

2. In a large college 58% of students are female and 42% are male. A random sample of 100 students is chosen from the college. Using a suitable approximation find the probability that more than half the sample are female.

(7)



3. A test statistic has a Poisson distribution with parameter λ .

Given that

$$H_0 : \lambda = 9, H_1 : \lambda \neq 9$$

(a) find the critical region for the test statistic such that the probability in each tail is as close as possible to 2.5%. **(3)**

(b) State the probability of incorrectly rejecting H_0 using this critical region. **(2)**



- 6. A call centre agent handles telephone calls at a rate of 18 per hour.
 - (a) Give two reasons to support the use of a Poisson distribution as a suitable model for the number of calls per hour handled by the agent. (2)
 - (b) Find the probability that in any randomly selected 15 minute interval the agent handles
 - (i) exactly 5 calls,
 - (ii) more than 8 calls.(5)

The agent received some training to increase the number of calls handled per hour. During a randomly selected 30 minute interval after the training the agent handles 14 calls.

- (c) Test, at the 5% level of significance, whether or not there is evidence to support the suggestion that the rate at which the agent handles calls has increased. State your hypotheses clearly. (6)



7. A random variable X has probability density function given by

$$f(x) = \begin{cases} \frac{1}{2}x & 0 \leq x < 1 \\ kx^3 & 1 \leq x \leq 2 \\ 0 & \text{otherwise} \end{cases}$$

where k is a constant.

(a) Show that $k = \frac{1}{5}$ **(4)**

(b) Calculate the mean of X . **(4)**

(c) Specify fully the cumulative distribution function $F(x)$. **(7)**

(d) Find the median of X . **(3)**

(e) Comment on the skewness of the distribution of X . **(2)**



