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## Text Instructions

1. Annotations and abbreviations

| Annotation in scoris | Meaning |
| :--- | :--- |
| $\checkmark$ and $\boldsymbol{x}$ |  |
| BOD | Benefit of doubt |
| FT | Follow through |
| ISW | Ignore subsequent working |
| M0, M1 | Method mark awarded 0, 1 |
| A0, A1 | Accuracy mark awarded 0, 1 |
| B0, B1 | Independent mark awarded 0, 1 |
| SC | Special case |
| $\wedge$ | Omission sign |
| MR | Misread |
| Highlighting |  |
|  | Meaning |
| Other abbreviations in <br> mark scheme | Mark for explaining a result or establishing a given result |
| E1 | Correct answer only |
| dep* | Or equivalent |
| cao | Rounded or truncated |
| oe | Seen or implied |
| rot | Without wrong working |
| soi | Answer given |
| www | Anything which ound to |
| AG | By Calculator |
| awrt | This indicates that th i truction In this question you must show detailed reasoning appears in the question. |
| BC | DR |

## 2. Subject-specific Marking Instructions for A Level Mathematics B (MEI)

a Annotations should be used whenever appropriate during your marking. The $A, M$ and $B$ annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded. For subsequent marking you must make it clear how you have arrived at the mark you have awarded.
b An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly. Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not cor esp nd to the mark scheme, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.
If you are in any doubt whatsoever you should contact your Team Leader.
c The following types of marks are available.
M
A suitable method has been selected and applied in a manner which shows that th method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specifi problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

A
Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be award

B
Mark for a correct result or statement independent of Method marks.
E
A given result is to be established or a result has to $b$ explained. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.
d When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep*' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
e The abbreviation FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only - differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, what is acceptable will be detailed in the mark scheme. If this is not the case please, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.
Sometimes the answer to one part of a question is used in a later part of the same question. I this ca e, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if th s is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by que tion.
$\mathrm{f} \quad$ Unless units are specifically requested, there is no penalty for wrong or missing units as lo $g$ as the answer is numerically correct and expressed either in SI or in the units of the question. (e.g. lengths will be assumed to be in metres un ess in a particular question all the lengths are in km, when this would be assumed to be the unspecified unit.) We are usually quite flexible about the a cura $y$ to which the final answer is expressed; over-specification is usually only penalised where the scheme explicitly says so. When a value is given in he pap ronly accept an answer correct to at least as many significant figures as the given value. This rule should be applied to each case. When a val e is not given in the paper accept any answer that agrees with the correct value to 2 s.f. Follow through should be used so that only one mark is lost for ach distinct accuracy error, except for errors due to premature approximation which should be penalised only once in the examinat $n$. The e is no penalty for using a wrong value for $g$. E marks will be lost except when results agree to the accuracy required in the question.
$\mathrm{g} \quad$ Rules for replaced work: if a candidate attempts a question $m r$ than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests; if there are two or mor att pts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore $t$ e other. NB Follow these maths-specific instructions rather than those in the assessor handbook.

For a genuine misreading (of numbers or symbols) ich is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candida e s data A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A mark in the que tion. Marks designated as cao may be awarded as long as there are no other errors. E marks are lost unless, by chance, the given results are established by equivalent working. 'Fresh starts' will not affect an earlier decision about a misread. Note that a miscopy of the candidate's own working is not a misread but an accuracy error.

If a calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers (provided, of course, that there is nothing in the wording of the question specifying that analytical methods are required). Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.
j If in any case the scheme operates with considerable unfairness consult your Team Leader.

| Question |  |  | Answer | Marks | AOs | Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  | DR $\begin{aligned} & y=4-2 x \\ & 4-2 x=x^{2}+x \\ & \Rightarrow x^{2}+3 x-4=0 \end{aligned}$ $\begin{aligned} \Rightarrow x & =1 \text { or } x=-4 \\ y & =2 \text { or } y=12 \end{aligned}$ <br> $(1,2)$ and $(-4,12)$ | M1 <br> M1 <br> A1 <br> A1 <br> A1 <br> [5] | $\begin{aligned} & 2.1 \\ & 1.1 \\ & 1.1 \\ & 1.1 \\ & 2.5 \end{aligned}$ | Eliminating x or y must be seen <br> Form a quadratic equation <br> For final A mark, corresponding valu of $x$ nd $y$ must be expressed as coo dinates from well set out cor ct so ution | Or $y^{2}-14 y+24=0$ <br> SC1 for one pair of coordinates only |
| 2 |  |  | [1-way] stretch scale factor 2 in $y$-direction translation $\binom{0}{-1}$ | M1 A1 M1 A1 $[4]$ |  | If transformations given in reverse order then M1, A1, M1 are still available (but not final A1) $\mathrm{Or}-1$ in $y$-direction |  |


| Question |  |  | Answer | Marks | AOs | Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Que |  |  | $\begin{aligned} & \int_{0}^{\frac{\pi}{12}} \cos 3 x \mathrm{~d} x=\left[\frac{\sin 3 x}{3}\right]_{0}^{\frac{\pi}{12}} \\ & =\frac{1}{3}\left(\sin \frac{\pi}{4}-0\right) \\ & =\frac{\sqrt{2}}{6} \text { о.e. } \end{aligned}$ | B1 <br> M1 <br> A1 <br> [3] | 1.1 <br> 1.1 <br> 1.1 | $\frac{\sin 3 x}{3}$ <br> Must be in exact form |  |
| 4 |  |  | $\begin{aligned} & y=x^{3}-4 x \leftrightarrow y \\ & x=y^{3}-4 \\ & \Rightarrow x+4=y^{3} \\ & \Rightarrow y=\sqrt[3]{x+4} \text { so } \mathrm{f}^{-1}(x)=\sqrt[3]{x+4} \\ & \\ & \text { range of } \mathrm{f} \text { is }-5 \leq y \leq 4 \\ & \text { so domain of } \mathrm{f}^{-1} \text { is }-5 \leq x \leq 4 \\ & \text { range is }-1 \leq y \leq 2 \end{aligned}$ | $\begin{gathered} \text { M1 } \\ \text { A1 } \\ \text { M1 } \\ \text { A1 } \\ \text { B1 } \\ 5] \end{gathered}$ | 1.1 <br> 11 <br> 1.1 <br> 12 <br> 1.1 | at empt to invert <br> acc pt $y=\sqrt[3]{x+4}$ but not $x=\sqrt[3]{y+4}$ <br> May be implied <br> or $[-5,4]$ <br> or $-1 \leq \mathrm{f}^{-1}(x) \leq 2$ or $[-1,2]$ |  |
| 5 |  |  | $\begin{array}{\|l} \hline \operatorname{Binomial}(20,0.08) \\ \mathrm{P}(2 \text { blue })=0.27[11] \end{array}$ | $\begin{gathered} \hline \text { M1 } \\ \text { A1 } \\ {[2]} \end{gathered}$ | $\begin{aligned} & \hline 3.3 \\ & 1.1 \end{aligned}$ | BC |  |
| 6 | (a) | (i) <br> (ii) | $\text { Mean }=17$ <br> Either <br> Points of inflection are approx. 3 above and below mean so SD = approx. 3 | $\begin{aligned} & \hline \text { B1 } \\ & \text { E1 } \end{aligned}$ | $\begin{aligned} & \hline 3.4 \\ & 2.4 \end{aligned}$ | AG |  |
|  |  |  | Or <br> Limits are approx. 9 above and below mean so $\mathrm{SD}=9 \div 3=3$ | E1 | 2.4 | AG |  |



|  |  |  | Marks | AOs | Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10 |  | Method A - E.g. Will not sample people who work then/people who do not walk down that street. Method B - E.g. This will only get answers from those who want to send in an answer. Method C - E.g. This will only get answers from those who use the council website. E.g. Those who use the internet more frequently are more likely to see the question. | B1 <br> B1 <br> B1 <br> [3] | $\begin{aligned} & 2.4 \\ & 2.4 \\ & 2.4 \end{aligned}$ |  |  |
| 11 |  | Suppose $x+y$ is rational <br> So $x+y=\frac{p}{q}$, where $p$ and $q$ are integers $\Rightarrow x=\frac{p}{q}-\frac{m}{n}=\frac{(p n-m q)}{q n}$ which is rational $x$ is irrational so this is a contradiction | E1 <br> B1 <br> B1 <br> E1 <br> [4] | 2.1 <br> 2.1 <br> 3.1a <br> 24 | or stating that the difference of two fractions is rational |  |
| 12 | (a) | $\begin{aligned} & 6 x^{2}+3 y^{2} \frac{\mathrm{~d} y}{\mathrm{~d} x}=5 \frac{\mathrm{~d} y}{\mathrm{~d} x}\left[\Rightarrow \frac{\mathrm{~d} y}{\mathrm{~d} x}=\frac{6 x^{2}}{5-3 y^{2}}\right] \\ & \text { when } x=1, y=2,6+12 \frac{\mathrm{~d} y}{\mathrm{~d} x}=5 \frac{\mathrm{~d}}{\mathrm{~d} x} \\ & \Rightarrow \frac{\mathrm{~d} y}{\mathrm{~d} x}=-\frac{6}{7} \end{aligned}$ | M1 <br> A1 <br> M1 <br> A1 <br> [4] | $\begin{gathered} \hline 1.1 \mathrm{a} \\ 1.1 \\ 1.1 \\ 2.1 \end{gathered}$ | implicit differentation correct substituting $x=1, y=2$ cao |  |
| 12 | (b) | $\frac{\mathrm{d} y}{\mathrm{~d} x}=0 \text { so } 6 x^{2}=0$ <br> $x=0$ so all stationary points lie on $y$-axis | B1 <br> E1 <br> [2] | $1.2$ $2.1$ | Substitute $\frac{\mathrm{d} y}{\mathrm{~d} x}=0$ into their differentiated expression Completion of argument |  |




| Question |  |  | Answer | Marks | AOs | Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 15 | (a) |  | Estimated number $=4+\frac{16}{3}=9 \frac{1}{3}$ <br> $\frac{9 \frac{1}{3}}{80}=0.1166 \ldots$ so proportion is approximately 0.117 | M1 <br> A1 <br> [2] | $\begin{gathered} \hline \text { 3.1b } \\ 1.1 \end{gathered}$ | for attempt at interpolation |  |
| 15 | (b) |  | E.g. Midpoints <br> Mean $=170$ <br> Standard deviation $=3.4$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { A1 } \\ & {[3]} \\ & \hline \end{aligned}$ | $\begin{aligned} & \hline 1.1 \\ & 1.1 \\ & 1.1 \end{aligned}$ | evidence of valid method for estimation <br> BC Mean in the range 169-171 BC SD in the range 3-3.5 |  |
| 15 | (c) |  | The histogram e.g. seems to have a rough bell shape e.g. is symmetrical (around the estimated mean ) e.g. appears to have all data within 3 s.d. of the mean so this does support the manager's belief | B1 <br> B1 <br> 2] | $3.5 \mathrm{a}$ <br> 3.5a | for one re son <br> for at least two reasons and 'supports belief' |  |
| 15 | (d) | (i) <br> (ii) | $\begin{aligned} & \mathrm{P}(\text { Lifetime }>174) \text { for } \mathrm{N}\left(170,3.4^{2}\right) \\ & 0.1197 \end{aligned}$ <br> Answer is very similar to estimate in part (i) | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { B1 } \\ & {[3]} \\ & \hline \end{aligned}$ | $\begin{aligned} & 3.4 \\ & 1.1 \\ & 3.5 \mathrm{a} \end{aligned}$ | oe <br> BC FT their mean and standard deviation |  |


| Question |  | Answer | Marks | AOs | Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 15 | (e) | Either <br> Test statistic $=\frac{207.3-210}{3.4 / \sqrt{8}}=-2.246$ <br> Lower $5 \%$ level 1 tailed critical value of $z=-1.645$ <br> $-2.246<-1.645$ so significant | M1 <br> A1 <br> B1 | $\begin{aligned} & 3.4 \\ & \\ & 1.1 \\ & 1.1 \end{aligned}$ | Must include $\sqrt{ } 8$ <br> For comparison leading to correct conclusion |  |
|  |  | or <br> Under $\mathrm{H}_{0}, \bar{X} \sim \mathrm{~N}\left(210, \frac{3.4^{2}}{8}\right)$ $\mathrm{P}(\bar{X} \leq 207.3)=0.01235$ <br> $0.01235<0.05$ so significant | M1 <br> A1 <br> B1 | 3.4 <br> 1.1 <br> 1.1 | BC |  |
|  |  | There is sufficient evidence to reject $\mathrm{H}_{0}$ There is sufficient evidence to conclude that the mean lifetime is less than 210 minutes. | A1 <br> E1 <br> [5] | $\begin{array}{\|c} \hline 22 \mathrm{~b} \\ \hline 2.4 \end{array}$ | - |  |


| Question |  |  | Answer | Marks | AOs | Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 16 | (a) |  | Comment about shape of distribution for first graph <br> Comment about shape of distribution for second graph | B1 <br> B1 <br> [2] | $\begin{aligned} & \hline 2.2 \mathrm{~b} \\ & 2.2 \mathrm{~b} \end{aligned}$ | Comments can be combined e.g Both distributions negatively skewed gets both marks e.g. 1974 distribution has greater spread than 2014 gets both marks | If zero scored, SC1 for "The 2014 distribution is shifted to the right of the 1974 distribution" oe |
| 16 | (b) | (i) | Life expectancy went down [between 1974 and 2014] in [at least] one country | E1 [1] | 2.2a | NOT increase $n$ life expectancy is negative |  |
| 16 | (b) | (ii) | The box plot is not symmetrical. | $\begin{aligned} & \text { B1 } \\ & {[1]} \end{aligned}$ | 3.5b |  |  |
| 16 | (b) | (iii) | Not appropriate with reason | E1 <br> [1] | $2.4$ | e.g. [some] values of life expectancy re estimates <br> The values of life expectancy are not available to this level of accuracy |  |
| 16 | (b) | (iv) | Comment about life expectancy at birth data for countries and not individual people | B1 [1] | 2.4 |  |  |
| 16 | (c) |  | Use of Q3 + $1.5 \times($ Q3 - Q1) $15.873+1.5(8.9154)=29.2461(\text { year })$ <br> The maximum value is an outlier as $30.742>29.2461$. | M1 M1 <br> A1 [3] | $\begin{aligned} & \hline 1.2 \\ & 1.1 \\ & 1.1 \end{aligned}$ |  |  |


| Question |  |  | Answer | Marks | AOs | Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 16 | (d) | (i) <br> (ii) <br> (iii) | approx 60.8-37.5=23.3 (years) <br> Change in life expectancy for Sweden approx 81.9 - $72.5=9.4 \text { (years) }$ <br> E.g. Countries with a lower life expectancy in 1974 have greater opportunity to increase life expectancy in 2014. | M1 <br> A1 <br> A1 <br> E1 [4] | $\begin{gathered} \text { 3.1b } \\ 1.1 \\ 1.1 \\ \\ \text { 3.2a } \end{gathered}$ | Attempt to estimate change in life expectancy at birth soi. <br> FT 'their 37.5 between $35-40$ ' <br> FT 'their 72.5 between 70-75' OR Countries with a higher life expectancy in 1974 have less opportunity to increase life expectan y in 204. |  |
| 16 | (e) | (i) | $\begin{aligned} & 30.98+0.67 \times 37.4 \\ & =56.0 \text { (years) } \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & {[2]} \end{aligned}$ | $\begin{aligned} & 3.4 \\ & 1.1 \end{aligned}$ |  |  |
| 16 | (e) | (ii) | E.g. Large amount of scatter at the lower values [and South Sudan is 37.4]. <br> E.g. Not having the data value could indicate that there are problems in the country which could mean it does not follow the pattern for other countries | E1 <br> E1 <br> [2] | $\begin{aligned} & 3.5 b \\ & 3.5 b \end{aligned}$ | E1 Reason inferred from Fig 16.4 <br> E1 For knowing why data may be missing |  |
| 16 | (f) |  | Correct method <br> Clearly explained <br> 6 | M1 <br> E1 <br> A1 <br> [3] | $\begin{gathered} \hline \mathbf{3 . 1 b} \\ 2.4 \\ \\ \hline 1.1 \end{gathered}$ | e.g. draw " $y=x$ " on graph <br> e.g. The value on the vertical axis must be lower than the one on the horizontal axis <br> FT their correct method |  |


| Question | A01 | AO2 | AO3(PS) | A03(M) | Total | LDS |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 3 | 2 |  |  | 5 |  |
| 2 | 4 |  |  |  | 4 |  |
| 3 | 3 |  |  |  | 3 |  |
| 4 | 5 |  |  |  | 5 |  |
| 5 | 1 |  |  | 1 | 2 |  |
| 6 a |  | 1 |  | 1 | 2 |  |
| 6 b | 2 |  |  |  | 2 |  |
| 7 | 3 |  | 1 |  | 4 |  |
| 8 |  | 2 | 1 |  | 3 |  |
| 9 a | 1 | 1 |  |  | 2 |  |
| 9 b |  | 2 |  |  | 2 |  |
| 10 |  | 3 |  |  | 3 |  |
| 11 |  | 3 | 1 |  | 4 |  |
| 12 a | 3 | 1 |  |  | 4 |  |
| 12 b | 1 | 1 |  |  | 2 |  |
| 13 | 4 |  | 2 |  | 6 |  |
| 14 a | 5 | 2 | 1 |  | 8 |  |
| 14 b i | 2 |  |  |  | 2 |  |
| 14 b ii |  | 1 | 1 |  | 2 |  |
| 15 a | 1 |  | 1 |  | 2 |  |
| 15 b | 3 |  | - | , | 3 |  |
| 15 c |  |  |  | 2 | 2 |  |
| 15 d | 1 |  |  | 2 | 3 |  |
| 15 e | 2 | 2 |  | 1 | 5 |  |
| 16 a |  | 2 |  |  | 2 |  |
| 16 b i |  | 1 |  |  | 1 |  |
| 16 b ii |  |  |  | 1 | 1 |  |
| 16 b iii |  | 1 |  |  | 1 | 1 |
| 16 b iv |  | 1 |  |  | 1 | 1 |
| 16 c | 3 |  |  |  | 3 |  |
| 16 di | 1 |  | 1 |  | 2 |  |
| 16 d ii | 1 |  |  |  | 1 |  |
| 16 d iii |  |  | 1 |  | 1 | 1 |
| 16 e i | 1 |  |  | 1 | 2 |  |
| 16 e ii |  |  |  | 2 | 2 | 1 |
| 16 f | 1 | 1 | 1 |  | 3 |  |
| Totals | 51 | 27 | 11 | 11 | 100 | LDS |
| \begin{tabular}{\|l||c|}
\hline
\end{tabular} |  |  |  |  |  |  |

