

GCSE Mathematics

Paper 1 43651F Mark scheme

43651F June 2015

Version 1: Final Mark Scheme

Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts: alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Assessment Writer.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

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Glossary for Mark Schemes

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

If a student uses a method which is not explicitly covered by the mark scheme the same principles of marking should be applied. Credit should be given to any valid methods. Examiners should seek advice from their senior examiner if in any doubt.

М	Method marks are awarded for a correct method which could lead to a correct answer.
Α	Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.
В	Marks awarded independent of method.
ft	Follow through marks. Marks awarded for correct working following a mistake in an earlier step.
SC	Special case. Marks awarded for a common misinterpretation which has some mathematical worth.
M dep	A method mark dependent on a previous method mark being awarded.
B dep	A mark that can only be awarded if a previous independent mark has been awarded.
oe	Or equivalent. Accept answers that are equivalent.
	e.g. accept 0.5 as well as $\frac{1}{2}$
[a, b]	Accept values between a and b inclusive.
[a, b)	Accept values a ≤ value < b
3.14	Accept answers which begin 3.14 e.g. 3.14, 3.142, 3.1416
Q	Marks awarded for quality of written communication
Use of brackets	It is not necessary to see the bracketed work to award the marks.

Examiners should consistently apply the following principles

Diagrams

Diagrams that have working on them should be treated like normal responses. If a diagram has been written on but the correct response is within the answer space, the work within the answer space should be marked. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working, and is not, therefore, penalised.

Responses which appear to come from incorrect methods

Whenever there is doubt as to whether a candidate has used an incorrect method to obtain an answer, as a general principle, the benefit of doubt must be given to the candidate. In cases where there is no doubt that the answer has come from incorrect working then the candidate should be penalised.

Questions which ask candidates to show working

Instructions on marking will be given but usually marks are not awarded to candidates who show no working.

Questions which do not ask candidates to show working

As a general principle, a correct response is awarded full marks.

Misread or miscopy

Candidates often copy values from a question incorrectly. If the examiner thinks that the candidate has made a genuine misread, then only the accuracy marks (A or B marks), up to a maximum of 2 marks are penalised. The method marks can still be awarded.

Further work

Once the correct answer has been seen, further working may be ignored unless it goes on to contradict the correct answer.

Choice

When a choice of answers and/or methods is given, mark each attempt. If both methods are valid then M marks can be awarded but any incorrect answer or method would result in marks being lost.

Work not replaced

Erased or crossed out work that is still legible should be marked.

Work replaced

Erased or crossed out work that has been replaced is not awarded marks.

Premature approximation

Rounding off too early can lead to inaccuracy in the final answer. This should be penalised by 1 mark unless instructed otherwise.

Paper 1 Foundation Tier

Q	Answer	Mark	Comments			
	Tallies correct for coffee and orange ie Ⅲ Ⅲ	B1	Must use five bar gate for orange Milk tally must be as given			
1(a)	Frequencies correct for milk, coffee and orange ie 5, 3 and 8	B1ft	ft their tallies for milk, coffee and orange			
	Ac	ditional G	buidance			
	Frequencies for coffee and orange may	t or follow through from their tallies				
	3 bars labelled M(ilk), C(offee), O(range) of equal width (1 square), with equal gaps and correct heights	Q2ft	Strand (i) Q1ft Fully correct apart from one error ie unequal widths, unequal or missing gaps, incorrect or missing labels or one height incorrect ft their table (tally or frequency)			
	Additional Guidance					
4(b)	Heights may be correct or follow throug	h from thei	r table			
1(b)	Labelled bars may be in any order. Ass	ume unlab	elled bars are in the given order			
	Mark intention ie condone unruled bars					
	Bars do not need to be shaded or to have matching shading					
	Only check the gaps between the four bars so spacing of 1, 2, 2, 2 squares is correct					
	Equal widths may be eg 2 squares if Te	a bar is ch	anged to 2 squares			
	Accept a key in place of labels					
	Allow the bar chart to be extended to sh	now a heigl	nt of 9, for example			

Q	Answer	Mark	Commen	ts	
	36 or 45 or 54 seen	M1			
	36 and 45 and 54 chosen	M1dep			
	135	A1ft	ft M1M0 correct total of their three num SC1 Correct total of three numbers between 31 and 59 inclusive		
2(a)	Ad	ditional G	luidance		
	39, 48 and 57 chosen and answer 144	(must be	e three numbers added)	SC1	
	36, 45 and 54 chosen in working and a	answer 3		M2A0	
	36, 45 and 56 chosen and answer 137	7		M1M0A1ft	
	135 must not come from incorrect work	ling		A0	
2(b)	At least one of 9, 19, 89 and at least one of 90, 91, 97 seen	M1			
	20	A1	SC1 Answer 19		
3(a)	Plot at (1, 2)	B1	Allow for vertex of rectangle	e at (1, 2)	
	20	B1			
3(b)	cm ²	B1			
4(a)	triangle	B1			
4(b)	pentagon	B1			
4(c)	square	B1			
5	less than greater than equal to	B2	B1 for 2 correct		

Q	Answer	Mark	Comments			
	Alternative method 1 (Price per tin or	for 2 tins)				
	300 ÷ 6 and 180 ÷ 4 or 300 ÷ 3 and 180 ÷ 2	M1	oe			
	50 and 45 or 100 and 90	A1	ое			
	Box of 4 tins identified eg £1.80	Q1ft	Strand (iii) ft their values if M1 awarded SC2 45 and 50 seen SC1 45 or 50 seer			
	Alternative method 2 (Scaling to an ed	qual numbe	er of tins eg multiple of 12)			
	eg 12 tins 2 × 3 and 3 × 1.8(0)	M1	ое			
	6 and 5.4(0)	A1	ое			
6	Box of 4 tins identified eg £1.80	Q1ft	Strand (iii) ft their values if M1 awarded SC2 45 and 50 seen SC1 45 or 50 seen			
	Alternative method 3 (Using small box	to work o	ut cost of 6 tins)			
	180 ÷ 4 or 45 or 180 ÷ 2 or 90 and 180 + their 45×2 or their 45×6	M1	oe 180 + their 90 or their 90 $ imes$ 3			
	(6 tins =) 270	A1	ое			
	Box of 4 tins identified eg £1.80	Q1ft	Strand (iii) ft their values if M1 awarded SC2 45 and 50 seen SC1 45 or 50 see			
	Alternative method 4 (Using large box to work out cost of 4 tins)					
	300 ÷ 6 or 50 or 300 ÷ 3 or 100 and 300 – their 50×2 or their 50×4	M1	oe 300 – their 100 or their 100 × 2			
	(4 tins =) 200	A1	ое			
	Box of 4 tins identified eg £1.80	Q1ft	Strand (iii) ft their values if M1 awarded SC2 45 and 50 seen SC1 45 or 50 see			

Additional Guidance on next page

				Addi	tional Guio	dance				
	Allow workin	g in £ and	/or pence	with or wit	thout units	throughou	t			
	Check the diagram for values									
	All schemes	work in th	e same wa	ay:						
	M1 for full m matching to									
	A1 for evaluation	ating their	value(s)							
	Q1ft, if M1A) awarded	and corre	ct decision	made for t	their evalua	ation(s)			
	However SC			1	1					
6 nt		1	2	3	4	6	8	13	2	24
	Box of 6	50p	£1	£1.50	£2	(£3)	£4	£	6	£12
	Box of 4	45p	90p	£1.35	(£1.80)	£2.70	£3.60	£5.	.40	£10.80
They must have two values to compare (one may have been given) otherwise they will not score (apart from possible SC marks) eg Using box of 4, 8 tins cost £3.60 You get two tins more for only 60p (or each extra tin only costs 30p) Box of 4					ise		M0 A0			
	-		for only 60	p (or each	extra tin o		(0P)			QO
	You get two	tins more tins per £	is impracti	ical on a no	on-calculate	or paper.				
	You get two Box of 4 Working out	tins more tins per £ livisions m	is impracti	ical on a no	on-calculate	or paper.				



0	20÷4 or 5 or 4 \times 5	M1	May be on a diagram
0	25	A1	

Q	Answer	Mark	Comment	S	
	(Area A =) 8	B1	May be on diagram Accept $\frac{8}{16}$ oe		
	(Area B =) 8	(Area B =) 8 B1 May be on diagram Accept $\frac{8}{16}$ oe			
	A has the same area as B indicated B1ft correct ft decision for their awarded				
	Ac	ditional C	Guidance		
	They don't need to explicitly state both areas if same area box is indicated eg Area B = 8 and correct box indicated implies the first B1				
	or Both are 8 and correct box indicated				
	Only indicating the same area box (with no incorrect values for areas)				
9	Area A = 4, Area B = 8 and A < B box in	ndicated		B0B1B1ft	
	Perimeter				
	Where possible award benefit of doubt eg student appears to be counting around the edge of shape A when they may just be counting squares/ unshaded squares				
	If student mentions both area and perimeter, just mark the area part				
	Even if student mentions only perimeter ticking A has the same area as B, howe for ticking one of the other boxes			B0B0B1	
	However, stating $A = 2 + 2 + 2 + 2$ (ie 8 or 14 is clearly perimeter so do not give		1 + 4 + 1 + 1 + 2 + 2 + 2 + 1	B0B0B0	
	Condone no units or incorrect units				
	Two areas seen that are not labelled ar	nd not linke	ed to the diagram		
	eg 2 × 2 = 4 and 1 × 4 + 2 × 2 = 8, then A < B				

Q	Answer	Mark	Comment	S	
	0.15 × 70 oe	M1	If using build-up, must see c correct, full method	completely	
	10.50	Q1	Strand (i) 10.5 or £10.50p is M1Q0 SC1 59.5(0)		
10(a)	Ad	Guidance			
	Build-up must be correct or have full correct method				
	10% = 7, 5% = 2.5 Answer 9.50		M0Q0		
	10% = 7, 7 ÷ 2 = 2.5 Answer 9.50				
	10.5(0) seen in working but then added	to or dedu	icted from 70	M1Q0	

	Alternative method 1				
	40 ÷ 200 (× 100) or $\frac{40}{200}$	M1	oe		
	20	A1	A1 SC1 80		
	Alternative method 2				
10(b)	$\pounds 20 = 10\%$ or $\pounds 10 = 5\%$ or $\pounds 2 = 1\%$	M1	M1 Correct % for any factor/multiple of £40		
	20 A1 SC1 80				
	Additional Guidance				
	40 = 20% seen, then answer 40	M1A0			
	Assume 20 on the answer line is 20% n	M1A1			

Q	Answer	Mark	Comments
11(a)	Scalene	B1	
44/1->	Fully correct ie Angle at either end of line of [68, 72] Angle at other end of line of [58,62] Triangle drawn with ruled straight lines	B2	B1 one angle drawn within tolerance Ignore angle labels
11(b)	A	dditional (Guidance
	If student uses own base line must be s	9 cm ± 2 m	m
	Angles must be at the ends of the lines	, allow tole	erance of ± 2 mm (but judge by eye)
12(a)	20 + 10 - 8 - 8 or 30 or 16	M1	May be on diagram 30 for LHS total 16 for two hearts
	14	A1	
12(b)	20 + 8 + 8 - 10 or 36 - 10 or 26 or 10 + 26 = 36	M1	May be on diagram 26 for two stars
	13	A1	
13(a)	-33	B1	Ignore units eg °C
13(b)	(+)1	B1	Ignore units
13(c)	$K = \frac{5}{9} \ (F - 32) + 273$	B1	
	One correct value in table (-3, -11) or (3, 7)	B1	May be implied from graph if table blank

Q	Answer	Mark	Comments
15(a)	10 <i>xy</i>	B1	
15(b)	6	B2	B1 $18 = (1 \times) 2 (\times) 3 (\times) 3$ or $30 = (1 \times) 2 (\times) 3 (\times) 5$ or one correct prime factor tree or one correct prime factor ladder or one complete set of factors (may be in product pairs) 1, 2, 3, 6, 9, 18 or 1, 2, 3, 5, 6, 10, 15, 30 SC1 Answer 2 and/or 3 or 2 × 3

	Alternative method 1		
	3 × 4.5 or 13.5 or 3 × 4500 or 13500	M1	ое
	their 13.5 ÷ 10 × 200 or $\frac{\text{their } 13500 \div 10 \times 200}{1000}$	M1dep	ое
	270	A1	SC1 digits 27
	Alternative method 2		
16	(200 $ imes$ 4.5) ÷ 10 or 90 (ml)	M1	ое
10	their 90 $ imes$ 3	M1dep	
	270	A1	SC1 digits 27
	Alternative method 3		
	200 : 10000 or $\frac{1}{50}$ and $\frac{1}{50} \times 3$ or 0.06	M1	oe
	their 0.06 \times 4.5 \times 1000	M1dep	ое
	270	A1	SC1 digits 27

Additional Guidance on next page

Q	Answer	Mark	Comm	nents			
	Additional Guidance						
	Students may convert wrongly to millilitres using a factor of 10 (ie 450) then convert back using the same 'wrong' factor to get the correct answer. Allow this, as the method is valid. However, partial marks cannot be awarded if a wrong conversion factor is used but if digits 27 seen allow SC1						
	(1 gallon =) 45 millilitres (3 gallons =) 135 millilitres 135 millilitres \div 10 = 13.5 litres 13.5 \div 10 \times 200 = 270			M1, M1dep, A1			
16	(1 gallon =) 45 millilitres (3 gallons =) 135 millilitres 135 \div 10 \times 200 = 2700	SC1					
cont	If a 'build up' method is used to get millilitres equivalent to 13.5 litres then it must be fully correct to get the M1dep						
	13.5 10 = 200, 1 = 20, 3 × 20 = 80, 200 + 80 + 10 = 290	M1 M1dep A0					
	13.5 10 = 200, 1 = 20, 3 = 60, 0.5 = 200 + 20 + 60 + 10 = 290	M1 M0 A0					
	Gallons 1	×3	→ 3	M1			
	Litres 4.5	10	13.5 13.5	M1dep			
	Lawn feed (ml)	200	×1.35 →270	A1			

Q	Answer	Mar	k	Comments		
	Alternative method 1					
	6 × 18 or 108	M1		(16.2 + 18.1 + 15.9 + 17.8 + 21 + <i>x</i>) ÷ 6		
	their 108 – (16.2+18.1+15.9+17.8+21)	M1 d	ер	oe eg complete repeated subtraction Look for total written under or by table		
	19	A1		SC1 89 seen		
	Alternative method 2	I				
	18 – each value in table, eg 1.8, –0.1, +2.1, +0.2, –3	M1		Allow one error		
17	Totals their subtractions their $(1.8 + -0.1 + 2.1 + 0.2 + -3)$ or 1 and adds to 18	M1de	ep			
	19 A1					
	Additional Guidance					
	16.2 + 18.1 = 34.2, 34.2 + 15.9 = 60.1 60.1 + 17.8 = 77.9, 77.9 + 21.0 = 88.9 $6 \times 18 = 118$ 118 - 88.9 = 30.9				M1 M1dep A0	
		$(16.2 + 18.1 + 15.9 + 17.8 + 21 + x) \div 6 = 18$ $x = 118 - 89.7$			M1 M1dep A0	
	1.8 – 0.1 + 2.1 + 0.3 –3 = 1.1 19.1				M1, M1dep, A0	

Q	Answer	Mark	Comments		
18(a)	5 <i>x</i>	B1			
	1	1	1		
	w = z - 3 or w = -3 + z or $z - 3 = w \text{ or } -3 + z = w$	B1	Must have $w = \text{or} = w$		
18(b)	Additional Guidance				
	Many students write z like the number 2. Allow for this				
	1		 		

	2y(2y + 3)	B2	B1 for $2(2y^2 + 3y)$ or $y(4y + 3y)$	- 6)		
	Additional Guidance					
	Allow × signs between numbers, brackets and letters, eg 2y × (2y + 3) or 2(2 × y^2 + 3 × y)					
18(c)	Factorising may be done in two 'steps', ie $y(4y + 6)$ followed by $2y(2y + 3)$. If the second attempt is done wrongly, B1 can still be awarded.					
	<i>y</i> (4 <i>y</i> + 6)			B1		
	y(4y + 6) 2 $y(2y + 6)$			В0		
	$2(2y^2 + 3y)$			B1		
	$2(2y^2 + 3y)$ 2y(y + 3)			B0		

Q	Answer	Mark	Comment	S	
	Two of the four correct approximations $21.6 \rightarrow 20, 98 \rightarrow 100,$ $34 \rightarrow 30, 18.6 \rightarrow 20$ or denominator $\rightarrow 50$	M1	50 must not come from an incorrect methodeg $54 \rightarrow 50$		
19	Three correct approximations used in the correct calculation or All four correct approximations $21.6 \rightarrow 20, 98 \rightarrow 100,$ $34 \rightarrow 30, 18.6 \rightarrow 20$	M1 dep	eg $\frac{22 \times 100}{30 + 20} \text{ or } \frac{20 \times 98}{30 + 20} \text{ or } \frac{20 \times 100}{34 + 20} \text{ or}$ $\frac{20 \times 100}{30 + 19} \text{ or } \frac{22 \times 100}{50} \text{ or } \frac{20 \times 98}{50}$ 30 and 20 may be implied by 50 but 50 must not come from an incorrect method		
	40 and all approximations correct	A1			
	Additional Guidance				
	Must show correct approximations Answer only of 40 $\frac{22 \times 100}{30 + 20}$ and answer 40 $34 + 19 = 53, 20 \times 100 = 2000, 2000 \div$ $\frac{22 \times 100}{35 + 20} = \frac{2200}{55}$, answer 40 $\frac{2000}{50} = 40$	M0M0A0 M1M1A0 M1M0A0 M1M0A0 M1M0A0			

Q	Answer	Mark	Comments		
	Alternative method 1				
	Correctly lists first three bus times to X or Y				
	ie 7 25, 7 50, 8 15, …	M1	Accept any notation for time eg 7.20, 7:20 7 20, 0720, 7-20, 20 past 7, 720		
	or 7 20, 7 40, 8 00,				
	Continues both lists at least as far as a common time				
	ie 7 25, 7 50, 8 15, 8 40,	M1dep	Allow one error up to and including their common time, ignore errors after		
	and 7 20, 7 40, 8 00, 8 20, 8 40,				
20	8.40 (am) or 08 40 or after/in 100 minutes or after/in 1h 40 minutes	A1	SC2 No other working and any time that is 7 am + 100 <i>n</i> minutes eg 10 20, 12 00, 13 40 etc		
	Alternative method 2				
	Correctly lists first three multiples of 25 or 20				
	ie 25, 50, 75, …	M1	25 × 4 and 20 × 5		
	or 20, 40, 60,				
	Stops both lists at 100 or identifies 100 or 1 hour 40 minutes	M1dep			
	8.40 (am) or 08 40 or after/in 100 minutes or after/in 1h 40 minutes	A1	SC2 No other working and any time that is 7 am + 100 <i>n</i> minutes eg 10 20, 12 00, 13 40 etc		

Additional Guidance on next page

	A	dditional Guidance				
	7 25, 7 50, 8 15, 8 40, 9 05, 7 20, 7 40, 8 00, 8 20, 8 40, 9 00, (Answer =) 8 40 pm	pm is wrong	M1 M1dep A0			
	(No working) (Answer =) 8 40 pm	Method by implication	M2			
	7 25, 7 50, 8 05, 8 30, 8 55, 9 20 7 20, 7 40, 8 00, 8 20, 8 40, 9 00 9 20 (Answer =) 9 20	Second list correct for 3 values. One error in first list. Both lists taken to a common value	M1 M1dep A0			
	7 25, 7 50, 8 10, 8 30, 9 00, 9 15 7 20, 7 40, 8 00, 8 20, 8 40, 9 00 (Answer =) 9 00	Second list correct for 3 values. Both lists taken to a common value but more than one error in first list.	M1 M0dep A0			
20 cont	25, 50, 75, 80, 20, 40, 60, 80, (Answer =) 8 10	At least one list correct for 3 values. Does not get to 100	M1 M0 A0			
	7 00, 25, 50, 8 15, 40, 9 05, 7 00, 20, 40, 8 00, 20, 40, 9 00 8 40	Intention to list times clear	M1 M1dep A1			
	As question asks for 'When' rather than 'What time' then the students do not have to say 8.40 but could qualify it as a length of time after 7am. If so then the wording must be clear.					
	7 25, 7 50, 8 15, 8 40, 9 05, 7 20, 7 40, 8 00, 8 20, 8 40, 9 00, (Answer =) 1 h 40 after 7	Must make it clear that the time is after 7 (am)	M1 M1dep A1			
	7 25, 7 50, 8 15, 8 40, 9 05, 7 20, 7 40, 8 00, 8 20, 8 40, 9 00, (Answer =) 1 h 40	Not clear that the time is after 7 am	M1 M1dep A0			

Q	Answer	Mark	Comments			
			B2 All three conditions met numbers	t but not all whole		
	7, 8, 9, 11, 11, 11 7, 7, 9, 11, 11, 11	В3	B2 two conditions met with (need not be integers)	six numbers		
	7, 9, 9, 11, 11, 11		B1 one condition met with (need not be integers)	six numbers		
			Numbers do not have to be in order			
	Additional Guidance					
	Mark answer line unless blank, then look for an obvious set of 6 numbers. Must be 6 numbers.					
21	7, 9, 9 $\frac{1}{2}$, 10 $\frac{1}{2}$, 11, 11	Mode, range and median but not all whole numbers		B2		
	7 8 10 11 11 11	Mode and range		B2		
	7 8 9 10 11 11	Mode and range		B2		
	8 9 10 10 11 12	Median and range		B2		
	8 9 10 11 12 11	Mode and range (unordered ok)		B2		
	7.5, 8, 10, 11, 11, 11.5	Mode and range		B2		
	8 9 10 10 11 11	Median		B1		

Q	Ar	nswer	Mark	Comments
	0.4 (relative frequency of carp)			oe
	or		B1	
	1 (bream)			
	their roach frequency ÷ 10 (must be less than 1)		M1	
	or			oe
	1 – their carp relative frequency – 0.1			
	or			
22(a)	0.5			
	Fully correct table ie			oe accept equivalent fractions or
	(4) 1	5	A1	percentages for relative frequencies
	0.4 (0.1)	0.5		throughout
	Additional Guidance			
	If table fully correct award 3 marks. If not check for 0.4 or 1. Either scores B1. Then check la column/bottom row. If the roach relative frequency = roach frequency ÷ 10 or if the total of t relative frequencies is 1 then award M1.			

	Increase sample size Repeat it Check some more Catch more fish					
	Additional Guidance					
	Count it again, catch more fish	Last bit scores		B1		
22(b)	Fish on more days	More impl	B1			
	Fish for longer	Longer implies increased sample		B1		
	Fish on different days	Different does not imply increased sample		В0		
	Do the estimate twice	Not implying increasing sample		В0		
	Catch them all	Not a sam	ple	В0		
	Experiment at different times of day	Not implyi	В0			