.

In a model, the frog hops from its position on one lily pad to either of the other two lily pads with equal probability.

Let  $p_n$  be the probability that the frog is on lily pad A after  $n$  hops.

- (a) Explain, with reference to the model, why  $p_1 = 0$  (1)

The probability  $p_n$  satisfies the recurrence relation

$$p_{n+1} = \frac{1}{2}(1 - p_n) \quad n \geq 1 \quad \text{where } p_1 = 0$$

- (b) Prove by induction that, for  $n \geq 1$

$$p_n = \frac{2}{3} \left( -\frac{1}{2} \right)^n + \frac{1}{3} \quad (6)$$

- (c) Use the result in part (b) to explain why, in the long term, the probability that the frog is on lily pad A is  $\frac{1}{3}$  (1)

















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(Total for Question 5 is 6 marks)



P 6 5 5 0 6 A 0 1 5 3 2



















9.

$$I_n = \int_0^{\frac{\pi}{2}} \sin^n 2x \, dx$$

(a) Prove that for  $n \geq 2$ 

$$I_n = \frac{n-1}{n} I_{n-2} \quad (4)$$

(b) Hence determine the exact value of

$$\int_0^{\frac{\pi}{2}} 64 \sin^5 x \cos^5 x \, dx \quad (3)$$











10.

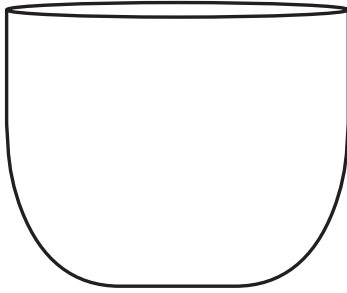


Figure 2

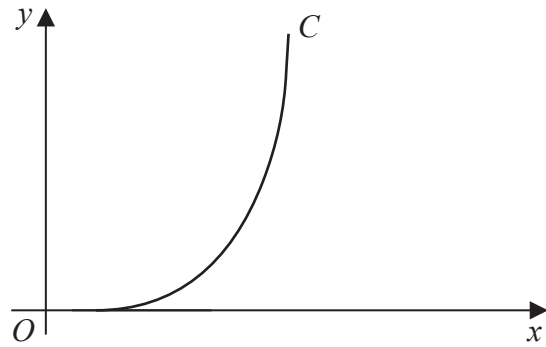


Figure 3

Figure 2 shows a picture of a plant pot.

The plant pot has

- a flat circular base of radius 10 cm
- a height of 15 cm

Figure 3 shows a sketch of the curve  $C$  with parametric equations

$$x = 10 + 15t - 5t^3 \quad y = 15t^2 \quad 0 \leq t \leq 1$$

The curved inner surface of the plant pot is modelled by the surface of revolution formed by rotating curve  $C$  through  $2\pi$  radians about the  $y$ -axis.

- (a) Show that, according to the model, the area of the curved inner surface of the plant pot is given by

$$150\pi \int_0^1 (2 + 3t + 2t^2 + 2t^3 - t^5) dt \tag{5}$$

- (b) Determine, according to the model, the total area of the inner surface of the plant pot. (4)

Each plant pot will be painted with one coat of paint, both inside and outside. The paint in one tin will cover an area of  $12\text{ m}^2$

- (c) Use the answer to part (b) to estimate how many plant pots can be painted using one tin of paint. (2)
- (d) Give a reason why the model might not give an accurate answer to part (c). (1)

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