

| Question number | Scheme | Marks |
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| 1. | $(4-3x)^{-\frac{1}{2}} = 4^{-\frac{1}{2}} \left(1 - \frac{3}{4}x\right)^{-\frac{1}{2}}$ $= \frac{1}{2} \left(1 + \frac{3}{8}x + \frac{\left(-\frac{1}{2}\right)\left(-\frac{3}{2}\right)\left(-\frac{3}{4}x\right)^2}{2} + \frac{\left(-\frac{1}{2}\right)\left(-\frac{3}{2}\right)\left(-\frac{5}{2}\right)\left(-\frac{3}{4}x\right)^3}{6} + \dots \right)$ $= \frac{1}{2} + \frac{3}{16}x + \frac{27}{256}x^2 + \frac{135}{2048}x^3 + \dots$ | <p>B1 M1</p> <p>A1, A1, A1</p> <p>(5 marks)</p> |
| 2. | $26x + 26yy' ; -10xy' - 10y = 0$ $y'(26y - 10x) = 10y - 26x$ $y' = \frac{10y - 26x}{26y - 10x} = \frac{5y - 13x}{13y - 5x}$ | <p>M1A1; M1A1</p> <p>M1 A1</p> <p>(6 marks)</p> |
| 3. | $x = \tan \theta \quad \frac{dx}{d\theta} = \sec^2 \theta \Rightarrow I = \int \frac{\sec^2 \theta}{\sec^4 \theta} d\theta$ <p>Limits $\frac{\pi}{4}$ and 0</p> $I = \int \cos^2 \theta d\theta = \int \frac{\cos 2\theta + 1}{2} d\theta$ $= \left[\frac{\sin 2\theta}{4} + \frac{\theta}{2} \right]_0^{\frac{\pi}{4}}$ $= \frac{1}{4} + \frac{\pi}{8} \quad (*)$ | <p>M1 A1</p> <p>B1</p> <p>M1 A1</p> <p>M1 A1</p> <p>A1 cao</p> <p>(8 marks)</p> |

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| <p>4. (a)</p> <p>(b)</p> <p>(c)</p> | $\frac{dx}{dt} = \sec^2 t \quad \frac{dy}{dt} = 2 \cos 2t, \Rightarrow \frac{dy}{dx} = \frac{2 \cos 2t}{\sec^2 t}$ <p>When $t = \frac{\pi}{3}$ gradient is $-\frac{1}{4}$</p> $y - \frac{\sqrt{3}}{2} = -\frac{1}{m}(x - \sqrt{3})$ <p>P has coordinates $(\sqrt{3}, \frac{\sqrt{3}}{2})$</p> $y - \frac{\sqrt{3}}{2} = 4(x - \sqrt{3})$ $y = 4x - \frac{7}{2}\sqrt{3}$ <p>$\frac{dy}{dx} = 0 \Rightarrow$ gradient of $\tan = 0$, gradient of normal undefined</p> <p>$\therefore x = \tan \frac{\pi}{4}$, i.e: $x = 1$</p> | <p>M1 A1, \Rightarrow M1</p> <p>B1 (4)</p> <p>B1</p> <p>M1</p> <p>A1 (3)</p> <p>M1</p> <p>A1 (2)</p> <p>(9 marks)</p> |
| <p>5. (a)</p> <p>(b)</p> <p>(c)</p> | $5 + \lambda = 2 - 3\mu, \quad 3 - 2\lambda = -11 - 4\mu$ $\therefore \lambda + 3\mu + 3 = 0$ $2\lambda - 4\mu - 14 = 0$ $2\lambda + 6\mu + 6 = 0$ $10\mu + 20 = 0 \Rightarrow \mu = -2 \therefore \lambda = 3$ <p>\therefore point is $(8, -3, 4)$</p> $\therefore a - 10 = 4 \quad \Rightarrow a = 14$ $\cos \theta = \frac{-3 + 8 + 10}{\sqrt{9}\sqrt{25 + 25}}$ $= \frac{15}{3 \times 5\sqrt{2}} = \frac{1}{\sqrt{2}}$ <p>Angle = 45°</p> | <p>B1 B1</p> <p>M1 A1</p> <p>A1 (5)</p> <p>M1 A1 (2)</p> <p>M1 A1</p> <p>M1 A1 (4)</p> <p>(11 marks)</p> |

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| <p>6. (a)</p> <p>(b)</p> | $11x - 1 \equiv A(2 + 3x) + B(1 - x)(2 + 3x) + C(1 - x)^2$ <p>Putting $x = 1 \Rightarrow A = 2$</p> $\text{Putting } x = -\frac{2}{3} \Rightarrow -\frac{25}{3} = \frac{25}{9}C \Rightarrow C = -3$ <p>cf x^2 $0 = -3B + C \Rightarrow B = -1$</p> $\int_0^{\frac{1}{2}} \frac{2}{(1-x)^2} - \frac{1}{(1-x)} - \frac{3}{(2+3x)} dx$ $= \left[\frac{2}{1-x} + \ln 1-x - \ln 2+3x \right]$ $= [4 + \ln \frac{1}{2} - \ln 3 \frac{1}{2} - (2 - \ln 2)]$ $= 2 + \ln \frac{\frac{1}{2} \times 2}{3 \frac{1}{2}}$ $= 2 + \ln \frac{2}{7}$ | <p>B1</p> <p>B1</p> <p>M1A1 (4)</p> <p>M1 A1ft A1ft</p> <p>A1ft</p> <p>M1</p> <p>M1</p> <p>A1 (7)</p> <p>(11 marks)</p> |
| <p>7. (a)</p> <p>(b)</p> | $\frac{du}{dx} = \frac{1}{2} - \frac{1}{2} \cos 4x; = \frac{1}{2} - \frac{1}{2}(1 - 2 \sin^2 2x) = \sin^2 2x$ $V = \pi \int x \sin^2 2x dx$ $= \pi \left[x \left(\frac{x}{2} - \frac{1}{8} \sin 4x \right) - \int \frac{x}{2} - \frac{1}{8} \sin 4x dx \right]_0^{\frac{\pi}{4}}$ $= \pi \left[\frac{x^2}{2} - \frac{x}{8} \sin 4x - \left(\frac{x^2}{4} + \frac{1}{32} \cos 4x \right) \right]_0^{\frac{\pi}{4}}$ $= \pi \left[\frac{\pi^2}{64} + \frac{1}{32} + \frac{1}{32} \right] = \pi \left[\frac{\pi^2}{64} + \frac{1}{16} \right]$ | <p>M1 A1; M1 A1 (4)</p> <p>M1</p> <p>M1 A1 A1</p> <p>M1 A1</p> <p>M1 A1 (8)</p> <p>(12 marks)</p> |

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| 8. (a) | $\frac{dr}{dt} = \frac{k}{r^2}$ $A = \pi r^2 \quad \therefore \frac{dA}{dr} = 2\pi r$ $\therefore \frac{dA}{dt} = 2\pi r \frac{k}{r^2} = \frac{(2\pi k)}{r}; = \frac{(2\pi k)}{\left(\frac{A}{\pi}\right)^{\frac{1}{2}}} = \frac{2\pi^{\frac{3}{2}}k}{\sqrt{A}}$ $\therefore \frac{dA}{dt} \propto \frac{1}{\sqrt{A}} \quad (*)$ | B1 M1A1 M1; M1 A1 (6) |
| | (b) $\int \sqrt{S} \, dS = \int 2e^{2t} \, dt$ $\frac{2}{3} S^{\frac{3}{2}} = e^{2t} + C$ $t = 0, S = 9 \quad \Rightarrow C = 17$ $\therefore \frac{2}{3} S^{\frac{3}{2}} = e^{2t} + 17 \text{ and use } S = 16$ $\left(\frac{128}{3} - 17\right) = e^{2t} \quad \Rightarrow t = \frac{1}{2} \ln \left[\frac{77}{3}\right]$ $= 1.6$ | M1 M1A1 B1 M1 M1 A1 (7) (13 marks) |