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General Certificate of Education Advanced Subsidiary Examination January 2011

# **Mathematics**

MM1B

**Unit Mechanics 1B** 

Wednesday 19 January 2011 1.30 pm to 3.00 pm

#### For this paper you must have:

• the blue AQA booklet of formulae and statistical tables. You may use a graphics calculator.

#### Time allowed

1 hour 30 minutes

### Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer all questions.
- Write the question part reference (eg (a), (b)(i) etc) in the left-hand margin.
- You must answer the questions in the spaces provided. Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost
- Do all rough work in this book. Cross through any work that you do not want to be marked.
- The **final** answer to questions requiring the use of calculators should be given to three significant figures, unless stated otherwise.
- Take  $g = 9.8 \text{ m s}^{-2}$ , unless stated otherwise.

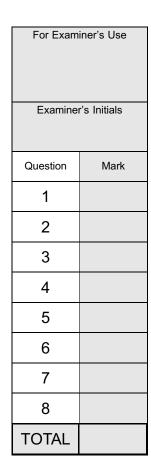
#### Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 75.
- Unit Mechanics 1B has a written paper only.

## Advice

 Unless stated otherwise, you may quote formulae, without proof, from the booklet.





Answer all questions in the spaces provided.				
1	A trolley, of mass 5 kg, is moving in a straight line on a smooth horizontal surface. It has a velocity of $6 \mathrm{ms^{-1}}$ when it collides with a stationary trolley, of mass $m\mathrm{kg}$ . Immediately after the collision, the trolleys move together with velocity $2.4 \mathrm{ms^{-1}}$ .			
	Find m. (3 marks)			
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2 The graph shows how the velocity of a train varies as it moves along a straight railway line.

Velocity (m s<sup>-1</sup>)

(a) Find the total distance travelled by the train. (4 marks)

30

40

Time (seconds)

20

10

- (b) Find the average speed of the train. (2 marks)
- (c) Find the acceleration of the train during the first 10 seconds of its motion. (2 marks)
- (d) The mass of the train is 200 tonnes. Find the magnitude of the resultant force acting on the train during the first 10 seconds of its motion. (2 marks)

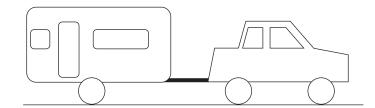
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A car, of mass 1200 kg, tows a caravan, of mass 1000 kg, along a straight horizontal road. The caravan is attached to the car by a horizontal tow bar, as shown in the diagram.



Assume that a constant resistance force of magnitude 200 newtons acts on the car and a constant resistance force of magnitude 300 newtons acts on the caravan. A constant driving force of magnitude P newtons acts on the car in the direction of motion. The car and caravan accelerate at  $0.8 \, \mathrm{m \, s^{-2}}$ .

- (a) (i) Find *P*. (3 marks)
  - (ii) Find the magnitude of the force in the tow bar that connects the car to the caravan.

    (3 marks)
- (b) (i) Find the time that it takes for the speed of the car and caravan to increase from  $7 \,\mathrm{m\,s^{-1}}$  to  $15 \,\mathrm{m\,s^{-1}}$ .
  - (ii) Find the distance that they travel in this time. (3 marks)
- (c) Explain why the assumption that the resistance forces are constant is unrealistic.

  (1 mark)

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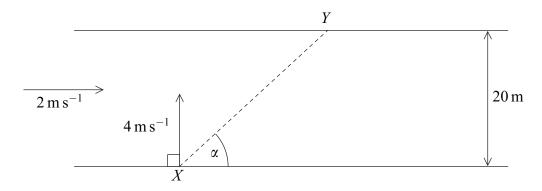
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A canoe is paddled across a river which has a width of 20 metres. The canoe moves from the point X on one bank of the river to the point Y on the other bank, so that its path is a straight line at an angle  $\alpha$  to the banks. The velocity of the canoe relative to the water is  $4 \text{ m s}^{-1}$  perpendicular to the banks. The water flows at  $2 \text{ m s}^{-1}$  parallel to the banks.



Model the canoe as a particle.

- (a) Find the magnitude of the resultant velocity of the canoe. (2 marks)
- (b) Find the angle  $\alpha$ . (2 marks)
- (c) Find the time that it takes for the canoe to travel from X to Y. (2 marks)

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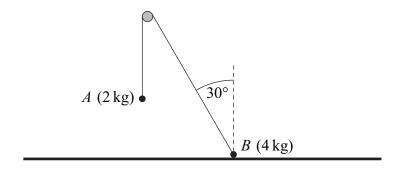
5		A particle moves with constant acceleration $(-0.4\mathbf{i}+0.2\mathbf{j})\mathrm{ms^{-2}}$ . Initially, it has velocity $(4\mathbf{i}+0.5\mathbf{j})\mathrm{ms^{-1}}$ . The unit vectors $\mathbf{i}$ and $\mathbf{j}$ are directed east and north respectively.				
(a	)	Find an expression for the velocity of the particle at time $t$ seconds.	(2 marks)			
(b	) (i)	Find the velocity of the particle when $t = 22.5$ .	(2 marks)			
	(ii)	State the direction in which the particle is travelling at this time.	(1 mark)			
(с	)	Find the time when the speed of the particle is $5 \mathrm{ms^{-1}}$ .	(6 marks)			
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Two particles, A and B, are connected by a light inextensible string which passes over a smooth peg. Particle A has mass 2 kg and particle B has mass 4 kg. Particle A hangs freely with the string vertical. Particle B is at rest in equilibrium on a rough horizontal surface with the string at an angle of 30° to the vertical. The particles, peg and string are shown in the diagram.



- (a) By considering particle A, find the tension in the string. (2 marks)
- (b) Draw a diagram to show the forces acting on particle B. (2 marks)
- Show that the magnitude of the normal reaction force acting on particle *B* is 22.2 newtons, correct to three significant figures. (3 marks)
- (d) Find the least possible value of the coefficient of friction between particle B and the surface. (4 marks)

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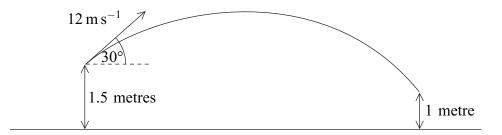
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An arrow is fired from a point at a height of 1.5 metres above horizontal ground. It has an initial velocity of  $12 \,\mathrm{m\,s^{-1}}$  at an angle of  $30^\circ$  above the horizontal. The arrow hits a target at a height of 1 metre above horizontal ground. The path of the arrow is shown in the diagram.



Model the arrow as a particle.

- (a) Show that the time taken for the arrow to travel to the target is 1.30 seconds, correct to three significant figures. (5 marks)
- (b) Find the horizontal distance between the point where the arrow is fired and the target. (2 marks)
- (c) Find the speed of the arrow when it hits the target. (4 marks)
- (d) Find the angle between the velocity of the arrow and the horizontal when the arrow hits the target. (2 marks)
- (e) State one assumption that you have made about the forces acting on the arrow.

  (1 mark)

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8	A van, of mass 2000 kg, is towed up a slope inclined at $5^{\circ}$ to the h tow rope is at an angle of $12^{\circ}$ to the slope. The motion of the van resistance force of magnitude 500 newtons. The van is accelerating at $0.6 \mathrm{ms^{-2}}$ .	is opposed by a
	5°	
	Model the van as a particle.	
(a)	Draw a diagram to show the forces acting on the van.	(2 marks)
(b)	Show that the tension in the tow rope is 3480 newtons, correct to tingures.	hree significant (5 marks)
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