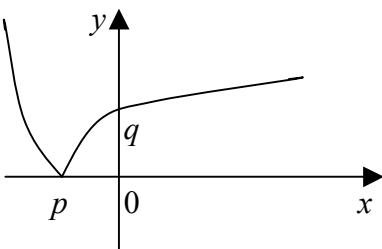
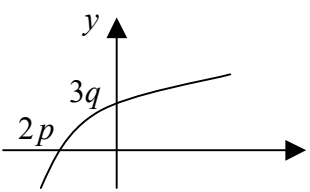
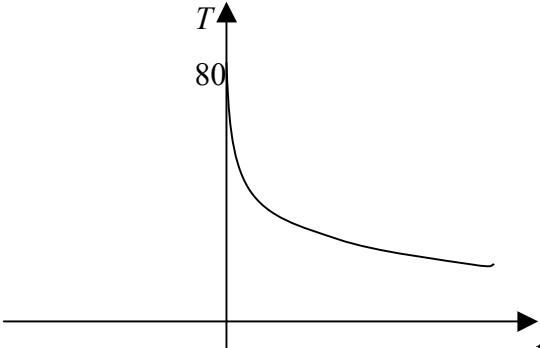


Question number	Scheme	Marks
1.	(a) $ x - 2  - 3 = 1$ <span style="float: right;"><math>x = 6</math></span> $-(x - 2) - 3 = 1 \Rightarrow x = -2$	B1 M1 A1 (3)
	(b) $g(x) = x^2 - 4x + 11 = (x - 2)^2 + 7$ or $g'(x) = 2x - 4$ $g'(x) = 0 \Rightarrow x = 2$ Range: $g(x) \geq 7$ .	M1 A1 A1 (3)
	(c) $gf(-1) = g(0)$ correct order; $= 11$	M1 A1 (2)
<b>(8 marks)</b>		
2.	(a) $f(2) = 8 - 4 - 5 = -1$ <span style="float: right;">method shows change of sign</span> $f(3) = 27 - 6 - 5 = 16$ <span style="float: right;"><math>\Rightarrow</math> root with accuracy</span>	M1 A1 (2)
	(b) $x_1 = 2.121, x_2 = 2.087, x_3 = 2.097, x_4 = 2.094$	M1 A2 (1, 0) (3)
	(c) Choosing suitable interval, e.g. [2.09455, 2.09465] $f(2.09455) = -0.00001\dots$ <span style="float: right;">shows change of sign</span> $f(2.09465) = +0.001(099\dots)$ <span style="float: right;">accuracy and conclusion</span>	M1 A1 (3)
	<b>(8 marks)</b>	
3.	(a) $\cos(A + B) = \cos A \cos B - \sin A \sin B$ (formula sheet) $\cos(\frac{1}{2}\theta + \frac{1}{2}\theta)$ $= \cos(\frac{1}{2}\theta) \cos(\frac{1}{2}\theta) - \sin(\frac{1}{2}\theta) \sin(\frac{1}{2}\theta) = \cos^2(\frac{1}{2}\theta) - \sin^2(\frac{1}{2}\theta)$ $= \{1 - \sin^2(\frac{1}{2}\theta)\} - \sin^2(\frac{1}{2}\theta) = 1 - 2\sin^2(\frac{1}{2}\theta)$	M1 M1 A1 (3)
	(b) $\sin\theta + 1 - \cos\theta = 2 \sin(\frac{1}{2}\theta) \cos(\frac{1}{2}\theta) + 2 \sin^2(\frac{1}{2}\theta)$ $= 2 \sin(\frac{1}{2}\theta) [\cos(\frac{1}{2}\theta) + \sin(\frac{1}{2}\theta)]$ [M1 use of $\sin 2A = 2 \sin A \cos A$ ; M1 use of (a)]	M1 M1 A1 (3)
	(c) $2 \sin(\frac{1}{2}\theta) [\cos(\frac{1}{2}\theta) + \sin(\frac{1}{2}\theta)] = 0$ $\Rightarrow \sin(\frac{1}{2}\theta) = 0$ or $\cos(\frac{1}{2}\theta) + \sin(\frac{1}{2}\theta) = 0$ $\theta = 0$ $\tan \frac{1}{2}\theta = -1; \Rightarrow \theta = \frac{3}{2}\pi$	M1 B1 M1 A1 (4)
<b>(10 marks)</b>		

Question number	Scheme	Marks
<p>4. (a)</p> <p>(b)</p>	<p><math>x^2 + 2x - 3 = (x + 3)(x - 1)</math></p> <p><math>f(x) = \frac{x(x^2 + 2x - 3) + 3(x + 3) - 12}{(x + 3)(x - 1)} \quad \left[ = \frac{x^3 + 2x^2 - 3}{(x + 3)(x - 1)} \right]</math></p> <p><math>= \frac{(x - 1)(x^2 + 3x + 3)}{(x - 1)(x + 3)}</math></p> <p><math>= \frac{(x^2 + 3x + 3)}{(x + 3)}</math></p> <p><math>f'(x) = \frac{(x + 3)(2x + 3) - (x^2 + 3x + 3)}{(x + 3)^2} \quad \left[ = \frac{x^2 + 6x + 6}{(x + 3)^2} \right]</math></p> <p>Setting <math>f'(x) = \frac{22}{25}</math> and attempting to solve quadratic</p> <p><math>x = 2</math> (only this solution)</p>	<p>B1</p> <p>M1A1</p> <p>M1</p> <p>A1 (5)</p> <p>M1 A2, 1, 0</p> <p>M1</p> <p>A1 (5)</p> <p><b>(10 marks)</b></p>
<p>ALT (b)</p>	<p>ALT: <math>f(x) = x + \frac{3}{x + 3}, \quad f'(x) = 1 - \frac{3}{(x + 3)^2}</math></p>	

Question number	Scheme	Marks
<p>5. (a)</p>	<p>(i) </p>	<p>Shape correct: B1 Intercepts B1 (2)</p>
	<p>(ii) </p>	<p>Shape correct B1 (2p, 0) on x B1 (0, 3q) on y B1 (3)</p>
	<p>(b) <math>q = 3 \ln 3</math></p>	<p>B1 (1)</p>
	<p>(c) <math>\ln(2p + 3) = 0 \Rightarrow 2p + 3 = 1; \quad p = -1</math></p>	<p>M1 A1 (2)</p>
	<p>(d) <math>\frac{dy}{dx} = \frac{6}{2x+3};</math> evaluated at <math>x = p</math> (6)</p>	<p>M1 A1</p>
	<p>Equation: <math>y = 6(x + 1)</math> any form</p>	<p>M1 A1ft (4) <b>(12 marks)</b></p>

Question number	Scheme	Marks
6. (a)	$T = 80$	B1 (1)
(b)	$e^{-0.1t} \geq 0$ or equivalent	B1 (1)
(c)	<p>Negative exponential shape</p> <p><math>t \geq 0</math>, "80"</p> <p>clearly not <math>\rightarrow x</math>-axis</p> 	M1  A1 (2)
(d)	$60 = 20 + 60 e^{-0.1t} \Rightarrow 60 e^{-0.1t} = 40$ $\Rightarrow -0.1t = \ln\left(\frac{2}{3}\right)$ $t = 4.1$	M1  M1A1  A1 (4)
(e)	$\frac{dT}{dt} = -6 e^{-0.1t}$	M1A1 (2)
(f)	<p>Using <math>\frac{dT}{dt} = -1.8</math></p> <p>Solving for <math>t</math>, or using value of <math>e^{-0.1t}</math> (0.3)</p> $T = 38$	B1  M1  A1 (3)
		<b>(13 marks)</b>

Question number	Scheme	Marks
7. (i)	$\frac{dy}{dx} = \sec^2 x - 2 \sin x$	B1 B1
	<p style="text-align: center;">When <math>x = \frac{1}{4}\pi</math>, <math>\frac{dy}{dx} = 2 - \sqrt{2}</math></p>	B1 (3)
(ii)	$\frac{dx}{dy} = \frac{1}{2} \sec^2 \frac{1}{2} y$	B1
	$\frac{dy}{dx} = \frac{2}{\sec^2\left(\frac{y}{2}\right)} = \frac{2}{1 + \tan^2\left(\frac{y}{2}\right)} = \frac{2}{1 + x^2}$	M1 M1 A1 (4)
(iii)	$\frac{dy}{dx} = 2e^{-x} \cos 2x - e^{-x} \sin 2x = e^{-x} (2\cos 2x - \sin 2x)$ <p>Method for R: <math>R = 2.24</math> (allow <math>\sqrt{5}</math>)</p> <p>Method for <math>\alpha</math>: <math>\alpha = 0.464</math></p>	M1 A1 A1 M1 A1 M1 A1 (7) <b>(14 marks)</b>