

1. Find

$$\int \left(6x^2 + \frac{2}{x^2} + 5 \right) dx$$

giving each term in its simplest form.

(4)

Q1

(Total 4 marks)



5. A sequence of numbers $a_1, a_2, a_3 \dots$ is defined by

$$a_1 = 3$$

$$a_{n+1} = 2a_n - c \quad (n \geq 1)$$

where c is a constant.

(a) Write down an expression, in terms of c , for a_2 (1)

(b) Show that $a_3 = 12 - 3c$ (2)

Given that $\sum_{i=1}^4 a_i \geq 23$

(c) find the range of values of c . (4)



6. A boy saves some money over a period of 60 weeks. He saves 10p in week 1, 15p in week 2, 20p in week 3 and so on until week 60. His weekly savings form an arithmetic sequence.

(a) Find how much he saves in week 15 **(2)**

(b) Calculate the total amount he saves over the 60 week period. **(3)**

The boy's sister also saves some money each week over a period of m weeks. She saves 10p in week 1, 20p in week 2, 30p in week 3 and so on so that her weekly savings form an arithmetic sequence. She saves a total of £63 in the m weeks.

(c) Show that

$$m(m + 1) = 35 \times 36 \quad \text{(4)}$$

(d) Hence write down the value of m . **(1)**



Question 6 continued

Lined area for writing the answer to Question 6. The area consists of 30 horizontal lines.



7. The point $P(4, -1)$ lies on the curve C with equation $y = f(x)$, $x > 0$, and

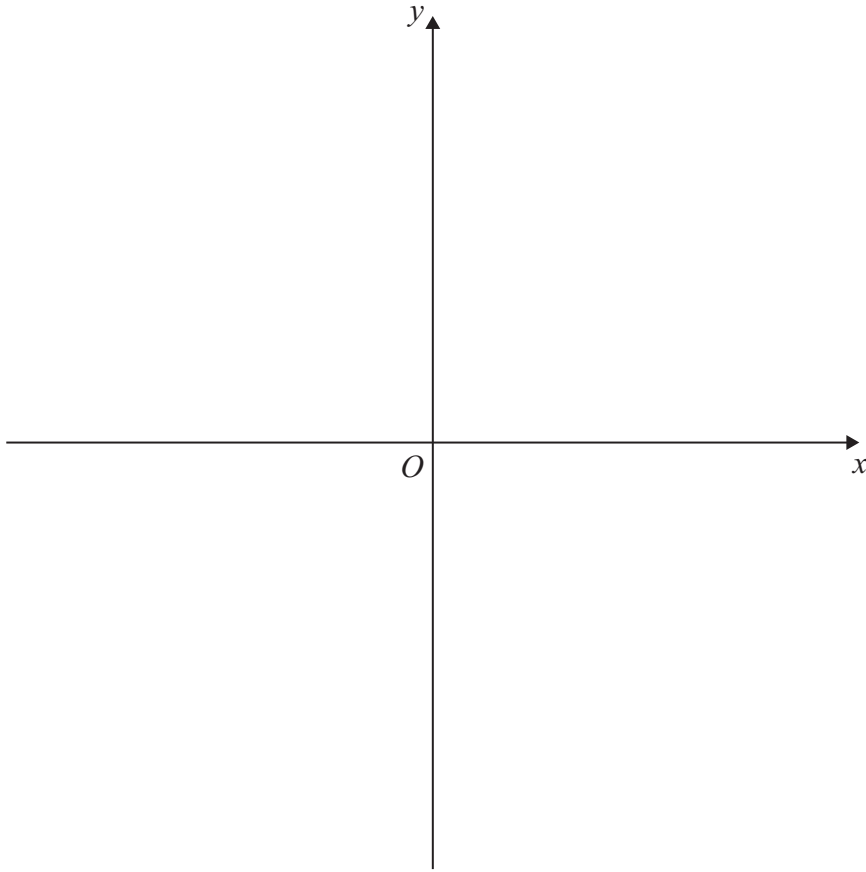
$$f'(x) = \frac{1}{2}x - \frac{6}{\sqrt{x}} + 3$$

(a) Find the equation of the tangent to C at the point P , giving your answer in the form $y = mx + c$, where m and c are integers. (4)

(b) Find $f(x)$. (4)



Question 8 continued



A series of 18 horizontal lines provided for writing the answer to the question.

(Total 8 marks)

Q8



9. The line L_1 has equation $4y + 3 = 2x$

The point $A (p, 4)$ lies on L_1

(a) Find the value of the constant p .

(1)

The line L_2 passes through the point $C (2, 4)$ and is perpendicular to L_1

(b) Find an equation for L_2 giving your answer in the form $ax + by + c = 0$, where a, b and c are integers.

(5)

The line L_1 and the line L_2 intersect at the point D .

(c) Find the coordinates of the point D .

(3)

(d) Show that the length of CD is $\frac{3}{2}\sqrt{5}$

(3)

A point B lies on L_1 and the length of $AB = \sqrt{80}$

The point E lies on L_2 such that the length of the line $CDE = 3$ times the length of CD .

(e) Find the area of the quadrilateral $ACBE$.

(3)



10.

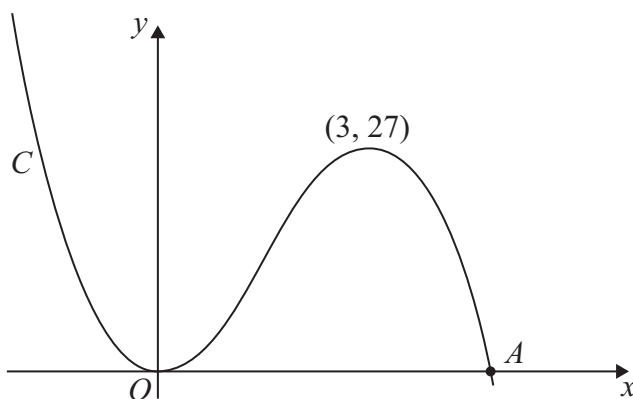


Figure 1

Figure 1 shows a sketch of the curve C with equation $y = f(x)$ where

$$f(x) = x^2(9 - 2x)$$

There is a minimum at the origin, a maximum at the point $(3, 27)$ and C cuts the x -axis at the point A .

(a) Write down the coordinates of the point A . (1)

(b) On separate diagrams sketch the curve with equation

(i) $y = f(x + 3)$

(ii) $y = f(3x)$

On each sketch you should indicate clearly the coordinates of the maximum point and any points where the curves cross or meet the coordinate axes. (6)

The curve with equation $y = f(x) + k$, where k is a constant, has a maximum point at $(3, 10)$.

(c) Write down the value of k . (1)



