## ADVANCED SUBSIDIARY GCE UNIT

Concepts for Advanced Mathematics (C2)

## TUESDAY 16 JANUARY 2007

Morning
Time: 1 hour 30 minutes

## Additional materials:

Answer booklet (8 pages)
Graph paper
MEI Examination Formulae and Tables (MF2)

## INSTRUCTIONS TO CANDIDATES

- Write your name, centre number and candidate number in the spaces provided on the answer booklet.
- Answer all the questions.
- You are permitted to use a graphical calculator in this paper.
- Final answers should be given to a degree of accuracy appropriate to the context.


## INFORMATION FOR CANDIDATES

- The number of marks is given in brackets [ ] at the end of each question or part question.
- $\quad$ The total number of marks for this paper is 72.
- There is an insert for use in Question 13.


## ADVICE TO CANDIDATES

- Read each question carefully and make sure you know what you have to do before starting your answer.
- You are advised that an answer may receive no marks unless you show sufficient detail of the working to indicate that a correct method is being used.
This document consists of 6 printed pages, 2 blank pages and an insert.
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## Section A (36 marks)

1 Differentiate $6 x^{\frac{5}{2}}+4$.

2 A geometric progression has 6 as its first term. Its sum to infinity is 5 . Calculate its common ratio.

3 Given that $\cos \theta=\frac{1}{3}$ and $\theta$ is acute, find the exact value of $\tan \theta$.

4 Sequences A, B and C are shown below. They each continue in the pattern established by the given terms.

$$
\begin{array}{lllllll}
\text { A: } & 1, & 2, & 4, & 8, & 16, & 32, \\
\text { B: } & 20, & -10, & 5, & -2.5, & 1.25, & -0.625,
\end{array} \ldots
$$

(i) Which of these sequences is periodic?
(ii) Which of these sequences is convergent?
(iii) Find, in terms of $n$, the $n$th term of sequence A.

5 A is the point $(2,1)$ on the curve $y=\frac{4}{x^{2}}$.
B is the point on the same curve with $x$-coordinate 2.1.
(i) Calculate the gradient of the chord AB of the curve. Give your answer correct to 2 decimal places.
(ii) Give the $x$-coordinate of a point C on the curve for which the gradient of chord AC is a better approximation to the gradient of the curve at A .
(iii) Use calculus to find the gradient of the curve at A.

6 Sketch the curve $y=\sin x$ for $0^{\circ} \leqslant x \leqslant 360^{\circ}$.
Solve the equation $\sin x=-0.68$ for $0^{\circ} \leqslant x \leqslant 360^{\circ}$.

7 The gradient of a curve is given by $\frac{\mathrm{d} y}{\mathrm{~d} x}=x^{2}-6 x$. Find the set of values of $x$ for which $y$ is an increasing function of $x$.

8 The 7th term of an arithmetic progression is 6 . The sum of the first 10 terms of the progression is 30.

Find the 5th term of the progression.

9 A curve has gradient given by $\frac{\mathrm{d} y}{\mathrm{~d} x}=6 x^{2}+8 x$. The curve passes through the point $(1,5)$. Find the equation of the curve.

10 (i) Express $\log _{a} x^{4}+\log _{a}\left(\frac{1}{x}\right)$ as a multiple of $\log _{a} x$.
(ii) Given that $\log _{10} b+\log _{10} c=3$, find $b$ in terms of $c$.
[Section B starts on the next page.]

## Section B (36 marks)

11 Fig. 11.1 shows a village green which is bordered by 3 straight roads $\mathrm{AB}, \mathrm{BC}$ and CA . The road AC runs due North and the measurements shown are in metres.


Not to
scale

Fig. 11.1
(i) Calculate the bearing of B from C, giving your answer to the nearest $0.1^{\circ}$.
(ii) Calculate the area of the village green.

The road $A B$ is replaced by a new road, as shown in Fig. 11.2. The village green is extended up to the new road.


Not to
scale

Fig. 11.2
The new road is an arc of a circle with centre O and radius 130 m .
(iii) (A) Show that angle AOB is 1.63 radians, correct to 3 significant figures.
(B) Show that the area of land added to the village green is $5300 \mathrm{~m}^{2}$ correct to 2 significant figures.

12 Fig. 12 is a sketch of the curve $y=2 x^{2}-11 x+12$.


Not to
scale

Fig. 12
(i) Show that the curve intersects the $x$-axis at $(4,0)$ and find the coordinates of the other point of intersection of the curve and the $x$-axis.
(ii) Find the equation of the normal to the curve at the point $(4,0)$.

Show also that the area of the triangle bounded by this normal and the axes is 1.6 units $^{2}$. [6]
(iii) Find the area of the region bounded by the curve and the $x$-axis.

## 13 Answer part (ii) of this question on the insert provided.

The table gives a firm's monthly profits for the first few months after the start of its business, rounded to the nearest $£ 100$.

| Number of months after start-up $(x)$ | 1 | 2 | 3 | 4 | 5 | 6 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Profit for this month $(£ y)$ | 500 | 800 | 1200 | 1900 | 3000 | 4800 |

The firm's profits, $£ y$, for the $x$ th month after start-up are modelled by

$$
y=k \times 10^{a x}
$$

where $a$ and $k$ are constants.
(i) Show that, according to this model, a graph of $\log _{10} y$ against $x$ gives a straight line of gradient $a$ and intercept $\log _{10} k$.
(ii) On the insert, complete the table and plot $\log _{10} y$ against $x$, drawing by eye a line of best fit.
(iii) Use your graph to find an equation for $y$ in terms of $x$ for this model.
(iv) For which month after start-up does this model predict profits of about $£ 75000$ ?
(v) State one way in which this model is unrealistic.

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## INSERT

TUESDAY 16 JANUARY 2007

## Candidate

Name
Centre
Number $\square$ Candidate Number $\square$

## INSTRUCTIONS TO CANDIDATES

- This insert should be used in Question 13(ii).
- Write your name, centre number and candidate number in the spaces provided above and attach the page to your answer booklet.


## 13 (ii)

| Number of months after start-up $(x)$ | 1 | 2 | 3 | 4 | 5 | 6 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Profit for this month (£y) | 500 | 800 | 1200 | 1900 | 3000 | 4800 |
| $\log _{10} y$ | 2.70 |  |  |  |  |  |



