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Centre number		Candidate number	
Surname			
Forename(s)			
Candidate signature			

Level 2 Certificate in Further Mathematics FURTHER MATHEMATICS

Level 2 Paper 1 Non-Calculator

Monday 20 June 2016

Morning

Time allowed: 1 hour 30 minutes

Materials

For this paper you must have:mathematical instruments.

You must **not** use a calculator.



Instructions

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Answer all questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- Do all rough work in this book. Cross through any work you do not want to be marked.
- In all calculations, show clearly how you work out your answer.

Information

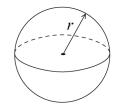
- The marks for questions are shown in brackets.
- The maximum mark for this paper is 70.
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to this answer book.



Formulae Sheet

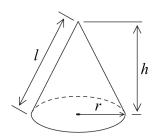
Volume of sphere
$$=\frac{4}{3}\pi r^3$$

Surface area of sphere
$$=4\pi r^2$$



Volume of cone
$$=\frac{1}{3}\pi r^2 h$$

Curved surface area of cone
$$=\pi rl$$



In any triangle ABC

Area of triangle =
$$\frac{1}{2}ab \sin C$$

Sine rule
$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$\sin C$$

$$\frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc\cos A$$

$$\cos A = \frac{b^2 + c^2 - a^2}{2bc}$$

The Quadratic Equation

The solutions of $ax^2 + bx + c = 0$, where $a \neq 0$, are given by

$$x = \frac{-b \pm \sqrt{(b^2 - 4ac)}}{2a}$$

Trigonometric Identities

$$\tan \theta \equiv \frac{\sin \theta}{\cos \theta}$$
 $\sin^2 \theta + \cos^2 \theta \equiv 1$

Answer all questions in the spaces provided.

1 $y = x^2(x - 10)$

Work out $\frac{dy}{dx}$

[3 marks]

Answer _____

 $4\begin{pmatrix} 1-2a\\a\end{pmatrix}=\begin{pmatrix} b\\12\end{pmatrix}$

Work out the values of a and b.

[3 marks]

a = _____

b = _____

3	The <i>n</i> th term of a sequence is $\frac{3n}{5n+12}$	
3 (a)	Work out the position of the term that has a value of $\frac{1}{2}$	[2 marks]
	Answer	
3 (b)	Write down the limiting value of $\frac{3n}{5n+12}$ as $n \to \infty$	[1 mark]
	Answer	

- $(x+5)^2 + (y-8)^2 = 10$ 4 The equation of a circle is
- What are the coordinates of the centre of the circle? 4 (a) Circle your answer.

[1 mark]

- (-5, -8) (-5, 8) (5, 8)

4 (b) Write down the radius of the circle.

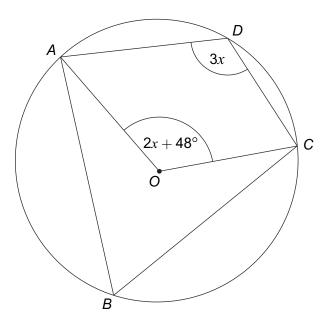
[1 mark]

Answer ____

Turn over for the next question

5 A, B, C and D are points on a circle, centre O.

Not drawn accurately



Work out the value of x.

	[3 marks]

x =	degrees

6	$mx + 4 - 2(x + p) \equiv 6(x + 1)$ where m and p are integers.	
	Work out the values of m and p .	[4 marks]
	m =	_
	p =	_
7	Work out the integer values of x for which $x^2 - 20x + 96 < 0$	
•	work out the integer values of x for which $x = 20x + 90 < 0$	[3 marks]
	Answer	-



8	Solve $(3 - \sqrt{x})^{\frac{1}{3}} = -2$	[3 marks]
	<i>x</i> =	_
	_	
9	Expand and simplify $(x-5)^3$	[3 marks]
9	Expand and simplify $(x-5)^3$	[3 marks]
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Do not write outside the box

10	$\sqrt[4]{x} = 2$ and $y^{-2} = 25$
	x > 0 and $y < 0$
	Work out the value of $\frac{x}{y}$ [4 marks]
	Answer
	Turn over for the next question

0 9

Turn over ▶

	10	
11	$A(1\frac{1}{5}, 3\frac{4}{5})$, $B(2, 1\frac{4}{5})$ and $C(5, 3)$ are points on a coordinate grid.	
	Show that the line segments AB and BC are perpendicular.	[3 marks]

12 You are given that	$x^2 + 6x + 2 \equiv (x+h)^2 + h$
-----------------------	-----------------------------------

12 (a) Work out the values of h and k.

[2 marks]



$$h =$$

12 (b) Write down the coordinates of the minimum point on the curve $y = x^2 + 6x + 2$ [1 mark]

Answer (______, ,____)

12 (c) Solve the equation $x^2 + 6x + 2 = 0$ Give your answers in the form $a \pm \sqrt{b}$

[1 mark]

Answer _____

13	Solve	$\sqrt{125} + \sqrt{20} = \sqrt{80} + \sqrt{x}$	[3 marks]
		x =	



14 (a)	(x-3) is a factor of	$x^3 - 8x^2 + ax + 42$	where a is an integer.	
	Show that the value of	<i>a</i> is 1		[2 marks]
14 (b)	Hence, factorise fully	$x^3 - 8x^2 + x + 42$		
				[3 marks]
	Ans	wer		_



15	Rationalise the denominator and simplify fully $\frac{6}{\sqrt{7}+2}$	[3 marks]
	Answer	



16	Angle $ heta$ is obtuse and $\sin heta = rac{\sqrt{11}}{6}$		
	Work out the value of $\cos\theta$	[4 marks]	
	Answer		

Turn over for the next question

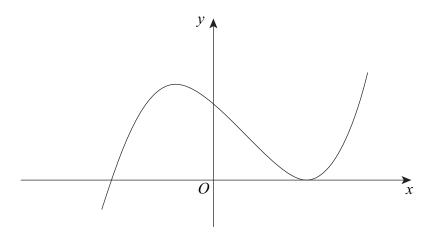


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The diagram shows a sketch of the cubic curve $y = \frac{1}{3}x^3 - x^2 - 3x + k$

The *x*-axis is a tangent to the curve at its minimum point.

Not drawn accurately



Work out the value of k.

where k is a constant.

[5 marks]

z = _____

		••	
18	Factorise fully	$x^4 - 81$	[2 marks]
		Amouse	
		Answer	
		Turn over for the next questio	n

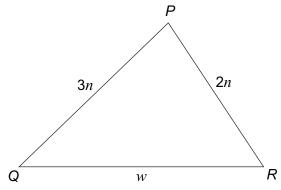
Turn over ▶

19	ABCD is a square. CDE is a straight line.	
	AC is $3\sqrt{2}$ cm and angle DEA = 60°	
	A $3\sqrt{2} \text{ cm}$ C D E	Not drawn accurately
19 (a)	Show that the side of the square is 3 cm	[2 marks]
19 (b)	Show that the perimeter of trapezium \textit{ABCE} is $3(3+\sqrt{3})\text{cm}$	[4 marks]



20 In triangle PQR, $\cos P = \frac{1}{3}$

Not drawn accurately



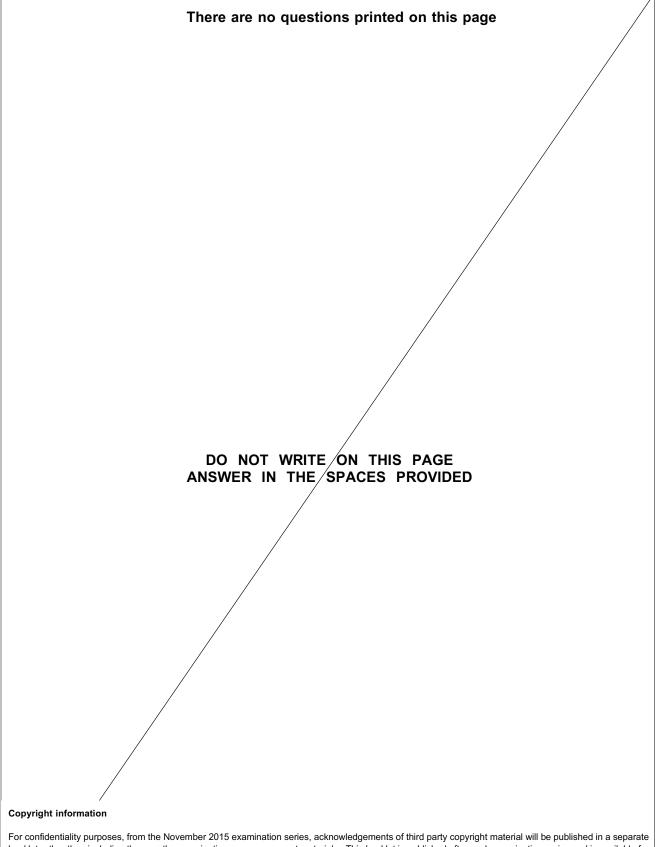
Show that triangle *PQR* is isosceles.

[4 marks]

END OF QUESTIONS







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