

GCSE MATHEMATICS 8300/2F

Foundation Tier Paper 2 Calculator

Mark scheme

June 2023

Version: 1.0 Final



Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts. Alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

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Glossary for Mark Schemes

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

If a student uses a method which is not explicitly covered by the mark scheme the same principles of marking should be applied. Credit should be given to any valid methods. Examiners should seek advice from their senior examiner if in any doubt.

М	Method marks are awarded for a correct method which could lead to a correct answer.
Α	Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.
В	Marks awarded independent of method.
ft	Follow through marks. Marks awarded for correct working following a mistake in an earlier step.
SC	Special case. Marks awarded for a common misinterpretation which has some mathematical worth.
M dep	A method mark dependent on a previous method mark being awarded.
B dep	A mark that can only be awarded if a previous independent mark has been awarded.
oe	Or equivalent. Accept answers that are equivalent.
	eg accept 0.5 as well as $\frac{1}{2}$
[a, b]	Accept values between a and b inclusive.
[a, b)	Accept values a
3.14	Accept answers which begin 3.14 eg 3.14, 3.142, 3.1416
Use of brackets	It is not necessary to see the bracketed work to award the marks.

Examiners should consistently apply the following principles.

Diagrams

Diagrams that have working on them should be treated like normal responses. If a diagram has been written on but the correct response is within the answer space, the work within the answer space should be marked. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working, and is not, therefore, penalised.

Responses which appear to come from incorrect methods

Whenever there is doubt as to whether a student has used an incorrect method to obtain an answer, as a general principle, the benefit of doubt must be given to the student. In cases where there is no doubt that the answer has come from incorrect working then the student should be penalised.

Questions which ask students to show working

Instructions on marking will be given but usually marks are not awarded to students who show no working.

Questions which do not ask students to show working

As a general principle, a correct response is awarded full marks.

Misread or miscopy

Students often copy values from a question incorrectly. If the examiner thinks that the student has made a genuine misread, then only the accuracy marks (A or B marks), up to a maximum of 2 marks are penalised. The method marks can still be awarded.

Further work

Once the correct answer has been seen, further working may be ignored unless it goes on to contradict the correct answer.

Choice

When a choice of answers and/or methods is given, mark each attempt. If both methods are valid then M marks can be awarded but any incorrect answer or method would result in marks being lost.

Work not replaced

Erased or crossed out work that is still legible should be marked.

Work replaced

Erased or crossed out work that has been replaced is not awarded marks.

Premature approximation

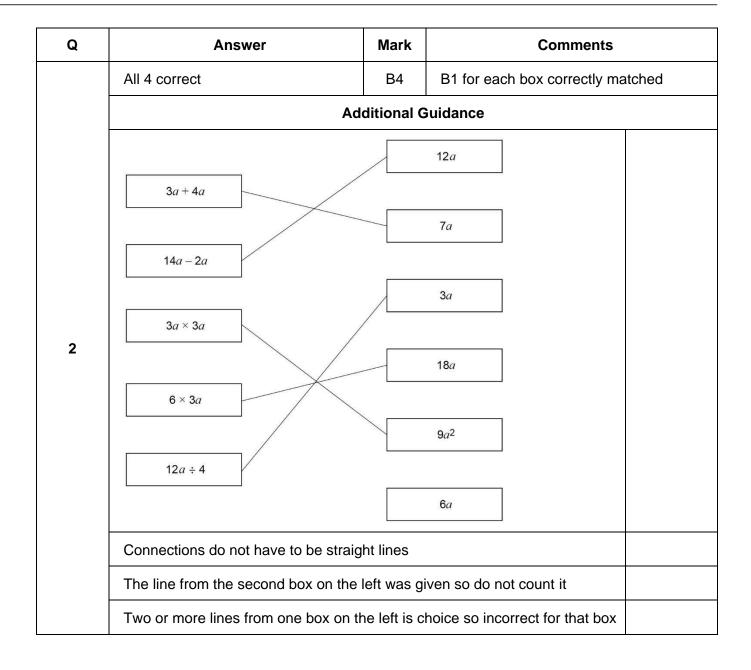
Rounding off too early can lead to inaccuracy in the final answer. This should be penalised by 1 mark unless instructed otherwise.

Continental notation

Accept a comma used instead of a decimal point (for example, in measurements or currency), provided that it is clear to the examiner that the student intended it to be a decimal point.

Q	Answer	Mark	Comments		
	35	B1			
1(a)	Additional Guidance				
	Mark the answer line. If this is blank, diagram	the answe	er may be seen on the		

Q	Answer	Mark	Comments	
	-2	B1		
1(b)	Additional Guidance			
	Mark the answer line. If this is blank, diagram	the answe	er may be seen on the	



Q	Answer	Mark	Comments		
	A and (A =) 14 and (B =) 12	B2	B1 (A =) 14 or (B =) 12 14 and/or 12 may be on the accept 140 and 120	diagram	
	Additional Guidance				
3(a)	Ignore reference to areas of any shapes and perimeters of the other shapes Ignore units, including for 140 and 120 If answer line blank, accept A clearly indicated in working Accept 14 on the answer line in place of A with 12 seen for B B2				

Q	Answer	Mark	Comments
3(b)	D	B1	

Q	Answer	Mark	Comments
3(c)	C and E	B1	either order

Q	Answer	Mark	Comments		
	Any correct reflection of shape with corresponding mirror line shown	B2	B1 any correct reflection of shape with no or incorrect mirror line		
	Additional Guidance				
	Mark intention for mirror line and sha				
3(d)	Ignore internal lines				
	For B2, if there is more than one sha apply the rules of choice	pe and/o	more than one mirror line,		
	For B1, any one correct reflection of the shape (even with other incorrect shapes) will score B1				

Q	Answer	Mark	Comments	
	(4, 3)	B1	accept (4, 3)	
44.	Additional Guidance Mark the answer line. If this is blank, the answer may be seen on the diagram but must be the coordinates for P			
4(a)				
	Do not allow x and y within the coordinates eg (42		(4x, 3y)	В0

Q	Answer	Mark	Comments	
	$(x, -3)$ where $x \neq 4$	B1	accept eg $\begin{pmatrix} x & y \\ 5, & -3 \end{pmatrix}$	
4(b)	Additional Guidance			
	Do not allow x and y within the coord	inates eg	(5x, -3y)	В0

Q	Answer	Mark	Comments	
	5 ÷ 0.75 or 500 ÷ 75 or 6.6() or 6.7 or 75 × 6 or 450 or 0.75 × 6 or 4.5 or 75 × 7 or 525 or 0.75 × 7 or 5.25	M1	oe eg build up or build down	
	6	A1		
5(a)	Additional Guidance			
	Incorrect work seen is A0 eg $75 \times 6 = 450$ and $75 \times 7 = 575$	Answer 6		M1A0
	Do not allow 5 ÷ 75 or 500 ÷ 0.75 unless recovered			
	Build up must be fully correct method, no errors, 75, 150, 225, 300, 375, 450, (525)			
	Build down must be fully correct meth 50	nod, no er	rors, 425, 350, 275, 200, 125,	

Q	Answer	Mark	Comments
	Alternative method 1 Comparing to	he cost of	24 bottles
	2.5 × 0.1 or 0.25 or 1 – 0.1 or 0.9	M1	oe eg 2.5 \div 10 discount or multiplier for shop X implied by 2.5 \times 6 \times 0.1 or 1.5 or 2.25
	(2.5 – their 0.25) × 6 or 2.5 × their 0.9 × 6 or 2.25 × 6 or 13.5	M1dep	oe eg 15 × 0.9 or 15 – 1.5 shop X
	7 × 2 or 14	M1	oe shop Z
	X with 13.5 and 14 seen	A1	oe
	Alternative method 2 Comparing to	he cost of	1 bottle
	2.5 × 0.1 or 0.25 or 1 – 0.1 or 0.9	M1	oe eg 2.5 \div 10 discount or multiplier for shop X implied by 2.5 \div 4 \times 0.1 or 0.06(25) or 2.25
5(b)	(2.5 – their 0.25) ÷ 4 or 2.5 × their 0.9 ÷ 4 or 2.25 ÷ 4 or 0.56(25) or 0.563	M1dep	oe eg 0.62(5) × 0.9 or 0.62(5) – 0.06(25) shop X
	7 ÷ 12 or 0.58(3)	M1	oe shop Z
	X with 0.56(25) or 0.563 and 0.58(3) seen	A1	oe
	Alternative method 3 Comparing to	he cost of	12 bottles
	2.5 × 0.1 or 0.25 or 1 – 0.1 or 0.9	M1	oe eg 2.5 \div 10 discount or multiplier for shop X implied by 2.5 \times 3 \times 0.1 or 0.75 or 2.25
	$(2.5 - \text{their } 0.25) \times 3$ or $2.5 \times \text{their } 0.9 \times 3$ or 2.25×3	M1dep	oe eg 7.5 × their 0.9 or 7.5 – 0.75 shop X
	X with 6.75 (and 7) seen	A2	A1 6.75 oe

Question 5(b) continues on the next page

Cost of 4

2.25

2.33(3...)

Cost of 6

3.37(5) or 3.38

3.5

	Additional Guidance	
	Up to 3 marks may be awarded for correct work with no answer or incorrect answer, even if this is seen amongst multiple attempts	
	Use the scheme that favours the student	
	eg 0.56 and 0.58 followed by 13.44 and 13.92 and X (mark by Alt 2)	M3A1
	Ignore incorrect money notation eg 13.5 or 14.0	
	All schemes can be oe in pence and allow work in a mix of pounds or pence for up to 3 marks	
	Condone eg answer 13.5 with 14 seen	M3A1
5(b) cont	For 0.1 × 2.5, accept 10% × 2.5 but do not accept 10% of 2.5 unless recovered	
	Allow variations	
	eg Shop X £15, Shop Z £14,	M1
	Shop X is £1 more but the discount is £1.50	M1M1
	Shop X cheaper	A1
	Where the student compares eg 2, 3, 4, 6, 48 or 96 bottles apply the principles some relevant figures given below (after offer)	s of Alt 2 –

Q	Answer	Mark	Comments			
6	All five extra sets ie AC or CA but not both and AD or DA but not both and BC or CB but not both and BD or DB but not both and CD or DC but not both	B2	list in any order B1 any three or four of the five correct			
	Additional Guidance					
	Mark the grid unless blank					
	Ignore extras, repeats and reversals	not for B2				

Cost of 3

1.68(75) or 1.69

1.75

Shop

Χ

Ζ

Cost of 2

1.12(5) or 1.13

1.16(6...) or 1.17

Q		An	swe	r			Mark	Comments	
	Two even and two odd numbers and the numbers all different and the sum of the four numbers is 46						B2	any order B1 two even and two odd not and the sum of the four numbers or the numbers all different and the sum of the four numbers or two even and two odd numb and the numbers all different and the sum of the four numbers	is 46 is 46 ers
						Add	ditional G	uidance	
7(a)	11 +	8	+	6	+	21			B2
	30 +	10	+	3	+	3	(no	t all different)	B1
	8 +	12	+	10	+	16	(no	odds)	B1
	10 +	16	+	1	+	11	(no	t 46 but in range)	B1
	15 +	10	+	15	+	10	(no	t all different and not 46)	ВО
	3 +	5	+	7	+	29	(no	evens and not 46)	ВО
	Negatives are acceptable for B1 or B2								
	0 is an even number for B1 or B2, but a blank box does not imply 0								
	Fractions and/or decimals are acceptable for four different numbers that sum to 46 for B1								
	Mark the boxes								

Q			Answer	Mark	Comments		
7(b)	3 × 10 or 6 × 5			B2	either order B1 uses a factor of 12 and the product of the two numbers is [24, 36] or uses a factor of 40 and the product of the two numbers is [24, 36] or the product of the two numbers is 30		
		1 1		Additional	Guidance	Τ	
	3	×	9			B1	
	7	×	5			B1	
	30	×	1			B1	
	15	×	2			B1	
	Fractio	ns a	and/or decimals	s are acceptable for	non-factors for B1		
	Mark th	ne b	oxes				

Q		Ans	swer	Mark	Comments	
	36	÷ 2		B2	B1 any square number > 1 or any prime number	
			Ad	ditional G	Buidance	
	Allow so	quares to l	be written in index f	orm for B2	2 or B1 eg	
7(c)	62	÷ 2				B2
	2	÷ 36				B1
		÷ 9				B1
	72	÷ 4				B1
	Mark the	e boxes				

Q	Answer	Mark	Comments		
	45 in No (Played)	B1			
	36 in No (More than one game played?)	B1			
	12 in Yes (More than one game		ft 48 – their 36		
	played?)	B1ft	their 36 must be a positive in than 48	nteger less	
	Ad	ditional G	Guidance		
	Mark the frequency tree				
8(a)	93 48 36				
	93 48	36 12		B1B0B1ft	

Q	Answer	Mark	Comments			
	Alternative method 1					
	0.68 × 93 or 63.2(4)	M1	oe			
	64	A1				
	Alternative method 2					
	$\frac{63}{93} = 0.67()$		other trials can be ignored			
	or	M1				
8(b)	$\frac{64}{93} = [0.68, 0.69]$					
	64	A1				
	Additional Guidance					
	Answer only 64			M1A1		
	0.69 × 93 or 64.1(7) or 64.2 with a (without seeing 0.68 × 93 or 63.2(4)	M0A0				
	For 0.68 × 93, accept 68% × 93 but of recovered	ao not acc	ept 66% Of 93 utiless			

Q	Answer	Mark	Comments			
	6 × 4 or 24		oe			
	or	M1				
	11 × (12 – 4) or 11 × 8 or 88					
9(a)	112	A1				
	Additional Guidance					
	112.00(p)			M1A1		
	112.0			M1A0		

Q	Answer	Mark	Comments			
	Alternative method 1 Works in min	or hrs for	9 episodes and 1 episode			
	$9 \times 50 \text{ or } 450$ or $9 \times \frac{50}{60} \text{ or } \frac{450}{60}$	M1 $eg \ 9 \times \frac{5}{9} \text{ or } \frac{45}{9} \text{ or } \frac{15}{9} \text$				
	$60 + 42$ or 102 or $\frac{102}{60}$ oe fraction or 1.7	M1	552 or 9.2 implies M1M1			
	9 hours 12 minutes SC2 9h 32 min or 6h 32 min or 9h 20 min			in		
	Alternative method 2 Works in min or hrs for 9 episodes and converts to hrs and min					
9(b)	$9 \times 50 \text{ or } 450$ or $9 \times \frac{50}{60} \text{ or } \frac{450}{60}$	M1	M1 eg $9 \times \frac{5}{6}$ or $\frac{45}{6}$ or $\frac{15}{2}$ or implied by 7 h 30 min			
	7 h 30 min ft conversion of their 450 to minutes if their 450 > 60 M1 or their $\frac{450}{60}$ to hours and reconstruction $\frac{450}{60}$ > 1					
	9 hours 12 minutes	A1	SC2 9h 32min or 6h 32min or 9h 20min			
	Additional Guidance					
	7 h 50 min + 1 h 42 min = 9 h 32 min		SC2			
	4 h 50 min + 1 h 42 min = 6 h 32 min			SC2		
	9.2 h = 9 h 20 min			SC2		

Q	Answer	Mark	Comments		
	1020 ÷ 5 (× 2) or 204 (× 2)	M1	oe		
	408	A1	SC1 612		
	Additional Guidance				
10(a)	$\frac{408}{1020}$ on answer line	M1A0			
	Condone 408 out of 1020	M1A1			
	For 0.4 × 1020, accept 40% × 1020 to recovered				

Q	Answer	Mark	Comments			
	$\frac{4}{7}$ B1	oe fraction				
10(b)	Additional Guidance					
	Conversion to decimal or percentage	В0				

Q	Answer	Mark	Comments		
	220 ÷ 250 (× 100) or 0.88	M1	oe		
40(-)	88	A1	SC1 12		
10(c)	Additional Guidance				
	Build-up methods must be correct or show correct method for each step				

Q	Answer	Mark	Comments			
	8 in W only	B1				
	21 in (H U W)'	B1ft	ft 29 – their 8 their 8 must be < 29			
11(a)	Additional Guidance					
	15 in W only 21 in (H U W)'			B0 B1		
	15 in W only 14 in (H U W)'			B0 B1ft		

Q	Answer	Mark	Comments				
	7 60 or [0.116, 0.117] or [11.6, 11.7]%	B1	oe fraction				
	Additional Guidance						
11(b)	Ignore conversion attempt to decimal after correct probability seen	, fraction	or percentage (but not ratio)				
	Do not allow eg 7 in 60 or 7 out of 60 unless the correct probability seen						
	Do not allow ratio						
	Ignore words if correct probability see	en					

Q	Answer	Mark	Comments		
	Valid explanation	B1	eg needs brackets around 3	5 – 19	
	Ad	ditional G	Guidance		
	Any calculations shown must be corre	ect			
	Ignore irrelevant, non-contradictory s	tatements	3		
	It gives 25.5 and it should be 8			B1	
	(It gives the wrong answer,) it should	be 8		B1	
	He shouldn't divide (by 2) first			B1	
	He needs brackets around the takeaway				
	He needs to subtract first	B1			
	He should do 35 – 19 and then divide	B1			
11(c)	(35 – 19) ÷ 2 (may correct the give	B1			
	$\frac{35-19}{2}$ (implies the brackets)	B1			
	This gives 25.5 (or 51) when he need	B1			
	$35 - 19 = 16$ $16 \div 2 = 8$ (needs to	say that	this is what he should do)	В0	
	This gives 25.5 (or 51) which is too m	nuch (ne	eds to compare with 8 or 16)	В0	
	He hasn't used BIDMAS			В0	
	It gives the wrong answer			В0	
	35 – 19 ÷ 2 = 8			В0	
	35 – 19 ÷ 2 = 25.50			В0	
	He needs brackets	В0			

Q	Answer	Mark	Comments			
	Ticks Both of them and gives valid reason for Kai eg references both values being divided (or multiplied) by 3 and gives valid reason for Jo eg references both values being divided (or multiplied) by 6	B2	oe valid reason eg1 9 ÷ 3 × 2 = 6 and 9 ÷ or eg2 9 ÷ 6 = 1.5 and 3 ÷ 2 * and 1.5 ÷ 1 = 1.5 B1 ticks Kai only and gives valid reason for K or ticks Jo only and gives valid reason for Jo or ticks Both of them and gives valid reason for Jo	= 1.5 Cai		
	Additional Guidance					
12	Ticks Both of them and gives correct reason for Kai or Jo and refs both values being divided (or multiplied) by 2 (to link Jo and Kai) Accept a build-up method to imply multiplying by 3 or by 6 eg all three of 3 : 2 and 6 : 4 and 9 : 6 or all six of 1.5 : 1 and 3 : 2 and 4.5 : 3 and 6 : 4 and 7.5 : 5 and 9 : 6					
	Condone eg 3:2 × 3 = 9:6 to imp					
	If evaluating 6 ÷ 9 = 0.66 and 2 ÷ 3 = 0.66() or 0.67					
	3 is a factor of 9 and 2 is a factor of 6	В0				
	9:6=3:2 or $\frac{9}{6} = \frac{3}{2}$ (not evaluated	В0				
	9:6 simplifies to 3:2 and 1.5:1 (with	В0				
	3 : 2 and 1.5 : 1 are both equivalent t	o 9 : 6 (wi	ith no reference to \times 3 or \times 6)	В0		

Q	Answer	Mark	Comments			
	Correct method or evaluation for the 25% or the 15% or correct multiplier for the increase or the decrease seen	M1	eg 28 × 0.25 or 7 or 40 × 0.15 or 6 or 1.25 or 0.85 oe			
	Correct method or evaluation for either calculation	M1dep	eg 28 + 28 × 0.25 or 35 or 40 × 0.85 or 34			
	Correct method or evaluation for both calculations	M1dep				
	35 with 34 seen	A1	oe eg 28 increased by 25% with 35 and seen			
13	Additional Guidance					
	28 × 1.25 or 35					
	40 × 0.85 or 34	M1M1				
	28 × 1.25 or 35 and 40 × 0.85 or	M1M1M1				
	Build-up methods must be correct or					
	eg 1 10% = 2.8, 5% = 1.4, 25% = 7	M1				
	eg 2 $10\% = 2.8$, $5\% = 2.8 \div 2 = 1.8$, method shown for that step)	M1				
	eg 3 10% = 2.8, 5% = 1.8, 25% = 7. shown for that step)	MO				
	35 and 34 seen and 35 chosen by eg circling					
	For 28 × 0.25, do not accept 28 × 25% unless recovered					

Q	Answer	Mark	Comments		
	3(4a + 5b)	B1			
	Ade	ditional G	Guidance		
	Condone missing final bracket ie 3(4a + 5b				
14	Allow multiplying back out to check their answer				
"	Further incorrect work after a correct response is B0				
	eg $3(4a + 5b) = 27ab$				
	3(a4 + b5)				
	$3\times(4a+5b)$			В0	

Q	Answer	Mark	Comments			
	-3, -2, -1, 0, 1	B2	any order B1 four correct and none incorrect or five correct and one incorrect			
15	Additional Guidance					
13	-2, -1, 0, 1			B1		
	-3, -2, -1, 0, 1, 2			B1		
	-3, -2, -1, 1			B1		
	-2, -1, 0, 1, 2			В0		

Q	Answer	Mark	Comments		
	3n + 4 or 4 + 3n	B2	oe eg 7 + (3n - 3) B1 3n (+) or 3n ()		
	Ade	ditional G	Guidance		
	Ignore LHS of formula given eg $T_n =$	3n + 4		B2	
	Condone $n = 3n + 4$ or n th term = 3	3n + 4		B2	
	Allow a multiplication sign eg $3 \times n + 4$ or $n \times 3 + 4$				
16	Allow other variables eg 3x + 4			B2	
	3x				
	n3				
	n3 + 4			B1	
	3nth + 4				
	3nth				
	3n + 4n			В0	

Q	Ans	wer		Mark	Comments			
	45 × 8 or 360			M1	oe number of 2p coins may be embedded			
	45 × 8 × 2 or 360 × 2 or 720 or 7.2(0)			M1dep	oe value of 2p coins implied by 1170 or 11.7(0)			
	17.7(0) – their 7.2 or 1770 – their 720 – or 6(.00) or 600).1(0)	M1dep	oe value of 5p coins implied by 7.2 : 6 oe ratio not in simple form or 6:7.2 oe ratio			
	6:5			A1	accept 1.2:1 or $\frac{6}{5}$:1 or $1\frac{1}{5}$:1 or 1:0.83() or 1: $\frac{5}{6}$			
17	Additional Guidance							
	Up to M3 may be awarded for correct work with no answer or incorrect answer, even if this is seen amongst multiple attempts							
	Allow working in pence or pounds throughout							
	Must work consistently in pence or pounds for the third mark (or recover)							
	Ignore units in the ratio eg 6p : 5p or £1.20 : £1						M3A1	
	720 may be seen in a ratio with the value of the 10p coins eg 720 : 450 or 7.2 : 4.5						M2	
	600 may be seen in a ratio with the value of the 10p coins eg 600 : 450 or 6 : 4.5					3	M3	
	For information:	Coin	10p	2p	5p			
		Number	45	360	120			
		Value	£4.50	£7.20	£6.00			

Q	Answer			Mark			Commen	ts		
	All values correct				B2	B1 1 or 2 rows correct				
		Additional Guidance								
40(-)		1	2	3		4	5	6		
18(a)	2x	2	4	6		8	10	12		B2
	3x	3	6	9		12	15	18		DZ
	x ²	1	4	9		16	25	36		

Q	Answer	Mark	Comments			
	$\frac{8}{18}$ or $\frac{4}{9}$ or 0.44(4) or 44(.4)%	B1ft	oe fraction, decimal or percentage ft their table with ≥ 12 values must be using 18 for the total number of possible scores			
	Additional Guidance					
18(b)	Ignore simplification or conversion at seen	tempt (not	ratio) after correct probability			
	Ratio answer eg 8 : 18, even alongsion	de a corre	ct probability is B0			
	ft decimals or percentages must be correct to the same accuracy as in the scheme					
	eg 10 winning values in their table					
	$\frac{10}{18}$ or 0.55(5) or 0.56 or 0.556 or 55(.5)% or 56% or 55.6%					

Q	Answer	Mark	Comments	
	$711 \times \text{their } \frac{8}{18}$	M1	oe ft their probability from (b) or if no probability in (b), ft their table with ≥ 12 values where 0 < their probability < 1 probabilities, if rounded in (c), must be truncated or rounded to at least 2 sf SC2 395	
	Ado	ditional G	Guidance	
	Answer 316		M1A1	
	$\frac{316}{711}$ on answer line	M1A0		
	Condone 316 out of 711	M1A1		
18(c)	Do not treat estimating by rounding a eg1 700 used instead of 711 eg2 (b) 0.44 (c) 0.4 × 711 (round eg3 (b) 0.4 (c) 0.4 × 711 (follow	m (c) for the probability) M0A0		
	Do not allow ft for a ratio from (b) but	eir (a) instead		
	For 0.44 × 711, accept 44% × 711 burecovered	accept 44% of 711 unless		
	The method mark may be implied by the nearest integer or rounded up to eg1 (b) $\frac{7}{18}$	· ·		
	(c) 276.5 or 276 or 277 (correct f			
	(c) 276.5 or 276 or 277 (correct	` , .		

Q	Answer	Mark	Comments				
	360 ÷ 8 or 135 seen	M1	oe eg $45 \times 8 = 360$ or $180 - \frac{(8-2) \times 180}{8}$ may be on diagram				
19(a)	45	A1					
	Additional Guidance						
	M1 may be awarded for correct work even if this is seen amongst multiple						
	45 seen but not chosen as answer, e	M1A0					

Q	Answer	Mark	Comments
19(b)	It is less than the answer to part (a)	B1	

Q	Answer	Mark	Comments	
	(4) (-3)	B2	B1 $\begin{pmatrix} 4 \\ \end{pmatrix}$ or $\begin{pmatrix} \\ -3 \end{pmatrix}$ SC1 $\begin{pmatrix} -4 \\ 3 \end{pmatrix}$	
	Ad	ditional G	Guidance	
	$(4, -3)$ or $\begin{pmatrix} -3\\4 \end{pmatrix}$			В0
	Ignore words if a vector is also seen			
	eg1 Reflection $\begin{pmatrix} 4 \\ -3 \end{pmatrix}$			B2
20	eg2 4 right 3 up and $\binom{4}{3}$			B1
	eg3 4 right 3 down			В0
	eg4 Rotate 4 left and 3 up and $\begin{pmatrix} -4 \\ 3 \end{pmatrix}$			SC1
	Condone any type of brackets			
	Condone missing brackets for B2 or B1 or SC1 but must have two numbers in a column			
	Condone 'fraction line' for B2 or B1 or SC1 but must have two numbers in a column			
	$\begin{pmatrix} 4x \\ -3y \end{pmatrix} \text{ or } \begin{pmatrix} x4 \\ -y3 \end{pmatrix} \text{ or } \begin{pmatrix} x+4 \\ y-3 \end{pmatrix} \text{ or } \begin{pmatrix} 4x \\ 3y-3 \end{pmatrix}$	4 right 3 down	or $\begin{pmatrix} 4 \text{ r} \\ 3 \text{ d} \end{pmatrix}$ or $\begin{pmatrix} 4 \rightarrow \\ 3 \downarrow \end{pmatrix}$	В0

Q	Answer	Mark	Comments	
	Alternative method 1 Compares 70% of volume of hemisphere with volume of water			
	$\frac{4}{3} \times \pi \times 12^3$ or 2304π		oe eg $\frac{4}{3}\pi \times 1728$	
	or [7216, 7239.2]		allow without any multiplication signs	
	or	M1	eg $\frac{4}{3}\pi 12^3$	
	$\frac{2}{3} \times \pi \times 12^3$ or 1152 π			
	or [3581, 3638]			
	$0.7 imes their 1152\pi$ or 806.4π		oe	
	or [2506, 2547]	M1dep	$0.7 \times \text{their} [3581, 3638] \text{ or } \frac{4032}{5} \pi$	
			must be using volume of hemisphere	
	325 × 8 or 2600	M1	oe	
	[2506, 2547] and 2600 and Yes	A1	oe	
21	Alternative method 2 Works out volume of water as proportion of volume of hemisphere			
	$\frac{4}{3} \times \pi \times 12^3$ or 2304π		oe eg $\frac{4}{3}\pi \times 1728$	
	or [7216, 7239.2]		allow without any multiplication signs	
	or	M1	eg $\frac{4}{3}\pi 12^3$	
	$\frac{2}{3} \times \pi \times 12^3$ or 1152 π			
	or [3581, 3638]			
	325 × 8 or 2600	M1	oe	
	their 2600 ÷ their 1152π	M1dep	oe eg their 2600 ÷ their [3581, 3638]	
	or [0.71, 0.73]		or 72%	
			dep on M2 must be using volume of hemisphere	
	[71 73](%) and Vac	A1	-	
	[71, 73](%) and Yes	AI	oe eg 0.72 and 0.7 and Yes	

Question 21 continues on the next page

	Alternative method 3 Works out time to fill 70% of volume of hemisphere			
	$\frac{4}{3} \times \pi \times 12^{3}$ or 2304π or $[7216, 7239.2]$ or $\frac{2}{3} \times \pi \times 12^{3}$ or 1152π	M1	oe eg $\frac{4}{3}\pi \times 1728$ allow without any multiplication signs eg $\frac{4}{3}\pi 12^3$	
21 cont	or [3581, 3638]			
	$0.7 \times$ their 1152π or 806.4π or $[2506, 2547]$ or their $1152\pi \div 325$ or $[11, 11.2]$	M1dep	oe $0.7 \times \text{their} [3581, 3638] \text{ or } \frac{4032}{5} \pi$ or $\text{their} [3581, 3638] \div 325$ must be using volume of hemisphere	
	$0.7 \times$ their $1152\pi \div 325$ or $0.7 \times$ their $[3581, 3638] \div 325$ or $[7.7, 7.84]$	M1dep	oe their [2506, 2547] ÷ 325 or 0.7 × their [11, 11.2]	
	[7.7, 7.84] and Yes	A1	oe	

Question 21 continues on the next page

	Additional Guidance			
	Up to M3 may be awarded for correct work with no answer or incorrect answer, even if this is seen amongst multiple attempts			
	Allow 1.33() for $\frac{4}{3}$			
	Allow 0.66() or 0.67 for $\frac{2}{3}$			
	π may be seen as [3.14, 3.142] eg Alt 1 $\frac{2}{3} \times 3.14 \times 12^3$	M1		
	If a number (or calculation) in terms of π is seen but π is subsequently omitted, treat as a miscopy for M marks			
21	eg Alt 1			
cont	1152π	M1		
	$0.7 \times 1152 = 806.4$	M1dep		
	$325 \times 8 = 2600$ Yes	M1A0		
	Yes cannot be implied by inequalities			
	Alts 1 and 2			
	$325\text{cm}^3 imes 8$ seen is M1 even if evaluated incorrectly			
	$325^3 \times 8$ seen is M0 unless recovered to 2600			
	Do not allow misreads of the given formula unless recovered			
	eg1 using 12 ² instead of 12 ³			
	eg2 using $\frac{3}{4}$ instead of $\frac{4}{3}$			
	For $0.7 \times$ their 1152 π , do not accept 70% \times their 1152 π unless recovered			

Q	Answer	Mark	Comments	
	$8 \div 5$ or $19.2 \div 12$ or $\frac{8}{5}$ or $\frac{19.2}{12}$ or 1.6 or $12 \div 5$ or $19.2 \div 8$ or $\frac{12}{5}$ or $\frac{19.2}{8}$ or 2.4	M1	oe use of a valid pair of side appropriate calculation or valeg 5 ÷ 8 or 0.625 or 5 ÷ 12 or [0.416, 0.417]	
	$8 \div 5 = 19.2 \div 12 \text{ or } \frac{8}{5} = \frac{19.2}{12}$ or $12 \div 5 = 19.2 \div 8 \text{ or } \frac{12}{5} = \frac{19.2}{8}$	A1	oe showing sides are in property of $5 \div 8 = 12 \div 19.2$ or $\frac{5}{12} = \frac{8}{19.2}$	portion
	Ad	ditional G	Buidance	
	For A1 equating may be implied by two calculations or two fractions with correct evaluation			
	eg $8 \div 5 = 19.2 \div 12$ is implied by $8 = 5 \times 1.6$ and $19.2 = 12 \times 1.6$			M1A1
22	For A1 equating may be implied by calculations eg1 $8 \div 5 = 19.2 \div 12$ is implied by $8 \div 5 = 1.6$ and $12 \times 1.6 = 19.2$ eg2 $8 \div 5 = 19.2 \div 12$ is implied by $\frac{8}{5} \times 12 = 19.2$			M1A1 M1A1
	5 × 19.2 = 8 × 12			M1A1
	$5 \times 19.2 = 96$ and $8 \times 12 = 96$			M1A1
	Non-contradictory working can be ignored eg correct response along with area calculations			M1A1
	Ignore words eg references to scale factors, enlargement, angles			
	Working on diagrams may be seen eg1 Arrows or lines from 5 to 8 and 12 to 19.2 with × 1.6 on them eg2 Arrows or lines from 5 to 8 and 12 to 19.2 with 1.6 on them Arrows or lines must unambiguously link relevant numbers			M1A1 M1A0
	For $8 \div 5$ or $\frac{8}{5}$ allow $8:5$ etc			

Q	Answer	Mark	Comments	
	$80 \times x$ or $80x$ or $x \times 80$ or $x80$ or $x \div 60$ or $\frac{x}{60}$ or $\frac{1}{60}x$ or $x \div \frac{1}{60}$ or $80 \div 60$ or $\frac{80}{60}$	M1	teabags per hour boxes per minute	
	$\frac{80x}{60} \left(= \frac{4x}{3} \right)$ or $80 \div 60 \times x \left(= \frac{4x}{3} \right)$	A1	oe showing 80 and 60 and x eg $\frac{80 \times x}{60} \left(= \frac{4x}{3} \right)$ or $x = \frac{80}{60}$ or $x = \frac{80}{60} \times x = \frac{4x}{3}$ or $x = \frac{4x}{3}$	$\left(=\frac{4x}{3}\right)$
	Additional Guidance			
	M1 may be awarded for correct work with no answer or incorrect answer, even if this is seen amongst multiple attempts			
23	Do not allow M1 if only seen embedded in an incorrect expression or calculation $eg 80x \times 4 = 320x$			MO
	$60 \times \frac{4x}{3} = 80x$ (M1 allowed as $80x$ is not embedded in an incorrect expression or calculation, A0 because using the given answer)			M1A0
	Condone x = 80 ÷ 60			M1A0
	$\frac{80x}{60} \left(= \frac{4x}{3} \right)$			M1A1
	$\frac{80}{60} = \frac{4}{3} \text{ and } \frac{4}{3} \times x \left(= \frac{4x}{3} \right)$ $\frac{80}{60} = \frac{4}{3} \text{ and } \frac{4x}{3}$			M1A1
				M1A0
	No equivalents allowed for M1			
	Ignore units			
	Condone 1.33() for $\frac{4}{3}$			
	Ignore non-contradictory working after	er M1A1 s	een	