

Oxford Cambridge and RSA Examinations

Advanced Subsidiary General Certificate of Education Advanced General Certificate of Education

MEI STRUCTURED MATHEMATICS STATISTICS 2, S2

4767

MARK SCHEME

Qu	Answer	Mark	Comment
1(i)	$H_0: \rho = 0, H_1: \rho \neq 0$ [where ρ is the population correlation coefficient]	B1 B1 [2]	For H ₀ For H ₁
1(ii)	$S_{xy} = \Sigma xy - n\overline{xy} = 35\ 212.5 - 20 \times 34.55 \times 50.9 = 40.6$ $S_{xx} = \Sigma x^2 - n\overline{x}^2 = 23\ 917 - 20 \times 34.55^2 = 42.95$ $S_{yy} = \Sigma y^2 - n\overline{y}^2 = 51\ 904 - 20 \times 50.9^2 = 87.8$ $r = \frac{40.6}{\sqrt{42.95 \times 87.8}} \text{ or }$ $\frac{2.03}{\sqrt{42.95 \times 87.8}} = 0.66\ (2.8.5.)$		S_{xy} or covariance S_{xx} S_{yy} Structure of r cao
	$\sqrt{2.1475}\sqrt{4.39}$ For $n = 20$, 1% critical value = 0.5614 Since 0.5614 < 0.661 we reject H ₀ :	M1,A1 M1	Critical value Comparison
	There is sufficient evidence at the 1% significance level to suggest there is correlation between head circumferences and lengths of babies. Background population is <i>bivariate Normal</i> .	A1 E1 [10]	Conclusion in words in context Explanation
1(iii)	$\sum x = 708, \qquad \sum y = 1001,$ $\sum x^2 = 25 \ 362, \qquad \sum y^2 = 50 \ 459,$ $n = 20, \qquad \sum xy = 35 \ 212.5$ $\Rightarrow S_{xy} = -222.9 \text{ and so } \rho < 0.$		All 6 correct (B2 for any 4 correct, B1 for any 2 correct)
1(iv)	The incorrect pair produce an <i>extreme</i> point to the <i>right</i>	E1	Extreme point
	<i>ana</i> <i>below</i> existing cluster, producing a negative correlation. (Or There will be a large change in the summary statistics, which will make the covariance negative.)		Relative position For large change For negative cov
		[2]	1 of nogative cov.

2(i) B1 Correct overall shat 5% 19% 4000 5000 2(ii) $P(X > 5000) = 0.19 \Rightarrow 5000 = \mu + 0.8779\sigma$ $P(X < 4000) = 0.05 \Rightarrow 4000 = \mu - 1.645\sigma$ Solving: $1000 = 2.523\sigma$ $\Rightarrow \sigma = \frac{1000}{2.523} = 396$ (3 s.f.) Hence: $\mu = 4000 + 1.645 \times 396 = 4650$ (3 s.f.) P(4250 < X < 4750) = P(-1 < Z < 0.25) $= 0.4400$	
2(ii) $P(X > 5000) = 0.19 \Rightarrow 5000 = \mu + 0.8779\sigma$ $P(X < 4000) = 0.05 \Rightarrow 4000 = \mu - 1.645\sigma$ Solving: $1000 = 2.523\sigma$ $\Rightarrow \sigma = \frac{1000}{2.523} = 396$ (3 s.f.) B1 M1 Both z-values Attempt at one equ z-value M1 Attempt at finding B1 A1 [5] 2(iii) $P(4250 < X < 4750) = P(-1 < Z < 0.25)$ = 0.5987 - (1 - 0.8413) = 0.4400 M1 Standardisations Probability calcula (a)	ape
2(ii) $P(X > 5000) = 0.19 \Rightarrow 5000 = \mu + 0.8779\sigma$ $P(X < 4000) = 0.05 \Rightarrow 4000 = \mu - 1.645\sigma$ Solving: $1000 = 2.523\sigma$ $\Rightarrow \sigma = \frac{1000}{2.523} = 396 (3 \text{ s.f.})$ B1 M1 Attempt at one equ z -valueM1Attempt at finding B1 σ A1 μ 2(iii) $P(4250 < X < 4750) = P(-1 < Z < 0.25)$ $= 0.5987 - (1 - 0.8413)$ $= 0.4400$ M1 Standardisations M1 A1 μ	right-hand e left-hand
2(ii) $P(X > 5000) = 0.19 \Rightarrow 5000 = \mu + 0.8779\sigma$ B1 Both z-values $P(X < 4000) = 0.05 \Rightarrow 4000 = \mu - 1.645\sigma$ M1 Attempt at one equal $Solving: 1000 = 2.523\sigma$ M1 Attempt at finding $\Rightarrow \sigma = \frac{1000}{2.523} = 396$ (3 s.f.) M1 Attempt at finding Hence: $\mu = 4000 + 1.645 \times 396 = 4650$ (3 s.f.) M1 Attempt at finding $P(4250 < X < 4750) = P(-1 < Z < 0.25)$ M1 Standardisations $= 0.5987 - (1 - 0.8413)$ M1 Standardisations $= 0.4400$ A1 cao	
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Solving: $1000 = 2.523\sigma$ $\Rightarrow \sigma = \frac{1000}{2.523} = 396 (3 \text{ s.f.})$ Hence: $\mu = 4000 + 1.645 \times 396 = 4650 (3 \text{ s.f.})$ 2(iii) $P(4250 < X < 4750) = P(-1 < Z < 0.25)$ = 0.5987 - (1 - 0.8413) = 0.4400 X = 0.4400 X = 0.5987 - (1 - 0.8413) = 0.4400	uation with
$\Rightarrow \sigma = \frac{1000}{2.523} = 396 (3 \text{ s.f.})$ Hence: $\mu = 4000 + 1.645 \times 396 = 4650 (3 \text{ s.f.})$ $M1 = B1 = \sigma$ A1 = [5] $M1 = [5]$ $P(4250 < X < 4750) = P(-1 < Z < 0.25)$ $= 0.5987 - (1 - 0.8413)$ $= 0.4400$ $M1 = P(-1 < Z < 0.25)$ $M1 = P(-1 < Z <$	
2.325 Hence: $\mu = 4000 + 1.645 \times 396 = 4650 \ (3 \text{ s.f.})$ $B1 \qquad A1 \qquad \mu$ $[5]$ $P(4250 < X < 4750) = P(-1 < Z < 0.25)$ $= 0.5987 - (1 - 0.8413)$ $= 0.4400$ $M1 \qquad \text{Standardisations}$ $M1 \qquad \text{Probability calcula}$ $A1 \qquad \text{cao}$ $[3]$	$,\sigma$
Hence: $\mu = 4000 + 1.645 \times 396 = 4650$ (3 s.f.) A1 μ 2(iii) P(4250 < X < 4750) = P(-1 < Z < 0.25) M1 Standardisations $= 0.5987 - (1 - 0.8413)$ M1 Probability calcula $= 0.4400$ A1 cao	
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= 0.5987 - (1 - 0.8413) $= 0.4400$ M1 Probability calcula cao [3]	
= 0.4400 A1 cao [3]	ations
2(iv) $P(X > 5450) = P(Z > 2)$ B1 cao	
=1-0.9772 = 0.0228	
2(v) $P(Z > -2.326) = 0.99$ B1 ± 2.326	
$\Rightarrow x = 4650 - 2.326 \times 400 = 3719.6$ M1 Calculation	
hence should quote 3700 hoursA1cao	
[3]	
2(vi)P(0 or 1 bulbs need replacing) = 0.8413 ⁶ + 6×0.8413 ⁵ × 0.1587 = 0.76 (2 s.f.)M1 M1,A1 A1 [4]0 or 1 Sum of 2 terms cao	

Qu	Answer	Mark	Comment
3(i)(A)	$P(X \ge 2) = 1 - P(X \le 1)$ = 1 - e ^{-1.63} (1+1.63) = 1 - 0.515 = 0.485 (3 s.f.)	M1 M1,A1 A1 [4]	Sum of 2 probs. 1 – sum of 2 probs.
3(i)(<i>B</i>)	$P(X = 1) \times P(Y = 1)$ = (e ^{-1.63} ×1.63)×(e ^{-1.17} ×1.17) = 0.116 (3 s.f.)	M1 M1 A1 [3]	2 probabilities Product
3(i)(C)	Using $\lambda = 1.63 + 1.17 = 2.8$: P(X + Y = 5) = 0.9349 - 0.8477 = 0.087 (2 s.f.) (or P(X + Y = 5) = e ^{-2.8} × $\frac{2.8^5}{5!}$ = 0.087 (2 s.f.))	M1,A1 M1 A1 [4]	$\lambda = 2.8$ For calculation cao
3(ii)	Two reasons why proposed model might not be suitable: Poisson parameter unlikely to be same for each team; lack of independence between the variables.	E1 E1 [2]	For one reason For second reason
3(iii)	$\lambda = 19 \times 1.63 = 30.97$, hence suitable approximating distribution is N(30.97, 30.97) P(more than 35 goals in a season) = P(X > 35.5) = P(Z > $\frac{35.5 - 30.97}{\sqrt{30.97}})$ = P(Z > 0.814) = 1-0.792 = 0.208 (3 s.f.)	M1,A1 B1 M1 A1 [5]	Use of Normal approx. Continuity corr. Calculation

Qu	Answer	Mark	Comment	
4(a)(i)	$H_1: \mu < 40.5$	B1 [1]	Hypothesis	
4(a)(ii)	$n = 12, \sum x = 485.4 \Longrightarrow \overline{x} = 40.45$	M1,A1	Mean value	
	Test statistic is $\frac{40.45 - 40.5}{\frac{0.2}{\sqrt{12}}} = -0.866$	M1 M1 A1	Numerator Denominator	
	Since $-0.866 > -1.645$, the result is not significant, and it is reasonable to accept that $\mu = 40.5$	B1 M1 A1 [8]	'1.645' Comparison Conclusion in words	
4(b)	H_0 : There is no association between inoculation and the occurrence of influenza H_1 : There is an association between inoculation and the occurrence of influenza	B1 B1		
	Expected frequencies:	M1,A1	Expected frequencies	
	Influenza Total Yes No Total Inoculated Yes 14.333 11.667 26 No 28.667 23.333 52 Totals 43 35 78			
	$\frac{(8-14.333)^2}{14.333} + \frac{(18-11.667)^2}{11.667} + \frac{(35-28.667)^2}{28.667} + \frac{(17-23.333)^2}{23.333}$ = 9.35 (3 s.f.)	M1 A1	Calculation of the test statistics cao	
	Since $9.35 > 3.84$, the result is significant, and therefore it seems there is association between incidence of inoculation and influenza	B1 M1 A1 [9]	3.84 Comparison Conclusion in words	
			Total: 72	

AO	Range	Total	Question Number				
			1	2	3	4	
1	14-22	15	7	1	2	5	
2	14-22	16	2	6	4	4	
3	18-26	20	5	9	5	1	
4	7-15	12	2	-	4	6	
5	3-11	9	2	2	3	2	
	Totals	72	18	18	18	18	