Oxford Cambridge and RSA

## GCE

## Mathematics B (MEI)

H640/02: Pure Mathematics and Statistics

Advanced GCE

## Mark Scheme for June 2019

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

Text Instructions

## Annotations and abbreviations

| Annotation in scoris | Meaning |
| :--- | :--- |
| $\checkmark$ and $\boldsymbol{x}$ | Benefit of doubt |
| BOD | Follow through |
| FT | Ignore subsequent working |
| ISW | Method mark awarded 0, 1 |
| M0, M1 | Accuracy mark awarded 0, 1 |
| A0, A1 | Independent mark awarded 0, 1 |
| B0, B1 | Special case |
| SC | Omission sign |
| $\wedge$ | Misread |
| MR |  |
| Highlighting | Meaning |
|  | Mark for explaining a result or establishing a given result |
| Other abbreviations in <br> mark scheme | Mark dependent on a previous mark, indicated by * |
| E1 | Correct answer only |
| dep* | Or equivalent |
| cao | Rounded or truncated |
| oe | Seen or implied |
| rot | Without wrong working |
| soi | Answer given |
| www | Anything which rounds to |
| AG | By Calculator |
| awrt | This indicates that the instruction In this question you must show detailed reasoning appears in the question. |
| BC |  |
| DR |  |

## Subject-specific Marking Instructions for A Level Mathematics B (MEI)

Annotations should be used whenever appropriate during your marking. The $A, M$ and $B$ annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded For subsequent marking you must make it clear how you have arrived at the mark you have awarded.
b An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly. Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.
If you are in any doubt whatsoever you should contact your Team Leader.
c The following types of marks are available.
M
A suitable method has been selected and applied in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

A
Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

B
Mark for a correct result or statement independent of Method marks.
E
A given result is to be established or a result has to be explained. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep*' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.

The abbreviation FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only - differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, what is acceptable will be detailed in the mark scheme. If this is not the case please, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.
Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.

We are usually quite flexible about the accuracy to which the final answer is expressed; over-specification is usually only penalised where the scheme explicitly says so.

- When a value is given in the paper only accept an answer correct to at least as many significant figures as the given value.
- When a value is not given in the paper accept any answer that agrees with the correct value to 2 s.f.

Follow through should be used so that only one mark is lost for each distinct accuracy error.

Rules for replaced work: if a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests; if there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others. NB Follow these maths-specific instructions rather than those in the assessor handbook.

For a genuine misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A mark in the question. Marks designated as cao may be awarded as long as there are no other errors. E marks are lost unless, by chance, the given results are established by equivalent working. 'Fresh starts' will not affect an earlier decision about a misread. Note that a miscopy of the candidate's own working is not a misread but an accuracy error.

If a graphical calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers (provided, of course, that there is nothing in the wording of the question specifying that analytical methods are required). Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.

| Question |  | Answer | Marks | AOs |  | Guidance |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | (a) | $\begin{aligned} & 0.2+0.1+k+2 k+4 k[=1] \text { soi } \\ & {[k=] 0.1} \end{aligned}$ | M1 <br> A1 <br> [2] | $\begin{gathered} 1.1 \mathrm{a} \\ 1.1 \end{gathered}$ |  |  |
| 1 | (b) | $\begin{aligned} & 1-2 \times \text { their } k \\ & 0.8 \text { or } \frac{4}{5} \text { cao } \end{aligned}$ | M1 <br> A1 <br> [2] | $\begin{aligned} & 1.1 \\ & 1.1 \end{aligned}$ | 1 - their $\mathrm{P}(X=4)$ oe |  |
| 2 | (a) | $\begin{aligned} & k\left(x^{2}+5\right)^{11} \text { seen } \\ & 24 x\left(x^{2}+5\right)^{11} \end{aligned}$ | M1 <br> A1 <br> [2] | $\begin{gathered} \text { 1.1a } \\ 1.1 \end{gathered}$ |  |  |
| 2 | (b) | $\begin{aligned} & a\left(x^{2}+5\right)^{12} \\ & 2\left(x^{2}+5\right)^{12}(+c) \end{aligned}$ | M1 <br> A1 <br> [2] | $\begin{aligned} & 1.1 \\ & 1.1 \end{aligned}$ | condone omission of $+c$ | A1 FT their $k x\left(x^{2}+5\right)^{11}$ from part (a) |
| 3 | (a) | 2.8 to 2.81 BC | B1 <br> [1] | 1.1 |  | NB 2.8063583815029.. |


| Question |  | Answer | Marks | AOs |  | Guidance |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3 | (b) | eg the data is already grouped oe eg we do not have the original raw data oe eg we are using the mid-point of the intervals eg we are assuming the data are uniformly distributed across each interval oe | B1 <br> [1] | 2.4 |  |  |
| 3 | (c) | eg using upper class limit in each case gives mean is 3.4 ...so it is possible that mean is more than 3 | $\begin{aligned} & \text { B1 } \\ & {[1]} \end{aligned}$ | 2.3 | or eg need 520 or more and using the upper limits gives 590 | simply stating eg the mean could be 3.4 is insufficient |
| 4 | (a) | $\frac{0.5}{2}\left[\sqrt{1+(-1)^{3}}+2 \sqrt{1+(-0.5)^{3}}+\sqrt{1+0^{3}}\right] \mathrm{oe}$ <br> $\sqrt{1+(-0.5)^{3}}$ soi <br> 0.717707 cao | M1 <br> B1 <br> A1 <br> [3] | 1.1 <br> 1.1 <br> 1.1 | condone omission of brackets $\text { NB } \frac{\sqrt{14}}{4}=0.9(35414346693)$ <br> NB $\frac{2+\sqrt{14}}{8}$ unsupported implies M1B1 | must be three terms in the bracket <br> if unsupported allow SC3 for 0.717707 and SC2 for 0.717707173347 unsupported to 7 or more dp |
| 4 | (b) | under-estimate since curve is concave down /convex up oe | $\begin{aligned} & \text { B1 } \\ & {[1]} \end{aligned}$ | 2.4 | or eg the slant lines of both trapezia are entirely below the curve allow annotated diagram with at least one trapezium | condone eg trapezium below curve allow integral is 0.841309 BC so my answer is an underestimate |


| Question |  | Answer | Marks | AOs |  | Guidance |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5 | (a) | 2.5 | $\begin{gathered} \text { B1 } \\ {[1]} \end{gathered}$ | 1.1 |  |  |
| 5 | (b) | positive skew cao | $\begin{aligned} & \text { B1 } \\ & {[1]} \end{aligned}$ | 1.1 |  |  |
| 5 | (c) | 1 | $\begin{aligned} & \text { B1 } \\ & {[1]} \end{aligned}$ | 1.1 |  |  |
| 6 |  | $k \frac{x^{-4}}{-4} \ln x-\int k \frac{x^{-4}}{-4} \times \frac{1}{x} \mathrm{~d} x$ oe <br> [32] $\frac{x^{-4}}{-4} \ln x-\int[32] \frac{x^{-4}}{-4} \times \frac{1}{x} \mathrm{~d} x_{\mathrm{oe}}$ <br> $-8 x^{-4} \ln x-2 x^{-4}+c$ oe isw | M1 <br> A1 <br> A1 <br> A1 [4] | 3.1a <br> 1.1 <br> 1.1 <br> 1.1 | allow sign errors only <br> all correct <br> two of three elements correct <br> all three elements correct |  |
| 7 | (a) | $\theta=\frac{72.576}{r^{2}}$ or $72.576 r^{-2} \mathrm{isw}$ | $\begin{aligned} & \text { B1 } \\ & {[1]} \end{aligned}$ | 1.1 | $\text { eg } \frac{9072}{125 r^{2}} \text { or } \frac{9072 r^{-2}}{125}$ |  |
| 7 | (b) | $r \theta+2 r$ or $r(\theta+2)=24.48$ seen and $\theta=\frac{24.48-2 r}{r}$ or equivalent constructive step to give $\frac{24.48}{r}-2 \quad \mathbf{A G}$ | B1 [1] | 1.1 | or $2 \pi r \frac{\theta}{2 \pi}+2 r=24.48$ |  |


| Question |  | Answer | Marks | AOs |  | Guidance |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 7 | (c) | their $\frac{2 \times 36.288}{r^{2}}=\frac{24.48}{r}-2 \quad$ oe $\begin{aligned} & r^{2}-12.24 r+36.288[=0] \\ & {[r=] 5.04 \text { or } 7.2 \mathrm{oe}} \end{aligned}$ | M1 <br> M1 <br> A1 <br> [3] | $\begin{gathered} \text { 3.1a } \\ 2.1 \\ 1.1 \end{gathered}$ | NB 72.576 <br> quadratic obtained in form $\mathrm{f}(r)[=0]$ | allow B3 for 5.04 and 7.2 unsupported or allow SC3 for obtaining and solving an equation for $\theta$ and then finding both values of $r$ |
| 8 | (a) | $\begin{aligned} & 0.4 \times 0.4 \text { or } 0.6 \times 0.2 \text { seen } \\ & 0.4 \times 0.4+0.6 \times 0.2 \\ & 0.28 \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { A1 } \\ & {[3]} \end{aligned}$ | 3.1a <br> 1.1 <br> 1.1 | or tree diagram with correct outcomes and probabilities shown | allow $0.4 \times 0.4 \times 0.4$ or $0.4 \times 0.6 \times 0.2$ <br> mark the final answer |
| 8 | (b) | $\begin{aligned} & \frac{1}{120} \text { or } \frac{5}{120} \text { seen } \\ & \frac{1}{24} \text { or } 0.0416666 \ldots \text { to } 2 \text { or more sf } \end{aligned}$ | M1 <br> A1 <br> [2] | $\begin{gathered} \text { 3.1a } \\ 1.1 \end{gathered}$ | B2 for $0.0416666 \ldots$...unsupported B0 for 0.042 unsupported | mark the final answer |


| Question |  | Answer | Marks | AOs |  | Guidance |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 8 | (c) | $\begin{aligned} & 1-\text { their } \frac{1}{24} \text { evaluated } \\ & 1-\left(\frac{23}{24}\right)^{n}>0.95 \mathrm{FT} \\ & \left(\frac{23}{24}\right)^{n}<0.05 \mathrm{FT} \\ & n=71 \text { cao } \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { M1 } \\ & \text { M1 } \\ & \text { A1 } \\ & {[4]} \end{aligned}$ | 3.1a <br> 2.1 <br> 1.1 <br> 2.2a | allow use of $=, \geqslant$ or $\leqslant$ <br> allow use of $=$ or $\leqslant$ <br> 70.3890...unsupported but rounded to 1 or more dp implies <br> M1M1M1 | award full marks for 71 unsupported or from trial and improvement |
| 9 | (a) | $(2 x+3-1)^{2}$ or $(2 x+3)^{2}-2(2 x+3)+1$ seen simplified to eg $4(x+1)^{2}$ or $4 x^{2}+8 x+4$ or $(2 x+2)^{2}$ <br> domain is $-1<x<0$ | M1 <br> A1 <br> B1 <br> [3] | 1.1 <br> 1.1 <br> 1.1 | substitution <br> mark the final answer <br> from $2 x+3>1$ | ignore superfluous work on eg finding roots |
| 9 | (b) | $0<\operatorname{gf}(x)<4$ | $\begin{aligned} & \text { B1 } \\ & {[1]} \end{aligned}$ | 1.1 |  |  |


| Question |  | Answer | Marks | AOs |  | Guidance |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 9 | (c) | factorise their $\operatorname{gf}(x)$ to obtain perfect square or complete the square <br> $y=4(x+1)^{2}$ or $(2 x+2)^{2}$ oe <br> $(x+1)=( \pm) \sqrt{\frac{y}{4}}$ oe <br> $\left[(\mathrm{gf})^{-1}(x)=\right] \sqrt{\frac{x}{4}}-1$ or $\frac{\sqrt{x}}{2}-1$ oe <br> domain is $0<x<4$ | M1 <br> A1 <br> M1 <br> A1 <br> B1 <br> [5] | 3.1a <br> 2.1 <br> 1.1 <br> 1.1 <br> 1.1 | allow eg $2(x+1)(2 x+2)$; may follow slip eg dividing by 4 FT <br> FT their (b) | or $\mathrm{g}^{-1}(x)=\sqrt{x}+1$ <br> or $\mathrm{f}^{-1}(x)=1 / 2(x-3)$ for M1 <br> A1 for both correct <br> M1 for <br> their $\mathrm{f}^{-1}$ (their $\sqrt{x}+1$ ) <br> A1 for $(\mathrm{gf})^{-1}(x)=\sqrt{\frac{x}{4}}-1$ or $\frac{\sqrt{x}}{2}-1$ oe <br> $x$ and $y$ may be interchanged for the first 3 marks but not for the final A1 |
| 10 | (a) | [=]153 | $\begin{aligned} & \text { B1 } \\ & {[1]} \end{aligned}$ | 1.1 |  |  |
| 10 | (b) | $z= \pm 1.645 \text { used }$ <br> their positive $1.645=\frac{183-\text { their } 153}{\sigma}$ oe $\begin{aligned} & (=18.237 \ldots \text { to } 18.248 \ldots) \\ & \sigma=18.2 \text { cao } \end{aligned}$ | B1 <br> M1 <br> A1 <br> [3] | 1.1 <br> 2.1 <br> 1.1 | or $\pm 1.644$ (85...) | M0 if continuity correction used |


| Question |  | Answer | Marks | AOs |  | Guidance |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10 | (c) | $\left[\frac{16}{452}=\right] 0.035(398 \ldots$... <br> their $\mathrm{P}(X<120)$ from $\mathrm{N}\left(\right.$ their 153 , their $\left.18.2^{2}\right)$ probability of 0.0349 to 0.0352 which agrees to 2 sf | B1 <br> M1 <br> A1 <br> [3] | $\begin{gathered} \text { 3.1b } \\ 1.1 \\ 2.2 b \end{gathered}$ | allow percentage <br> M0 if continuity correction used <br> allow percentage <br> or $\mathbf{B 1}$ for their $\mathrm{P}(X<120)$ then M1 for $452 \times$ their 0.03490 .. then $\mathbf{A 1}$ for 15.77 to 15.91 which is close to 16 oe <br> or B1 as main scheme then M1 for $\sigma=\frac{120-153}{\text { their }-1.809}$ <br> and $18.3 \approx 18.2$ for $\mathbf{A 1}$ | or B1 as main scheme then Invnorm ( 0.0353 , their 153 , their 18.2) for M1 NB 119.95 to 120.15 which is close to 120 oe for A1 <br> or B1 as main scheme then $\begin{aligned} & z=\frac{120-\text { their } 153}{\text { their } 18.2} \text { for } \mathbf{M 1} \\ & \mathbf{N B}-1.809 \text { to }-1.813 \end{aligned}$ <br> and <br> $\operatorname{Invnorm}(0.0353,0,1)$ <br> to obtain -1.806 to <br> -1.812 which is close to <br> -1.809 to -1.813 ) for $\mathbf{A 1}$ |



| Question |  | Answer | Marks | AOs |  | Guidance |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10 | (e) | reduce the value of $\mu$ <br> increase the value of $\sigma$ or $\sigma^{2}$ | $\begin{aligned} & \text { B1 } \\ & \text { B1 } \\ & {[2]} \end{aligned}$ | $\begin{aligned} & 3.5 \mathrm{c} \\ & 3.5 \mathrm{c} \end{aligned}$ | allow $\mathbf{B 1}$ for eg use new sample data to calculate new estimate for $\sigma$ or $\sigma^{2}$ | eg take a bigger sample is insufficient |
| 11 | (a) | differentiate to obtain $2 x-4$ <br> $+1 \times \ln x+x \times \frac{1}{x}$ oe <br> derivative $=0$ oe seen and terms combined $2 x-3+\ln x=0$ www isw AG | B1 <br> M1 <br> A1 <br> A1 <br> [4] | 3.1a <br> 2.1 <br> 1.1 <br> 2.4 | use of Product Rule all correct | allow one error |

\begin{tabular}{|c|c|c|c|c|c|c|}
\hline \multicolumn{2}{|l|}{Question} \& Answer \& Marks \& AOs \& \& Guidance <br>
\hline \multirow[t]{8}{*}{11} \& \multirow[t]{8}{*}{(b)} \& any rearrangement to obtain $x=\mathrm{g}(x)$ from given derivative $=0$
$$
x=\frac{3-\ln x}{2}
$$ \& M1*

A1 \& 2.1
1.1 \& allow sign error

any correct rearrangement \& | $\operatorname{eg} x=\mathrm{e}^{2 x-3}$ |
| :--- |
| need not see subscripts in iterative formula | <br>

\hline \& \& use of their $\mathrm{g}\left(x_{n}\right)=\frac{3-\ln x_{n}}{2}$ to obtain at least two iterates eg 2, 1.1534, 1.4286... \& M1dep* \& 1.1 \& must see iterates \& <br>
\hline \& \& 1.3500 cao \& A1 \& 2.2a \& \& 0 for 1.3500 unsupported <br>
\hline \& \&  \& [4] \& \& \& trial and improvement does not score <br>
\hline \& \& Alternatively,

$$
x_{n+1}=x_{n}-\frac{2 x_{n}-3+\ln x_{n}}{\text { their }\left(2+\frac{1}{x_{n}}\right)}
$$ \& M1* \& 2.1 \& Newton-Rapshon iterative formula seen (not for solving

$$
\mathrm{f}(x)=0)
$$ \& need not see subscripts in iterative formula <br>

\hline \& \& | use of their N-R formula to obtain $x_{1}, x_{2} \ldots$ |
| :--- |
| eg 1.5, 1.34795, 1.34996,....1.349962 | \& | A1 |
| :--- |
| M1dep* | \& 1.1

1.1 \& formula all correct must see iterates \& <br>
\hline \& \& 1.3500 cao \& \& \& \& <br>
\hline \& \& \& A1 [4] \& 2.2a \& \& <br>
\hline
\end{tabular}

| Question |  | Answer | Marks | AOs |  | Guidance |
| :---: | :--- | :--- | :---: | :---: | :--- | :--- |
| $\mathbf{1 2}$ | (a) | $0.94^{n}<k$ or $0.06^{n}<k$ seen | M1 | $\mathbf{3 . 4}$ |  | allow $=$ instead of $<$ |
|  |  | $k=0.025$ used in inequality as above | B1 | $\mathbf{1 . 1}$ |  |  |
|  |  | 60 | A1 | $\mathbf{2 . 2 a}$ | NB $59.617 .$. or $1.311 \ldots$ to 1 or <br> more dp if unsupported implies | 60 unsupported or from <br> trial and improvement <br> scores 3 |


| Question |  | Answer | Marks | AOs |  | Guidance |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 12 | (b) | $\mathrm{H}_{0}: p=0.06$ allow equivalent in words $\mathrm{H}_{1}: p \neq 0.06$ <br> $p$ is the probability that a jaguar chosen at random is a black panther / has black coat | B1 | 1.1 | or $p$ is the proportion of jaguars that are black panthers / have a black coat |  |
|  |  | use of $\mathrm{B}(83,0.06)$ to obtain $\mathrm{P}(X \leq K)$ oe | M1* | 3.3 | not $\mathrm{P}(X=K)$ | NB P $(X \leq 10)=.98927 \ldots$ |
|  |  | $\operatorname{cdfBinomial}(83,0.06,9)=0.973$ to $0.97321 \ldots$ or $1-\operatorname{cdfBinomial}(83,0.06,9)=0.02679$ to 0.027 | A1 | 1.1 | or critical region is $X \geq 11$ (ignore lower tail) | for comparison of their $\mathrm{P}(X>K)$ with 0.025 or |
|  |  | 1 - their $\mathrm{P}(X \leq K)$ compared with 0.025 or their $\mathrm{P}(X \leq K)$ compared with 0.975 oe | M1dep* | 3.4 | eg 10 compared with their critical region oe | their $\mathrm{P}(X \leq K)$ with 0.975 or stating whether 10 is in their critical region |
|  |  | result is not significant or do not reject $\mathrm{H}_{0}$ or reject $\mathrm{H}_{1}$ | A1 | 1.1 | must have the correct probability or correct critical region for the last two A marks | allow accept $\mathrm{H}_{0}$ |
|  |  | there is insufficient evidence at the $5 \%$ level to suggest that the probability that a jaguar selected at random from this population is a black panther is not 0.06 | A1 <br> [7] | 2.2b |  | do not allow eg conclude / prove / indicate or other assertive statement instead of suggest |
| 13 | (a) | 3 | $\begin{aligned} & \hline \text { B1 } \\ & {[1]} \end{aligned}$ | 3.3 |  |  |


| Question |  | Answer | Marks | AOs |  | Guidance |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 13 | (b) | $\left[8 \times 3^{4}=\right] 648$ | $\begin{aligned} & \text { B1 } \\ & {[1]} \end{aligned}$ | 1.1 |  |  |
| 13 | (c) | $\begin{aligned} & \frac{8\left(3^{n}-1\right)}{3-1} \\ & =4\left(3^{n}-1\right) \text { or }-4\left(1-3^{n}\right) \end{aligned}$ | B1 <br> [1] | 3.4 | use of formula for sum of gp mark the final answer | or $4 \times 3^{n}-4$ |
| 13 | (d) | their $4\left(3^{n}-1\right)=185207$ or $3^{n}=46303(.75)$ awrt 9.8 cao $\text { [=] } 9$ | M1 <br> A1 <br> A1 <br> [3] | 3.1a <br> 1.1 <br> 3.2a | M0 for eg $8 \times 3^{n-1}$ no FT available here not from wrong working | allow use of $<$ or $\leqslant$ for up to 3 marks allow M1 only for use of $>$ or $\geq$ or $3^{9}=19683$ and $3^{10}=59049$ seen for M1 then A1 (comparison with 46 303) |
| 13 | (e) | unlikely because <br> eg some of the population will be immune to the virus <br> eg some of the population will not be exposed to the virus <br> eg medical intervention <br> eg extrapolation <br> eg movement of people in and out of town | B1 <br> [1] | 3.5b | any sensible reason | it's unlikely that everyone will be affected oe is insufficient |


| Question |  | Answer | Marks | AOs |  | Guidance |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 14 | (a) | the data was not available for all countries oe | $\begin{aligned} & \hline \text { B1 } \\ & {[1]} \end{aligned}$ | 2.4 |  |  |
| 14 | (b) | use of $\mathrm{Q}_{1}-1.5 \times\left(\mathrm{Q}_{3}-\mathrm{Q}_{1}\right)$ and $\mathrm{Q}_{3}+1.5 \times\left(\mathrm{Q}_{3}-\right.$ $\mathrm{Q}_{1}$ ) seen for either set $\begin{aligned} & 4.135<6.28 \text { and } 15.775>14.46 \\ & 0.38<3.58 \text { and } 18.86>14.89 \end{aligned}$ | M1 <br> A1 <br> A1 <br> [3] | 3.1b <br> 1.1 <br> 1.1 | if A0A0 allow $\mathbf{S C 1}$ for 4.135, $15.775,0.38$ and 18.86 all seen |  |
| 14 | (c) | 22954 isw | B1 <br> [1] | 3.1b | allow 22 955, 22950 or 23000 | $\text { NB } 6411776 \times \frac{3.58}{1000}$ |
| 14 | (d) | there are almost certainly more "old" people in the population oe | B1 <br> [1] | 2.4 |  |  |


| Question |  | Answer | Marks | AOs | Guidance |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{1 4}$ | (e) | in African countries there is a negative <br> association / relationship between (or negative <br> correlation between the ranks of) median age <br> and crude death rate, but in Europe there seems <br> to be a positive association / relationship <br> between (or positive correlation between the <br> ranks of) median age and crude death rate <br> the "association"/ "relationship between" or <br> "correlation between the ranks of" median age <br> and crude death rate (appears to be) stronger in <br> Europe | $\mathbf{B 1}$ | $\mathbf{2 . 4}$ | do not allow "negative <br> correlation" and / or "positive <br> correlation" | comment comparing and <br> contrasting type of <br> relationship in both <br> continents for B1, and one <br> comment comparing and <br> contrasting strength of <br> relationship in both <br> continents for B1 |



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