

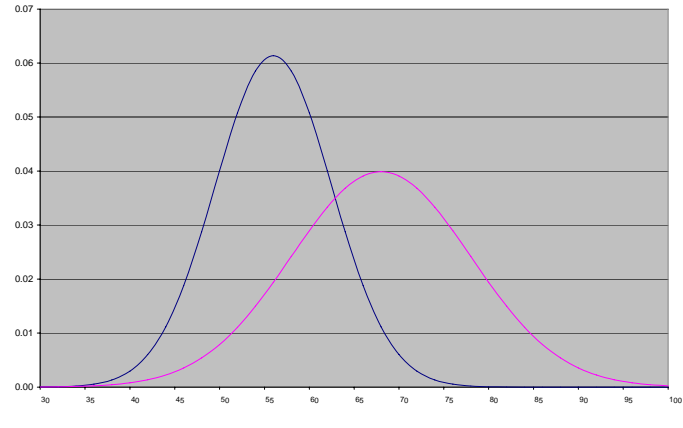
## Question 1

(i)	x is independent, y is dependent since the values of x are chosen by the student but the values of y are dependent on x	B1 E1 dep E1 dep	3
(ii)	$\bar{x} = 2.5, \bar{y} = 80.63$ $b = \frac{S_{xy}}{S_{xx}} = \frac{2530.3 - 30 \times 967.6/12}{90 - 30^2/12} = \frac{111.3}{15} = 7.42$ OR $b = \frac{2530.3/12 - 2.50 \times 80.63}{90/12 - 2.50^2} = \frac{9.275}{1.25} = 7.42$ Hence least squares regression line is: $y - \bar{y} = b(x - \bar{x})$ $\Rightarrow y - 80.63 = 7.42(x - 2.5)$ $\Rightarrow y = 7.42x + 62.08$	B1 for $\bar{x}$ and $\bar{y}$ used (SOI) M1 for attempt at gradient (b) A1 for 7.42 <b>cao</b> M1 for equation of line A1 FT ( $b > 0$ ) for complete equation	5
(iii)	(A) For $x = 1.2$ , predicted growth $= 7.42 \times 1.2 + 62.08 = 71.0$ (B) For $x = 4.3$ , predicted growth $= 7.42 \times 4.3 + 62.08 = 94.0$  Valid relevant comments relating to the predictions such as : Comment re interpolation/extrapolation Comment relating to the fact that $x = 4.3$ is only just beyond the existing data. Comment relating to size of residuals near each predicted value (need not use word 'residual')	M1 for at least one prediction attempted. A1 for both answers (FT their equation if $b > 0$ )  E1 (first comment) E1 (second comment)	4
(iv)	$x = 3 \Rightarrow$ predicted $y = 7.42 \times 3 + 62.08 = 84.3$ Residual = $80 - 84.3 = -4.3$	M1 for prediction  M1 for subtraction A1 FT ( $b > 0$ )	3
(v)	This point is a long way from the regression line. The line may be valid for the range used in the experiment but then the relationship may break down for higher concentrations, or the relationship may be non linear.	E1 E1 for valid in range E1 for <i>either</i> 'may break down' or 'could be non linear' or other relevant comment	3
			18

## Question 2

(i)	Binomial (94,0.1)	B1 for binomial B1 dep for parameters	2
(ii)	$n$ is large and $p$ is small	B1, B1 Allow appropriate numerical ranges	2
(iii)	$\lambda = 94 \times 0.1 = 9.4$  (A) $P(X = 4) = e^{-9.4} \frac{9.4^4}{4!} = 0.0269$ (3 s.f.) or from tables = $0.0429 - 0.0160 = 0.0269$ <i>cao</i> (B) Using tables: $P(X \geq 4) = 1 - P(X \leq 3)$  = $1 - 0.0160 = 0.9840$ <i>cao</i>	B1 for mean  M1 for calculation or use of tables A1 M1 for attempt to find $P(X \geq 4)$ A1 <i>cao</i>	5
(iv)	P(sufficient rooms throughout August) = $0.9840^{31} = 0.6065$	M1 A1 FT	2
(v)	(A) $31 \times 94 = 2914$ Binomial (2914,0.1)  (B) Use Normal approx with $\mu = np = 2914 \times 0.1 = 291.4$ $\sigma^2 = npq = 2914 \times 0.1 \times 0.9 = 262.26$  $P(X \leq 300.5) = P\left(Z \leq \frac{300.5 - 291.4}{\sqrt{262.26}}\right)$ = $P(Z \leq 0.5619) = \Phi(0.5619) = 0.7130$	B1 for binomial B1 dep, for parameters  B1  B1  B1 for continuity corr. M1 for probability using correct tail A1 <i>cao</i> , (but FT wrong or omitted CC)	5
			18

## Question 3

<b>(i)</b>	$X \sim N(56, 6.5^2)$ $P(52.5 < X < 57.5) = P\left(\frac{52.5 - 56}{6.5} < Z < \frac{57.5 - 56}{6.5}\right)$ $= P(-0.538 < Z < 0.231)$ $= \Phi(0.231) - (1 - \Phi(0.538))$ $= 0.5914 - (1 - 0.7046)$ $= 0.5914 - 0.2954$ $= 0.2960 \text{ (4 s.f.) or } 0.296 \text{ (to 3 s.f.)}$	<p>M1 for standardizing</p> <p>A1 for -0.538 and 0.231</p> <p>M1 for prob. with tables and correct structure</p> <p>A1 CAO (min 3 s.f., to include use of difference column)</p>	<b>4</b>
<b>(ii)</b>	$P(\text{5-year-old} < 62) = P\left(Z < \frac{62 - 56}{6.5}\right)$ $= \Phi(0.923) = 0.8220$ $P(\text{young adult} < 62) = P\left(Z < \frac{62 - 68}{10}\right)$ $= \Phi(-0.6) = 1 - 0.7257 = 0.2743$ $P(\text{One over, one under})$ $= 0.8220 \times 0.7257 + 0.1780 \times 0.2743$ $= 0.645$	<p>B1 for 0.8220 or 0.1780</p> <p>B1 for 0.2743 or 0.7257</p> <p>M1 for either product</p> <p>M1 for sum of both products</p> <p>A1 CAO</p>	<b>5</b>
<b>(iii)</b>		<p>G1 for shape</p> <p>G1 for means, shown explicitly or by scale</p> <p>G1 for lower max height in young adults</p> <p>G1 for greater variance in young adults</p>	<b>4</b>
<b>(iv)</b>	$Y \sim N(82, \sigma^2)$ <p>From tables <math>\Phi^{-1}(0.88) = 1.175</math></p> $\frac{62 - 82}{\sigma} = -1.175$ $-20 = -1.175 \sigma$ $\sigma = 17.0$	<p>B1 for 1.175 seen</p> <p>M1 for equation in <math>\sigma</math> with z-value</p> <p>M1 for correct handling of LH tail</p> <p>A1 cao</p>	<b>4</b>
			<b>17</b>

## Question 4

<p>(i)</p> <p><math>H_0</math>: no association between sex and subject;  <math>H_1</math>: some association between sex and subject;</p> <table border="1" data-bbox="247 347 973 560"> <thead> <tr> <th>OBS</th> <th>Maths</th> <th>English</th> <th>Both</th> <th>Neither</th> <th>Row sum</th> </tr> </thead> <tbody> <tr> <td>Male</td> <td>38</td> <td>19</td> <td>6</td> <td>32</td> <td>95</td> </tr> <tr> <td>Female</td> <td>42</td> <td>55</td> <td>9</td> <td>49</td> <td>155</td> </tr> <tr> <td>Col sum</td> <td>80</td> <td>74</td> <td>15</td> <td>81</td> <td>250</td> </tr> </tbody> </table> <table border="1" data-bbox="247 627 989 840"> <thead> <tr> <th>EXP</th> <th>Maths</th> <th>English</th> <th>Both</th> <th>Neither</th> <th>Row sum</th> </tr> </thead> <tbody> <tr> <td>Male</td> <td>30.40</td> <td>28.12</td> <td>5.70</td> <td>30.78</td> <td>95</td> </tr> <tr> <td>Female</td> <td>49.60</td> <td>45.88</td> <td>9.30</td> <td>50.22</td> <td>155</td> </tr> <tr> <td>Col sum</td> <td>80</td> <td>74</td> <td>15</td> <td>81</td> <td>250</td> </tr> </tbody> </table> <table border="1" data-bbox="247 907 973 1019"> <thead> <tr> <th>CONT</th> <th>Maths</th> <th>English</th> <th>Both</th> <th>Neither</th> </tr> </thead> <tbody> <tr> <td>Male</td> <td>1.900</td> <td>2.958</td> <td>0.016</td> <td>0.048</td> </tr> <tr> <td>Female</td> <td>1.165</td> <td>1.813</td> <td>0.010</td> <td>0.030</td> </tr> </tbody> </table> <p><math>\chi^2 = 7.94</math></p> <p>Refer to <math>\chi^2_3</math>  Critical value at 5% level = 7.815  Result is significant  There is evidence to suggest that there is some association between sex and subject choice.  NB if <math>H_0</math> <math>H_1</math> reversed, or 'correlation' mentioned, do not award first B1 or final E1</p>	OBS	Maths	English	Both	Neither	Row sum	Male	38	19	6	32	95	Female	42	55	9	49	155	Col sum	80	74	15	81	250	EXP	Maths	English	Both	Neither	Row sum	Male	30.40	28.12	5.70	30.78	95	Female	49.60	45.88	9.30	50.22	155	Col sum	80	74	15	81	250	CONT	Maths	English	Both	Neither	Male	1.900	2.958	0.016	0.048	Female	1.165	1.813	0.010	0.030	<p>B1</p> <p>M1 A2 for expected values  (allow A1 for at least one row or column correct)</p> <p>M1 for valid attempt at <math>(O-E)^2/E</math>  A1  NB These M1 A1 marks cannot be implied by a correct final value of <math>\chi^2</math></p> <p>M1 for summation  A1 <b>cao</b> for <math>\chi^2</math></p> <p>B1 for 3 deg of f  B1 CAO for cv</p> <p>B1</p> <p>E1</p>	<p>1</p> <p>7</p> <p>4</p>
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<p>(ii)</p> <p><math>H_0: \mu = 67.4</math>; <math>H_1: \mu &gt; 67.4</math>  Where <math>\mu</math> denotes the mean score of the population of students taught with the new method.</p> <p>Test statistic = <math>\frac{68.3 - 67.4}{8.9/\sqrt{12}} = \frac{0.9}{2.57} = 0.35</math></p> <p>10% level 1 tailed critical value of z = 1.282  <math>0.35 &lt; 1.282</math> so not significant.  There is insufficient evidence to reject <math>H_0</math>  There is insufficient evidence to conclude that the mean score is increased by the new teaching method.</p>	<p>B1 for both correct</p> <p>B1 for definition of <math>\mu</math></p> <p>M1</p> <p>A1 <b>cao</b></p> <p>B1 for 1.282</p> <p>M1 for comparison</p> <p>A1 for conclusion in words and in context</p>	<p>7</p> <p>19</p>																																																															