

Please check the examination details below before entering your candidate information

Candidate surname

Other names

Centre Number

Candidate Number

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Pearson Edexcel Level 3 GCE

Time 1 hour 30 minutes

Paper
reference

9FM0/02

Further Mathematics

Advanced

PAPER 2: Core Pure Mathematics 2

You must have:

Mathematical Formulae and Statistical Tables (Green), calculator

Total Marks

Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear.
Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 9 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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Q:1/1/1/1/1/




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4. (i) Given that

$$z_1 = 6e^{\frac{\pi}{3}i} \text{ and } z_2 = 6\sqrt{3}e^{\frac{5\pi}{6}i}$$

show that

$$z_1 + z_2 = 12e^{\frac{2\pi}{3}i} \quad (3)$$

(ii) Given that

$$\arg(z - 5) = \frac{2\pi}{3}$$

determine the least value of $|z|$ as z varies.

(3)



Question 6 continued

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Question 6 continued

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7.

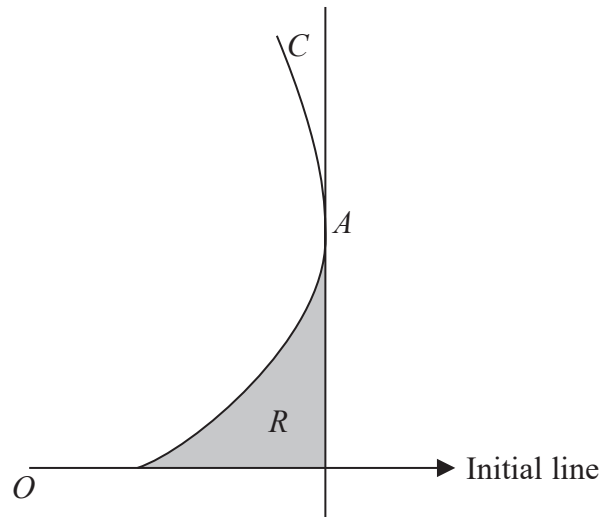


Figure 1

Figure 1 shows a sketch of the curve C with equation

$$r = 1 + \tan \theta \quad 0 \leq \theta < \frac{\pi}{3}$$

Figure 1 also shows the tangent to C at the point A .
This tangent is perpendicular to the initial line.

- (a) Use differentiation to prove that the polar coordinates of A are $\left(2, \frac{\pi}{4}\right)$ (4)

The finite region R , shown shaded in Figure 1, is bounded by C , the tangent at A and the initial line.

- (b) Use calculus to show that the exact area of R is $\frac{1}{2}(1 - \ln 2)$ (6)



Question 7 continued

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Question 7 continued

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(Total for Question 7 is 10 marks)



P 7 1 8 0 1 A 0 2 5 3 2

8. Two birds are flying towards their nest, which is in a tree.

Relative to a fixed origin, the flight path of each bird is modelled by a straight line.

In the model, the equation for the flight path of the first bird is

$$\mathbf{r}_1 = \begin{pmatrix} -1 \\ 5 \\ 2 \end{pmatrix} + \lambda \begin{pmatrix} 2 \\ a \\ 0 \end{pmatrix}$$

and the equation for the flight path of the second bird is

$$\mathbf{r}_2 = \begin{pmatrix} 4 \\ -1 \\ 3 \end{pmatrix} + \mu \begin{pmatrix} 0 \\ 1 \\ -1 \end{pmatrix}$$

where λ and μ are scalar parameters and a is a constant.

In the model, the angle between the birds' flight paths is 120°

- (a) Determine the value of a . (4)

- (b) Verify that, according to the model, there is a common point on the flight paths of the two birds and find the coordinates of this common point. (5)

The position of the nest is modelled as being at this common point.

The tree containing the nest is in a park.

The ground level of the park is modelled by the plane with equation

$$2x - 3y + z = 2$$

- (c) Hence determine the shortest distance from the nest to the ground level of the park. (3)

- (d) By considering the model, comment on whether your answer to part (c) is reliable, giving a reason for your answer. (1)



Question 8 continued

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Question 8 continued

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(Total for Question 8 is 13 marks)



P 7 1 8 0 1 A 0 2 9 3 2

9.
$$y = \cosh^n x \quad n \geq 5$$

(a) (i) Show that

$$\frac{d^2 y}{dx^2} = n^2 \cosh^n x - n(n - 1) \cosh^{n-2} x \tag{4}$$

(ii) Determine an expression for $\frac{d^4 y}{dx^4}$ (2)

(b) Hence determine the first three non-zero terms of the Maclaurin series for y , giving each coefficient in simplest form. (2)



Question 9 continued

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Question 9 continued

Lined writing area for the answer to Question 9.

(Total for Question 9 is 8 marks)

TOTAL FOR PAPER IS 75 MARKS

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