

Centre Number						Candidate Number				
Surname										
Other Names										
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For Examiner's Use	
Examiner's Initials	
Pages	Mark
3	
4 – 5	
6 – 7	
8 – 9	
10 – 11	
12 – 13	
14 – 15	
16	
TOTAL	



Level 2 Certificate in Further Mathematics

Further Mathematics

Level 2

8360/1

Practice Paper Set 4

Paper 1

Non-Calculator

<p>For this paper you must have:</p> <ul style="list-style-type: none"> mathematical instruments. <p>You may not use a calculator.</p>	
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Time allowed: 1 hour 30 minutes

Instructions

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer the questions in the space provided. Do not write outside the box around each page or on blank pages.
- Do all rough work in this book. Cross through any work that you do not want to be marked.
- In all calculations, show clearly how you work out your answer.

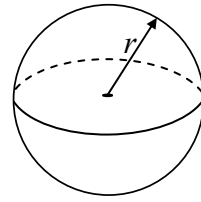
Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 70.
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to this answer booklet.

Formulae Sheet

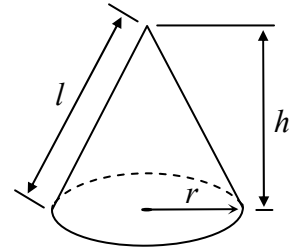
$$\text{Volume of sphere} = \frac{4}{3} \pi r^3$$

$$\text{Surface area of sphere} = 4\pi r^2$$



$$\text{Volume of cone} = \frac{1}{3} \pi r^2 h$$

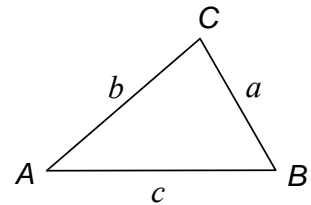
$$\text{Curved surface area of cone} = \pi r l$$



In any triangle ABC

$$\text{Area of triangle} = \frac{1}{2} ab \sin C$$

$$\text{Sine rule} \quad \frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$



$$\text{Cosine rule} \quad a^2 = b^2 + c^2 - 2bc \cos A$$

$$\cos A = \frac{b^2 + c^2 - a^2}{2bc}$$

The Quadratic Equation

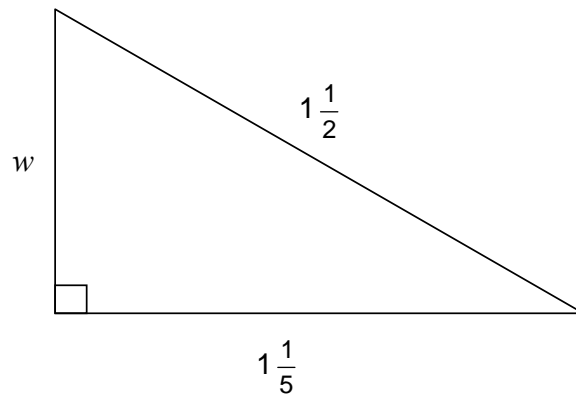
The solutions of $ax^2 + bx + c = 0$, where $a \neq 0$, are given by $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

Trigonometric Identities

$$\tan \theta \equiv \frac{\sin \theta}{\cos \theta} \quad \sin^2 \theta + \cos^2 \theta \equiv 1$$

Answer **all** questions in the spaces provided.

1



Not drawn
accurately

Work out the value of w .

$w = \dots\dots\dots$ (4 marks)

- 2** In this identity, h and k are integer constants.

$$4(hx - 1) - 3(x + h) \equiv 5(x + k)$$

Work out the values of h and k .

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$$h = \dots\dots\dots, k = \dots\dots\dots \quad (4 \text{ marks})$$

- 3 (a)** $x : y = 3 : 2$

Write x in terms of y .

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$$\text{Answer } \dots\dots\dots \quad (2 \text{ marks})$$

- 3 (b)** Use your answer to part (a) to simplify $2x + y : 3x - 2y$

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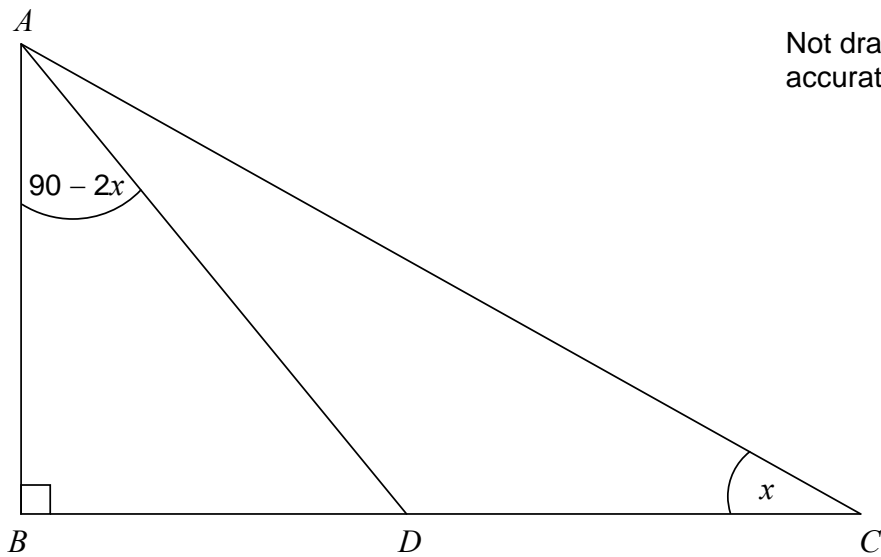
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$$\text{Answer } \dots\dots\dots \quad (2 \text{ marks})$$

4 ABC is a right-angled triangle.

$$\text{Angle } ACB = x$$

$$\text{Angle } BAD = 90 - 2x$$



Prove that ACD is an isosceles triangle.

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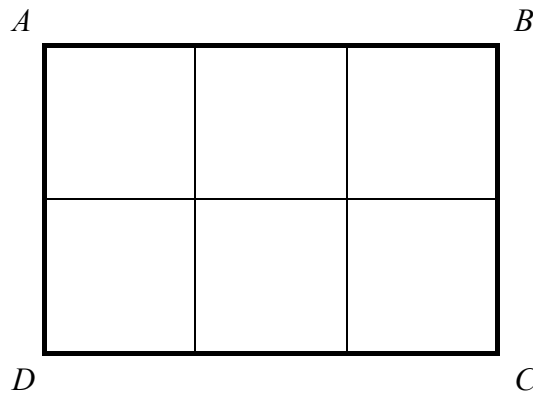
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(3 marks)

Turn over for the next question

- 5 The rectangle $ABCD$ is divided into 6 identical squares.
The side of each square is x cm.



Not drawn
accurately

When the perimeter and the area of $ABCD$ are given in cm and cm^3 respectively, they have the same numerical value.

Work out x .

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$x =$ (4 marks)

6

$$y = \frac{3x(2x^4 - 5x)}{x^2}$$

Work out $\frac{dy}{dx}$

$$\frac{dy}{dx} = \dots\dots\dots (3 \text{ marks})$$

7

Given that $\frac{2}{h} - \frac{3}{k} = 4$

show that $h = \frac{2k}{4k + 3}$

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(3 marks)

10

Turn over ►

8 Work out the gradient of the curve $y = (3x - 4)(x + 2)$ at the point $(2, 8)$

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Answer (3 marks)

10 $y = 10 - 8x - x^3$ for all values of x .

Show that y is a decreasing function for all values x .

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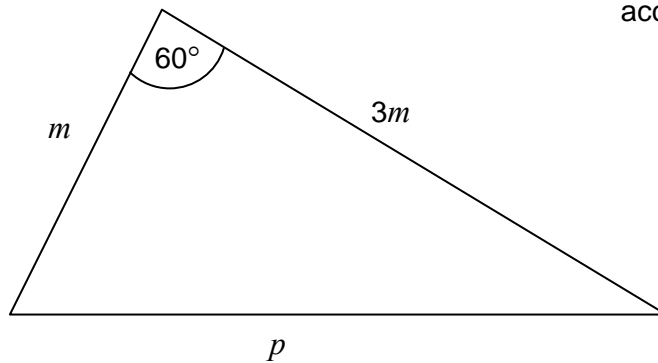
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(3 marks)

11



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accurately

Use the cosine rule to show that $p = m\sqrt{7}$

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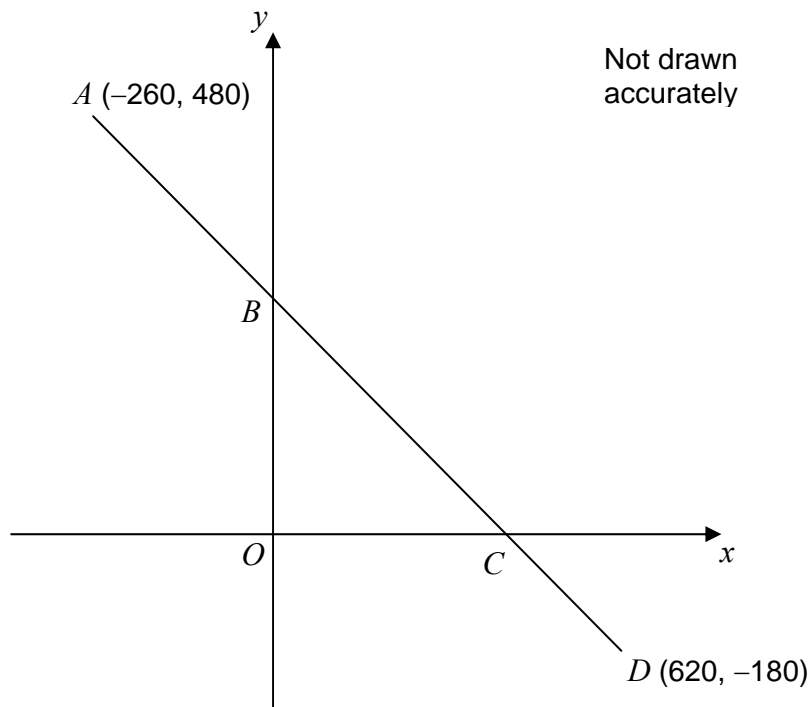
(3 marks)

12 The diagram shows a straight line $ABCD$.

A is the point $(-260, 480)$

D is the point $(620, -180)$

The line cuts the y -axis at B and the x -axis at C .



Work out the coordinates of B and C .

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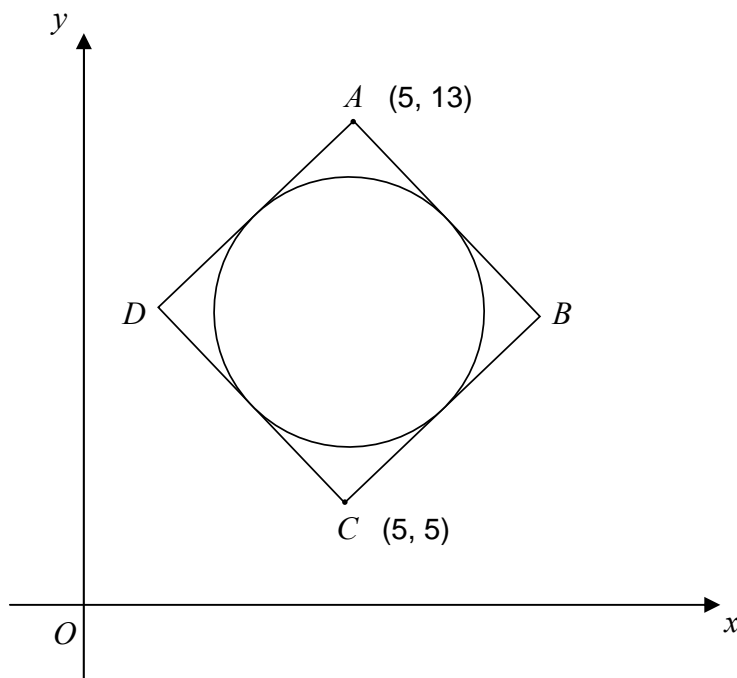
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$B = (\dots\dots\dots, \dots\dots\dots) \quad C = (\dots\dots\dots, \dots\dots\dots)$ (6 marks)

- 13** $ABCD$ is a square.
 A is the point $(5, 13)$
 C is the point $(5, 5)$

The circle touches the sides of the square.



Not drawn accurately

Work out the equation of the circle.

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Answer (5 marks)

14 (a) Show that $(x - 2)$ is a factor of $x^3 + 8x^2 + x - 42$

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(2 marks)

14 (b) Hence, or otherwise, work out **all** solutions of $x^3 - 8x^2 + x - 42 = 0$

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Answer (4 marks)

15 Rationalise the denominator and simplify $\frac{5\sqrt{5} - 2}{2\sqrt{5} - 3}$

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Answer (4 marks)

16 Prove that, for **all** values of x , $2x^2 - 8x + 9 > 0$

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(5 marks)

Turn over for the next question

$$17 \quad \begin{pmatrix} 2 & a \\ 1 & -3 \end{pmatrix} \begin{pmatrix} a \\ b \end{pmatrix} = \begin{pmatrix} -1 \\ 2 \end{pmatrix}$$

Work out **all** possible pairs of values of a and b .

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Answer (6 marks)

END OF QUESTIONS

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