4762

Q 1		mark		Sub
(a) (i)	240 i N s \rightarrow	B1		1
(ii) (A)	240 i = 70 i +50 v so v = 3.4 i m s ⁻¹	M1 A1	Equating to their 240 i in this part FT 240 i	
(B)	240 i = 70 <i>u</i> i – 50 <i>u</i> i	M1	Must have <i>u</i> in both RHS terms and opposite signs	
	$u = 12$ so $\mathbf{v} = -12 \mathbf{i} \mathrm{m s^{-1}}$	A1	FT 240 i	
(C)	240 $\mathbf{i} = 280(\mathbf{i} + \mathbf{j}) + 50\mathbf{v}_{B}$	M1	FT 240 i Must have all terms present	
	so $\mathbf{v}_{\rm B} = (-0.8 \mathbf{i} - 5.6 \mathbf{j}) \mathrm{m s^{-1}}$	A1	cao	6
(b) (i)	before 4 m s^{-1} 2 m s^{-1} after v_1 v_2 v_2 v_2 v_2			
	NEL $\frac{v_2 - v_1}{-2 - 4} = -0.5$ so $v_2 - v_1 = 3$ PCLM $8 - 6 = 2v_1 + 3v_2$ Solving $v_2 = 1.6$ so $1.6 \text{ m s}^{-1} \rightarrow v_1 = -1.4$ so $1.4 \text{ m s}^{-1} \leftarrow 0.5$	M1 A1 A1 A1 A1 A1	NEL Any form PCLM Any form Direction must be clear (accept diagram) Direction must be clear (accept diagram). [Award A1 A0 if $v_1 & v_2$ correct but directions not clear]	6
(ii)	1.6 m s ^{-1} at 60° to the wall (glancing angles both 60°) No change in the velocity component parallel	B1 B1 E1	FT their 1.6 Must give reason	
	to the wall as no impulse No change in the velocity component perpendicular to the wall as perfectly elastic	E1	Must give reason	4
	total	17		-

4762

Mark Scheme

Q 2		mark		Sub
(i)	We need $\frac{mgh}{t} = \frac{850 \times 9.8 \times 60}{20} = 24990$	M1	Use of $\frac{mgh}{t}$	
	so approx 25 kW	E1	Shown	2
(ii)	Driving force – resistance = 0 25000 = 800v so $v = 31.25$ and speed is 31.25 m s ⁻¹	B1 M1 A1	May be implied Use of $P = Fv$	3
(iii)	Force is $\frac{25000}{10} = 2500$ N	B1		
	N2L in direction of motion 2500 - 800 = 850a $a = 2 \text{ so } 2 \text{ m s}^{-2}$	M1 A1	Use of N2L with all terms	3
(iv)	$0.5 \times 850 \times 20^{2} = 0.5 \times 850 \times 15^{2}$ +25000 × 6.90 -800 x x = 122.6562 so 123 m (3 s. f.)	M1 B1 B1 B1 A1 A1	W-E equation with KE and power term One KE term correct Use of <i>Pt</i> .Accept wrong sign WD against resistance. Accept wrong sign All correct cao	6
(v)	either $0.5 \times 850 \times v^2 = 0.5 \times 850 \times 20^2$	M1	W-E equation inc KE, GPE and WD	
	$-850\times9.8\times\frac{105}{20}$	M1 A1	GPE term with attempt at resolution Correct. Accept expression. Condone wrong sign.	
	-800×105	B1	WD term. Neglect sign.	
	$v^2 = 99.452$ so 9.97 m s ⁻¹ or N2L + ve up plane	A1	сао	
	$-(800+850g\times0.05) = 850a$ a = -1.43117	M1 A1	N2L. All terms present. Allow sign errors. Accept \pm	
	$v^2 = 20^2 + 2 \times (-1.43117) \times 105$	M1 A1	Appropriate <i>uvast</i> . Neglect signs. All correct including consistent signs. Need not follow sign of <i>a</i> above.	
	$v^2 = 99.452$ so 9.97 m s ⁻¹	A1	cao	5
		19		

Q 3		mark		Sub
(i)	$28\left(\frac{\overline{x}}{\overline{y}}\right) = 16\left(\frac{2}{2}\right) + 2\left(\frac{5}{0}\right) + 2\left(\frac{6}{1}\right) + 2\left(\frac{5}{2}\right)$ $+ 2\left(\frac{0}{5}\right) + 2\left(\frac{1}{6}\right) + 2\left(\frac{2}{5}\right)$ $\overline{x} = 2.5$ $\overline{y} = 2.5$	M1 B1 B1 A1 A1	Complete method Total mass correct 3 c. m. correct (or 4 <i>x</i> - or <i>y</i> -values correct) [Allow A0 A1 if only error is in total mass] [If $\overline{x} = \overline{y}$ claimed by symmetry and only one component worked replace final A1, A1 by B1 explicit claim of symmetry A1 for the 2.5]	5
(ii)	$\overline{x} = \overline{y}$ $28\overline{x} = 16 \times 2 + 6 \times 4 + 2 \times 0 + 2 \times 1 + 2 \times 2$ $\overline{x} = \frac{31}{14} (2.21428)$ $\overline{z} = \frac{8 \times (-1) + 4 \times (-2)}{28} = -\frac{4}{7} (-0.57142)$	B1 M1 A1 A1 A1 A1	Or by direct calculation Dealing with 'folded' parts for \overline{x} or for \overline{z} At least 3 terms correct for \overline{x} All terms correct allowing sign errors	
	Distance is $\sqrt{\left(\frac{31}{14}\right)^2 + \left(\frac{31}{14}\right)^2 + \left(\frac{4}{7}\right)^2}$ = 3.18318 so 3.18 m (3 s. f.)	M1 F1	Use of Pythagoras in 3D on their c.m.	8
(iii)	A 3.18318 centre of mass	M1 B1	c.m. clearly directly below A Diagram showing α and known lengths (or equivalent). FT their values. Award if final answer follows their values.	
	$\sin \alpha = \frac{4}{7}/3.18318$ so $\alpha = 10.3415$ so 10.3° (3 s. f.)	M1 A1	Appropriate expression for α . FT their values. cao	4
	total	17		

Mark Scheme

Q 4		mark		Sub
(a) (i)	Moments c.w. about A 2R = 5L so $R = 2.5LResolve \rightarrow U = 0Resolve \uparrow V + R = Lso V = -1.5L$	E1 E1 M1 E1	Resolve vertically or take moments about B (or C)	
				4
(ii)	$A \xrightarrow{45^{\circ}} T_{AC}$ $1.5 L \xrightarrow{45^{\circ}} T_{AB}$	M1	Equilibrium at a pin-joint	
	For equilibrium at A	M1	Attempt at equilibrium at A or C including resolution with correct angle	
	$\uparrow T_{AB} \cos 45 + 1.5L = 0$ so $T_{AB} = -\frac{3\sqrt{2}L}{2}$ so $\frac{3\sqrt{2}L}{2}$ N (C) in AB $\rightarrow T_{AC} + T_{AB} \cos 45 = 0$	A1	(2.12 <i>L</i> (3 s. f.))	
	so $T_{AC} = \frac{3L}{2}$ so $\frac{3L}{2}$ N (T) in AC	F1	(1.5 <i>L</i>)	
	At C \downarrow $L + T_{\rm BC} \cos \theta = 0$	M1	Must include attempt at angle	
	$\tan\theta = 3/2 \Longrightarrow \cos\theta = 2/\sqrt{13}$	B1		
	so $T_{\rm BC} = -\frac{\sqrt{13}L}{2}$ so $\frac{\sqrt{13}L}{2}$ N (C) in BC	A1	(1.80 <i>L</i> (3 s. f.))	
		F1	Award for T/C correct from their internal forces. Do not award without calcs	8
(b) (i)	$ \begin{array}{c} F \\ A \\ W \\ W \\ B \\ \theta \\ \end{array} $	B1	All forces present with arrows and labels. Angles and distances not required.	1
(ii)	c.w.moments about B $R \times 3 - W \times 1 \cos \theta = 0$	M1 A1	If moments about other than B, then need to resolve perp to plank as well Correct	
	so $R = \frac{1}{3}W\cos\theta$	A1		3
(iii)	Resolve parallel to plank $F = W \sin \theta$ $F = W \sin \theta$	B1		
	$\mu = \frac{F}{R} = \frac{W\sin\theta}{\frac{1}{3}W\cos\theta} = 3\tan\theta$	M1	Use of $F = \mu R$ and their F and R	
		A1	Accept any form.	3
	total	19		