

Mark Scheme

| Qn | Answer | Mk | Comment | | | | | | | | | | | | | | | | | | | | | | | | |
|------|--|---|--|-------|--------------|-----|----|---|-----|-----|----|---|-----|-----|----|----|-----|-----|----|----|-----|-----|---|----|------|---|---|
| 1 | <table border="1"> <thead> <tr> <th>Time</th> <th>freq</th> <th>width</th> <th>freq density</th> </tr> </thead> <tbody> <tr> <td>40-</td> <td>26</td> <td>5</td> <td>5.2</td> </tr> <tr> <td>45-</td> <td>18</td> <td>5</td> <td>3.6</td> </tr> <tr> <td>50-</td> <td>31</td> <td>10</td> <td>3.1</td> </tr> <tr> <td>60-</td> <td>16</td> <td>10</td> <td>1.6</td> </tr> <tr> <td>70-</td> <td>9</td> <td>20</td> <td>0.45</td> </tr> </tbody> </table> | Time | freq | width | freq density | 40- | 26 | 5 | 5.2 | 45- | 18 | 5 | 3.6 | 50- | 31 | 10 | 3.1 | 60- | 16 | 10 | 1.6 | 70- | 9 | 20 | 0.45 | <p>M1 A1</p> <p>G1 G1 G1</p> | <p>Calculation of fd's (accept values in proportion)</p> <p>Linear scales Widths of bars Heights of bars</p> |
| Time | freq | width | freq density | | | | | | | | | | | | | | | | | | | | | | | | |
| 40- | 26 | 5 | 5.2 | | | | | | | | | | | | | | | | | | | | | | | | |
| 45- | 18 | 5 | 3.6 | | | | | | | | | | | | | | | | | | | | | | | | |
| 50- | 31 | 10 | 3.1 | | | | | | | | | | | | | | | | | | | | | | | | |
| 60- | 16 | 10 | 1.6 | | | | | | | | | | | | | | | | | | | | | | | | |
| 70- | 9 | 20 | 0.45 | | | | | | | | | | | | | | | | | | | | | | | | |
| (ii) | <p>e.g. The distribution is positively skewed The mode is at the extreme left of the distribution. Accept range = 50 or median = 52</p> | <p>E1 E1</p> | | | | | | | | | | | | | | | | | | | | | | | | | |
| 2 | <p>(i) Mean = $83.95/8 = 10.49$</p> $\text{Variance} = \frac{881.2119 - \frac{83.95^2}{8}}{7}$ $= 0.03737$ <p>Standard deviation = 0.193</p> <p>(ii) 2 standard deviations below mean</p> $= 10.49 - 2(0.193)$ $= 10.104$ <p>but $10.04 < 10.104$</p> <p>so 10.04 is an outlier.</p> <p>(iii) This time is much faster than the others. This may be the result of wind assistance, faulty timing, false start and should be discarded. Opposite conclusion such as this could be a genuinely fast time, can also receive full credit.</p> | <p>B1</p> <p>M1 A1</p> <p>M1 A1</p> <p>E1 E1</p> | <p>Follow through if divisor n has been used above.</p> <p>Appreciating need for investigation Comment in context</p> | | | | | | | | | | | | | | | | | | | | | | | | |

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|------------|--|--|--|-------|-------|---|---|------------|------|-------|-------|-------|-------|--|--|
| 3 | <p>Let $P(B) = x$</p> <p>Using $P(A \cup B) = P(A) + P(B) - P(A \cap B)$</p> $0.9 = 2x + x - 0.3$ $x = 0.4$ $P(B) = 0.4$ | M1 M1 A1 | Correct set of equations Correct solution | | | | | | | | | | | | |
| 4 | <p>(i)</p> <table style="margin-left: auto; margin-right: auto;"> <tr> <td style="text-align: center;">r</td> <td style="text-align: center;">0</td> <td style="text-align: center;">1</td> <td style="text-align: center;">2</td> <td style="text-align: center;">3</td> <td style="text-align: center;">4</td> </tr> <tr> <td style="text-align: center;">$P(X = r)$</td> <td style="text-align: center;">$6k$</td> <td style="text-align: center;">$10k$</td> <td style="text-align: center;">$12k$</td> <td style="text-align: center;">$12k$</td> <td style="text-align: center;">$10k$</td> </tr> </table> $50k = 1 \rightarrow k = 1/50$ <p>(ii) $E(X) = 110k = 2.2$</p> <p>(iii) $P(X > 2.2) = 22k = 0.44$</p> | r | 0 | 1 | 2 | 3 | 4 | $P(X = r)$ | $6k$ | $10k$ | $12k$ | $12k$ | $10k$ | B1 B1 M1 M1 A1 B1 | 1 value correct all 3 correct sum of 1 sum of rp cao |
| r | 0 | 1 | 2 | 3 | 4 | | | | | | | | | | |
| $P(X = r)$ | $6k$ | $10k$ | $12k$ | $12k$ | $10k$ | | | | | | | | | | |
| 5 | <p>(i) $\binom{12}{8}$ ways of choosing forwards = 495</p> <p>(ii)</p> $\binom{12}{8} \times \binom{11}{7}$ <p>ways of choosing team</p> $= 495 \times 330 = 163350$ | M1 A1 M1 M1 A1 | Product with (i) backs cao | | | | | | | | | | | | |
| 6 | <p>(i) $P(\text{Correct forecast}) = \frac{55 + 128 + 81}{365} = \frac{264}{365}$</p> <p>(ii) $P(\text{Correct forecast given sunny forecast})$</p> $= \frac{55}{75} = 0.733$ <p>(iii) $P(\text{Correct forecast given wet weather})$</p> $= \frac{81}{117} = 0.692$ <p>(iv) $P(\text{Cloudy weather given correct forecast})$</p> $= \frac{128}{264} = 0.485$ | M1 A1 M1 A1 M1 A1 M1 A1 | Numerator Denominator Denominator Denominator | | | | | | | | | | | | |
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| 7 | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|----------------------|---|-----------|---------------------------------|------------------|-----|--------------------|------|--------------------|----|--------------------|-----|---------------------|-------|----------------------|----|-------|-----------------|----|-------|------|---|------|--|-----|-------|----|------------|
| (i) | Median distance = 88 th value = 480 | M1 | Within 5 | | | | | | | | | | | | | | | | | | | | | | | | |
| A | | A1 | cao | | | | | | | | | | | | | | | | | | | | | | | | |
| B | Lower Quartile = 44 th value = 320 | B1 | | | | | | | | | | | | | | | | | | | | | | | | | |
| | Upper Quartile = 132 nd value = 680 | B1 | | | | | | | | | | | | | | | | | | | | | | | | | |
| | Interquartile range = 680 – 320 = 360 | M1 | ft | | | | | | | | | | | | | | | | | | | | | | | | |
| (ii) | | G1 | Basic idea | | | | | | | | | | | | | | | | | | | | | | | | |
| | | G1 | Linear 0 - 1200 | | | | | | | | | | | | | | | | | | | | | | | | |
| | | G1 | Box including median (accurate) | | | | | | | | | | | | | | | | | | | | | | | | |
| (iii) | <table style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th style="text-align: left;">Distance</th> <th style="text-align: right;">Frequency</th> </tr> </thead> <tbody> <tr> <td>$0 < d \leq 200$</td> <td style="text-align: right;">20</td> </tr> <tr> <td>$200 < d \leq 400$</td> <td style="text-align: right;">44</td> </tr> <tr> <td>$400 < d \leq 600$</td> <td style="text-align: right;">54</td> </tr> <tr> <td>$600 < d \leq 800$</td> <td style="text-align: right;">32</td> </tr> <tr> <td>$800 < d \leq 1000$</td> <td style="text-align: right;">19</td> </tr> <tr> <td>$1000 < d \leq 1200$</td> <td style="text-align: right;">7</td> </tr> </tbody> </table> | Distance | Frequency | $0 < d \leq 200$ | 20 | $200 < d \leq 400$ | 44 | $400 < d \leq 600$ | 54 | $600 < d \leq 800$ | 32 | $800 < d \leq 1000$ | 19 | $1000 < d \leq 1200$ | 7 | M1 | Correct classes | | | | | | | | | | |
| Distance | Frequency | | | | | | | | | | | | | | | | | | | | | | | | | | |
| $0 < d \leq 200$ | 20 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| $200 < d \leq 400$ | 44 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| $400 < d \leq 600$ | 54 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| $600 < d \leq 800$ | 32 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| $800 < d \leq 1000$ | 19 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| $1000 < d \leq 1200$ | 7 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | M1 | Correct frequencies | | | | | | | | | | | | | | | | | | | | | | | | |
| (iv) | <table style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th style="text-align: left;">Mid (x)</th> <th style="text-align: left;">f</th> <th style="text-align: left;">fx</th> </tr> </thead> <tbody> <tr> <td>100</td> <td>20</td> <td>2000</td> </tr> <tr> <td>300</td> <td>44</td> <td>13200</td> </tr> <tr> <td>500</td> <td>54</td> <td>27000</td> </tr> <tr> <td>700</td> <td>32</td> <td>22400</td> </tr> <tr> <td>900</td> <td>19</td> <td>17100</td> </tr> <tr> <td>1100</td> <td>7</td> <td>7700</td> </tr> <tr> <td></td> <td>176</td> <td>89400</td> </tr> </tbody> </table> | Mid (x) | f | fx | 100 | 20 | 2000 | 300 | 44 | 13200 | 500 | 54 | 27000 | 700 | 32 | 22400 | 900 | 19 | 17100 | 1100 | 7 | 7700 | | 176 | 89400 | M1 | mid points |
| Mid (x) | f | fx | | | | | | | | | | | | | | | | | | | | | | | | | |
| 100 | 20 | 2000 | | | | | | | | | | | | | | | | | | | | | | | | | |
| 300 | 44 | 13200 | | | | | | | | | | | | | | | | | | | | | | | | | |
| 500 | 54 | 27000 | | | | | | | | | | | | | | | | | | | | | | | | | |
| 700 | 32 | 22400 | | | | | | | | | | | | | | | | | | | | | | | | | |
| 900 | 19 | 17100 | | | | | | | | | | | | | | | | | | | | | | | | | |
| 1100 | 7 | 7700 | | | | | | | | | | | | | | | | | | | | | | | | | |
| | 176 | 89400 | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | M1 | fx | | | | | | | | | | | | | | | | | | | | | | | | |
| | Estimate of mean = 507.95 | A1 | | | | | | | | | | | | | | | | | | | | | | | | | |
| (v) | Mid point of first class now 150 | M1 | 150 | | | | | | | | | | | | | | | | | | | | | | | | |
| | Total increase of 1000 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | New estimate of mean = 513.6 | A1 | | | | | | | | | | | | | | | | | | | | | | | | | |
| (vi) | The point (0,0) would move to (100,0) | E1 | point (0,0) | | | | | | | | | | | | | | | | | | | | | | | | |
| | | E1 | point (100,0) | | | | | | | | | | | | | | | | | | | | | | | | |
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| | | | |
|-------|---|--|---|
| 8 | Number not turning up $X \sim B(16, 0.2)$ | | |
| (i) | $P(X = 0) = 0.8^{16} = 0.0281$ | M1 A1 | 0.8^{16} or tables |
| (ii) | $P(X > 3) = 1 - P(X \leq 3)$ or $P(X \leq 12)$ $= 1 - 0.5981 = 0.4019$ | M1 M1 A1 | Manipulation Use of tables |
| (iii) | $X \sim B(17, 0.2) \rightarrow P(X \geq 1) = 0.9775$ Greater than 0.9 so acceptable | M1 A1 E1 | B(17, 0.2) 0.9775 |
| (iv) | $X \sim B(18, 0.2) \rightarrow P(X \geq 2) = 0.9009$ Can make 18 appointments $X \sim B(19, 0.2) \rightarrow P(X \geq 3) = 0.7631$ | M1 A1 A1 M1 | 18 and ≥ 2 0.9009 18 ok 19 and ≥ 3 |
| (v) | Now $X \sim B(20, p)$ Let p be probability of not turning up. $H_0: p = 0.2$ $H_1: p \neq 0.2$ $P(X \leq 1) = 0.0692 > 2.5\%$ cannot reject H_0 conclude that the proportion of patients not turning up is unchanged. | B1 B1 B1 M1 M1 A1 E1 | 0.0692 correct comparison cannot reject H_0 |