

Please write clearly in block capitals.

Centre number

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Candidate number

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Surname

Forename(s)

Candidate signature

I declare this is my own work.

A-level MATHEMATICS

Paper 2

Wednesday 10 June 2020

Afternoon

Time allowed: 2 hours

Materials

- You must have the AQA Formulae for A-level Mathematics booklet.
- You should have a graphical or scientific calculator that meets the requirements of the specification.

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer each question in the space provided for that question. If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 100.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.

For Examiner's Use	
Question	Mark
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Section A

Answer **all** questions in the spaces provided.

- 1** Which one of these functions is decreasing for all real values of x ?

Circle your answer.

[1 mark]

$f(x) = e^x$

$f(x) = -e^{1-x}$

$f(x) = -e^{x-1}$

$f(x) = -e^{-x}$

- 2** Which one of the following equations has no real solutions?

Tick (✓) **one** box.

[1 mark]

$\cot x = 0$

☐

$\ln x = 0$

☐

$|x + 1| = 0$

☐

$\sec x = 0$

☐

3Find the coefficient of x^2 in the binomial expansion of $\left(2x - \frac{3}{x}\right)^8$ **[3 marks]**

Turn over for the next question**Turn over ►**

Using small angle approximations, show that for small, non-zero, values of x

where A is a constant to be determined.

[illegible]

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0 5

Use integration by substitution to show that

Fully justify your answer.

[illegible]

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6

$$5y + 12x = 298$$

A circle, C , has centre $(7, 9)$

L is a tangent to C .

6 (a)

Fully justify your answer.

[5 marks]

[illegible]

6 (b) Find the equation of C .

[3 marks]

Turn over for the next question

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7 a and b are two positive irrational numbers.

The sum of a and b is rational.

The product of a and b is rational.

Caroline is trying to prove $\frac{1}{a} + \frac{1}{b}$ is rational.

Here is her proof:

Step 1 $\frac{1}{a} + \frac{1}{b} = \frac{2}{a+b}$

Step 2 2 is rational and $a+b$ is non-zero and rational.

Step 3 Therefore $\frac{2}{a+b}$ is rational.

Step 4 Hence $\frac{1}{a} + \frac{1}{b}$ is rational.

7 (a) (i) Identify Caroline's mistake.

[1 mark]

7 (a) (ii) Write down a correct version of the proof.

[2 marks]



Prove by contradiction that the difference of any rational number and any irrational number is irrational.

[illegible]

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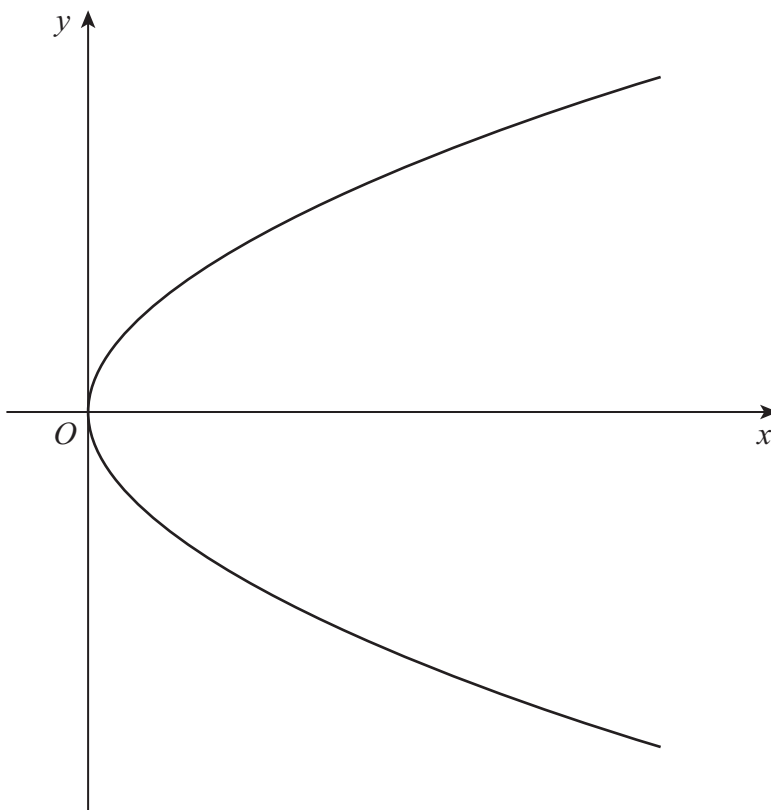


- 8** The curve defined by the parametric equations

$$x = t^2 \text{ and } y = 2t \quad -\sqrt{2} \leq t \leq \sqrt{2}$$

is shown in **Figure 1** below.

Figure 1



- 8 (a)** Find a Cartesian equation of the curve in the form $y^2 = f(x)$

[2 marks]

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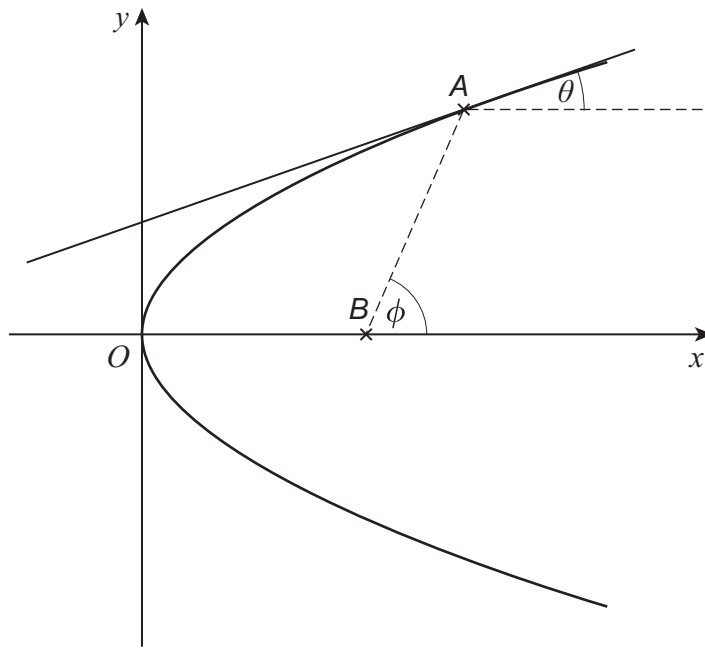


8 (b) The point A lies on the curve where $t = a$

The tangent to the curve at A is at an angle θ to a line through A parallel to the x -axis.

The point B has coordinates $(1, 0)$

The line AB is at an angle ϕ to the x -axis.



8 (b) (i) By considering the gradient of the curve, show that

$$\tan \theta = \frac{1}{a}$$

[3 marks]



8 (b) (ii) Find $\tan \phi$ in terms of a .

[2 marks]

8 (b) (iii) Show that $\tan 2\theta = \tan \phi$

[3 marks]

Turn over ►



$$V = \pi R^2 h - \pi h^3$$

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Fully justify your answer.

[illegible]

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Section B

Answer **all** questions in the spaces provided.

10

A vehicle is driven at a constant speed of 12 m s^{-1} along a straight horizontal road.

Only one of the statements below is correct.

Identify the correct statement.

Tick (✓) **one** box.

[1 mark]

The vehicle is accelerating

☐

The vehicle's driving force exceeds the total force resisting its motion

☐

The resultant force acting on the vehicle is zero

☐

The resultant force acting on the vehicle is dependent on its mass

☐
11

A number of forces act on a particle such that the resultant force is $\begin{pmatrix} 6 \\ -3 \end{pmatrix} \text{ N}$

One of the forces acting on the particle is $\begin{pmatrix} 8 \\ -5 \end{pmatrix} \text{ N}$

Calculate the total of the other forces acting on the particle.

Circle your answer.

[1 mark]

$$\begin{pmatrix} 2 \\ -2 \end{pmatrix} \text{ N}$$

$$\begin{pmatrix} 14 \\ -8 \end{pmatrix} \text{ N}$$

$$\begin{pmatrix} -2 \\ 2 \end{pmatrix} \text{ N}$$

$$\begin{pmatrix} -14 \\ 8 \end{pmatrix} \text{ N}$$



12

A particle, P , is moving with constant velocity $8\mathbf{i} - 12\mathbf{j}$

A second particle, Q , is moving with constant velocity $a\mathbf{i} + 9\mathbf{j}$

Q travels in a direction which is parallel to the motion of P .

Find a .

Circle your answer.

[1 mark]

−6

−5

5

6

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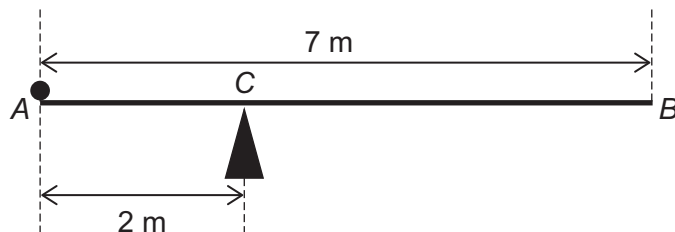


13

A uniform rod, AB , has length 7 metres and mass 4 kilograms.

The rod rests on a single fixed pivot point, C , where $AC = 2$ metres.

A particle of weight W newtons is fixed at A , as shown in the diagram.



The system is in equilibrium with the rod resting horizontally.

13 (a)

Find W , giving your answer in terms of g .

[2 marks]

13 (b)

Explain how you have used the fact that the rod is uniform in part (a).

[1 mark]



$$\mathbf{r} = (t^3 - 5t^2)\mathbf{i} + (8t - t^2)\mathbf{j}$$

[4 marks]

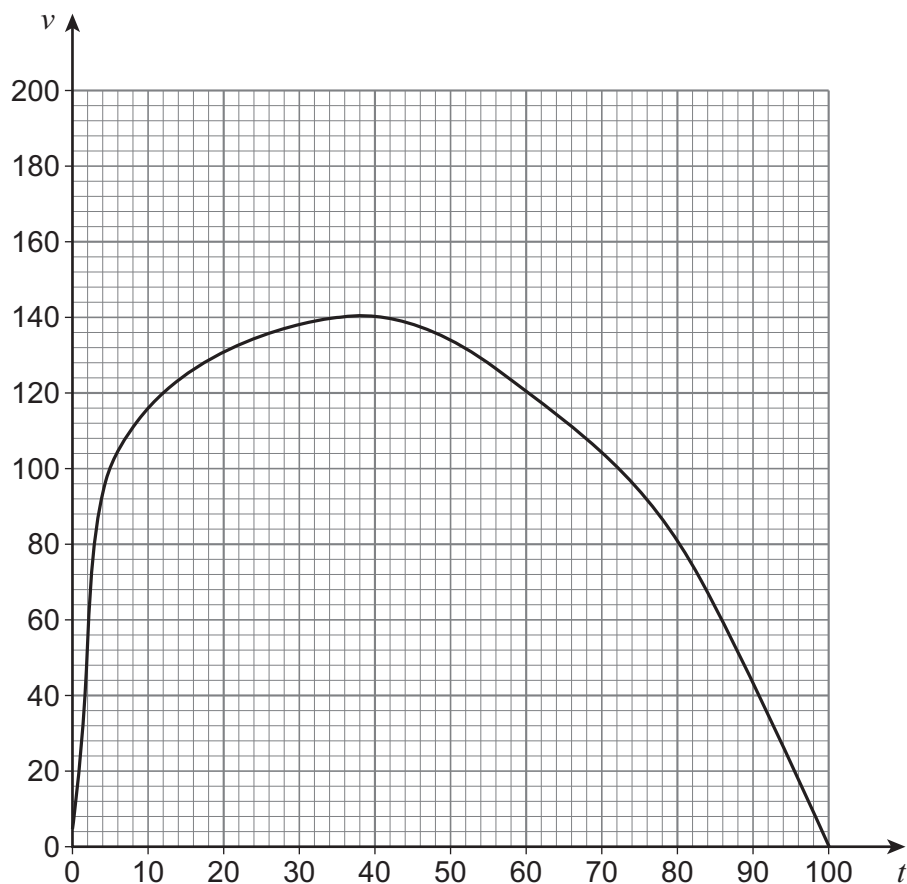
[illegible]

[3 marks]

[illegible]

15

A particle is moving in a straight line with velocity $v \text{ m s}^{-1}$ at time t seconds as shown by the graph below.

**15 (a)**

Use the trapezium rule with four strips to estimate the distance travelled by the particle during the time period $20 \leq t \leq 100$

[4 marks]



15 (b)

Over the same time period, the curve can be very closely modelled by a particular quadratic.

Explain how you could find an alternative estimate using this quadratic.

[1 mark]

Turn over for the next question

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16

Two particles A and B are released from rest from different starting points above a horizontal surface.

A is released from a height of h metres.

B is released at a time t seconds after A from a height of kh metres, where $0 < k < 1$

Both particles land on the surface 5 seconds after A was released.

Assuming any resistance forces may be ignored, prove that

$$t = 5(1 - \sqrt{k})$$

Fully justify your answer.

[5 marks]



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A ball is projected forward from a fixed point, P , on a horizontal surface with an initial speed $u \text{ m s}^{-1}$, at an acute angle θ above the horizontal.

You may assume the ball may be modelled as a particle and that air resistance may be ignored.

$$\sin 2\theta \geq \frac{dg}{u^2}$$
[illegible]

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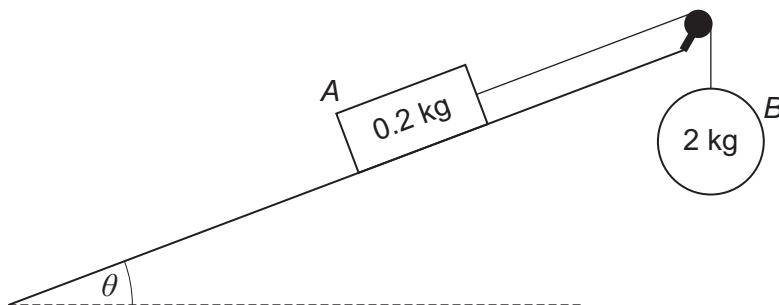
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18 Block A, of mass 0.2 kg, lies at rest on a rough plane.

The plane is inclined at an angle θ to the horizontal, such that $\tan \theta = \frac{7}{24}$

A light inextensible string is attached to A and runs parallel to the line of greatest slope until it passes over a smooth fixed pulley at the top of the slope.

The other end of this string is attached to particle B , of mass 2 kg , which is held at rest so that the string is taut, as shown in the diagram below.



18 (a) B is released from rest so that it begins to move vertically downwards with an acceleration of $\frac{543}{625} \text{ g m s}^{-2}$

Show that the coefficient of friction between A and the surface of the inclined plane is 0.17

[8 marks]

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[illegible]

When A reaches a speed of 0.5 m s^{-1} the string breaks.

18 (b) (i) Find the distance travelled by A after the string breaks until first coming to rest.

[4 marks]

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18 (b) (ii) State an assumption that could affect the validity of your answer to part (b)(i).

[1 mark]



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$$a = -0.1v^2$$

19 (a) By first forming a suitable differential equation, show that

$$v = \frac{20}{5 + 2t}$$

[6 marks]

[illegible]

19 (b) Find the acceleration of the particle when $t = 5.5$

[2 marks]

END OF QUESTIONS



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