Centre Number			Candidate Number		
Surname					
Other Names					
Candidate Signature					



General Certificate of Education Advanced Subsidiary Examination June 2014

# **Mathematics**

MPC2

Unit Pure Core 2

Thursday 22 May 2014 9.00 am to 10.30 am

#### For this paper you must have:

• the blue AQA booklet of formulae and statistical tables. You may use a graphics calculator.

#### Time allowed

• 1 hour 30 minutes

#### Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer all questions.
- Write the question part reference (eg (a), (b)(i) etc) in the left-hand margin.
- You must answer each question in the space provided for that question. If you require extra space, use an AQA supplementary answer book; do not use the space provided for a different question.
- Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

### Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 75.

#### **Advice**

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.

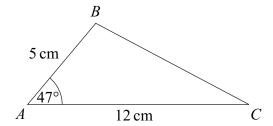
	iner's Use
Examine	r's Initials
Question	Mark
1	
2	
3	
4	
5	
6	
7	
8	
9	
TOTAL	



## Answer all questions.

Answer each question in the space provided for that question.

**1** The diagram shows a triangle ABC.



The size of angle BAC is  $47^{\circ}$  and the lengths of AB and AC are  $5~\rm cm$  and  $12~\rm cm$  respectively.

- (a) Calculate the area of the triangle ABC, giving your answer to the nearest  $cm^2$ . [2 marks]
- (b) Calculate the length of BC, giving your answer, in cm, to one decimal place. [3 marks]

QUESTION PART REFERENCE	Answer space for question 1



QUESTION PART REFERENCE	Answer space for question 1



<b>2 (a)</b> Find $\int \left(1 + 3x^{\frac{1}{2}} + x^{\frac{3}{2}}\right) dx$ .	2 (a)	Find	$\int \left(1 + \right)$	$-3x^{\frac{1}{2}} + x^{\frac{3}{2}}$	$\int dx$ .
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[3 marks]

**(b) (i)** The expression  $(1+y)^3$  can be written in the form  $1+3y+ny^2+y^3$ . Write down the value of the constant n.

[1 mark]

(ii) Hence, or otherwise, expand  $(1+\sqrt{x})^3$ .

[1 mark]

(c) Hence find the exact value of  $\int_0^1 (1+\sqrt{x})^3 dx$ .

[3 marks]

QUESTION PART REFERENCE	Answer space for question 2



QUESTION PART REFERENCE	Answer space for question 2



3		The first term of a geometric series is 54 and the common ratio of the series is $\frac{\delta}{9}$ .
(a	)	Find the sum to infinity of the series.  [2 marks]
(b	)	Find the second term of the series.  [1 mark]
(с	)	Show that the 12th term of the series can be written in the form $\frac{2^p}{3^q}$ , where $p$ and $q$ are integers.
		are integers.  [3 marks]
QUESTION PART REFERENCE	Ans	wer space for question 3



QUESTION PART REFERENCE	Answer space for question 3



4	A curve has equation	$y = \frac{1}{x^2} + 4x.$
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(a) Find  $\frac{\mathrm{d}y}{\mathrm{d}x}$ .

[3 marks]

(b) The point P(-1, -3) lies on the curve. Find an equation of the normal to the curve at the point P.

[3 marks]

(c) Find an equation of the tangent to the curve that is parallel to the line y = -12x.

[5 marks]

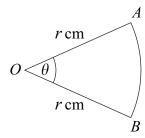
QUESTION PART REFERENCE	Answer space for question 4



QUESTION PART REFERENCE	Answer space for question 4



5 The diagram shows a sector OAB of a circle with centre O and radius  $r \, \mathrm{cm}$ .



The angle AOB is  $\theta$  radians.

The area of the sector is  $12 \, \text{cm}^2$ .

The perimeter of the sector is four times the length of the arc AB.

Find the value of r.

[6 marks]

QUESTION PART REFERENCE	Answer space for question 5



QUESTION PART REFERENCE	Answer space for question 5



6 (a) Sketch, on the axes given below, the graph of  $y = \sin x$  for  $0^{\circ} \leqslant x \leqslant 360^{\circ}$ .

[2 marks]

Describe the geometrical transformation that maps the graph of  $y = \sin x$  onto the (b) graph of  $y = \sin 5x$ .

[2 marks]

Describe the single geometrical transformation that maps the graph of  $y = \sin 5x$  onto (c) the graph of  $y = \sin(5x + 10^\circ)$ .

[2 marks]

QUESTION PART REFERENCE	Answer	space fo	r question 6				
(a)							
, ,	$\mathcal{Y}$	<b>^</b>					
	O		000	1000	2700	2600	X
			90°	180°	270°	360°	
						•••••	



QUESTION PART REFERENCE	Answer space for question 6



7 (a)	Given that	$\frac{\cos^2 x + 4\sin^2 x}{\cos^2 x + 2\sin^2 x} = 7$ , show that $\tan^2 x = 1$	3
i (a)	Given that	$1-\sin^2 x$	2 .

[3 marks]

(b) Hence solve the equation  $\frac{\cos^2 2\theta + 4\sin^2 2\theta}{1 - \sin^2 2\theta} = 7$  in the interval  $0^\circ < \theta < 180^\circ$ , giving your values of  $\theta$  to the nearest degree.

[4 marks]

QUESTION PART REFERENCE	Answer space for question 7



QUESTION PART REFERENCE	Answer space for question 7



8		An arithmetic series has first term $\boldsymbol{a}$ and common difference $\boldsymbol{d}$ .	
		The sum of the first 5 terms of the series is 575.	
(a	)	Show that $a + 2d = 115$ .	[3 marks]
(b	)	Given also that the $10 \mathrm{th}$ term of the series is $87$ , find the value of $d$ .	[3 marks]
(с	:)	The $n$ th term of the series is $u_n$ . Given that $u_k>0$ and $u_{k+1}<0$ , find the of $\sum\limits_{n=1}^k u_n$ .	value
		n=1	[5 marks]
QUESTION PART REFERENCE	Ans	wer space for question 8	
	1		



QUESTION PART REFERENCE	Answer space for question 8



- **9** A curve has equation  $y = 3 \times 12^x$ .
  - (a) The point (k, 6) lies on the curve  $y = 3 \times 12^x$ . Use logarithms to find the value of k, giving your answer to three significant figures.

[3 marks]

(b) Use the trapezium rule with four ordinates (three strips) to find an approximate value for  $\int_0^{1.5} 3 \times 12^x \, dx$ , giving your answer to two significant figures.

[4 marks]

(c) The curve  $y=3\times 12^x$  is translated by the vector  $\begin{bmatrix} 1\\p\end{bmatrix}$  to give the curve  $y=\mathbf{f}(x)$ . Given that the curve  $y=\mathbf{f}(x)$  passes through the origin  $(0,\,0)$ , find the value of the constant p.

[3 marks]

(d) The curve with equation  $y=2^{2-x}$  intersects the curve  $y=3\times 12^x$  at the point T. Show that the x-coordinate of T can be written in the form  $\frac{2-\log_2 3}{q+\log_2 3}$ , where q is an integer. State the value of q.

[5 marks]

QUESTION PART REFERENCE	Answer space for question 9



QUESTION PART REFERENCE	Answer space for question 9



QUESTION PART REFERENCE	Answer space for question 9
REFERENCE	
	END OF QUESTIONS
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